

Modeling dispersion of partial discharges due to propagation velocity variation in power cables

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Abstract

Existing models for partial discharge (PD) propagation based on a single attenuation constant are unable to explain how each frequency component travels with a different propagation velocity. This paper proposes a new model based on a complex propagation term whose real component does not depend on the frequency (f), and whose imaginary part is modeled with a second order polynomial in f . The proposed model explains how the PD is attenuated, delayed, and dispersed due to the fact that each frequency component is differently delayed.

A closed-form expression is proposed for the PD peak value and width, and a method to derive the model parameters from a reference model existing in the bibliography. Simulation results show that the peak value and width of the propagated PD pulse are similar to those obtained with the proposed model. Additionally, the proposed model provides the velocity of each PD frequency component, which is crucial to get an accurate estimation of the PD source location.

The parameters of the proposed model have been estimated using a vector network analyzer for a XLPE cable. These results have been compared to the measurement obtained in a medium voltage test bench where intentionally induced PDs have been captured and processed, confirming the results of attenuation, delay and dispersion predicted by the proposed model.

Keywords: Partial discharges, propagation model, distribution MV cables.

1. Introduction

The observation of the phenomenon known as partial discharge (PD) in cables allows engineers to predict imminent failures in medium voltage (MV) distribution networks. Locating PD sources allows to identify the cable degraded areas and, preventively, replace it to avoid a power outage that could affect hundreds of subscribers.

To get an accurate location of the area where partial discharges are being generated, it is necessary to know how these PDs propagate along the cable. Published propagation models are based on classical transmission line (TL) approaches [1–5]. But these models have the following disadvantages:

- It is difficult to estimate their parameters, mainly due to the cable complex structure, as well as the lack of knowledge about the high frequency behavior of its materials [2].
- Existing propagation models for partial discharges, including those based on transmission lines, usually yield to a nearly constant propagation velocity [2, 6]. However, experimental results shown in [1] or [2] demonstrate that this velocity depends on the PD frequency components.

This dependence leads to dispersion, i.e the pulse spreads because each frequency component travels at a different propagation velocity [7]. It is well-known that dispersion has a significant effect on the pulse shape [8], as well as negative implications for PD location using techniques such as Time Domain Reflectometry (TDR) [3]. Dispersion has also negative effect on PD pattern classification and recognition [9].

- Understanding how the propagation velocity varies with frequency, or even with cable aging, is crucial for an accurate location of the PD source [5].

Dispersion is mainly due to the high frequency behavior of the semiconducting layer [8]. In addition, small variations of the characteristic impedance along the cable, especially due to aging, also leads to dispersion [5].

Dispersion is modeled in the bibliography by means of a TL model where the propagation term is a real value that linearly depends on the frequency [10]. Thus, dispersion appears because the high frequency components are highly attenuated. Consequently, the signal bandwidth is reduced, and the original PD shape is spread in the time domain. Since the propagation term is real, this model is unable to explain how each spectral component travels at a different speed.

Present techniques for fault location use those less attenuated spectral components to estimate the fault location. As the fre-

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quency components could change, even from experiment to experiment, due to changes in external conditions, or due to cable aging, assuming the same propagation velocity for every frequency component can yield a non-negligible error in the fault location.

This paper proposes a new propagation model for medium voltage cables. This model can be used to study the propagation of PDs, or even other transient phenomenon (lighting impulses, switching transients or breakdowns). It is based on the contributions of Marcuse in the field of light pulse propagation in single-mode optical fibers [11]. The proposed model approaches the attenuation term as frequency invariant, since the useful parts of the spectrum of the signals measured at the cable ends exhibit a low dependence with frequency. The phase term is approximated by a second order polynomial in frequency. This approximation allows to explain how the propagation velocity varies with frequency leading to dispersion.

A simple method valid for both, symmetric and asymmetric pulses, is proposed in this paper to estimate the model parameters from the reference model in [10]. The results obtained with the proposed model are compared by simulation to those obtained with the model of that reference.

The main advantage of the proposed model is that the model parameters can be estimated from experimental measurements, and two methods are proposed here. The first one uses a vector network analyzer (VNA) to measure the frequency response of a cable sample. In the second technique, partial discharges are captured in a degraded cable and digitally processed to measure the pulse dispersion due to cable propagation. Experimental results obtained with a XLPE MV cable are shown to illustrate these methods.

This paper is organized in 5 additional sections. Section 2 describes the proposed propagation model for both, symmetric and asymmetric pulses. Section 3 describes how to extract the model parameters from the reference model described in [10]. Section 4 illustrates how the proposed model agrees with the experimental measurements. In section 5 we discuss some key aspects related to location of partial discharges that can be addressed with the proposed model. Finally, some conclusions are drawn in section 6.

2. Proposed propagation model

A transfer function $H(\omega, L)$, shown in (1), is proposed to model the propagation of PDs in MV cables. In (1), $\gamma(\omega)$ is the complex propagation term, and L is the propagated distance.

$$H(\omega, L) = \exp(-\gamma(\omega)L) \quad (1)$$

where: $\gamma(\omega) = \alpha_0 + j\beta(\omega)$.

The real part of the propagation term, α_0 , is responsible for PD power reduction in $8.68\alpha_0$ dB/m. A typical value for α_0 is 0.03 dB/m.

Concerning the imaginary part of the propagation term, or phase term $\beta(\omega)$, it models the phase variation due to propagation. Term $\beta(\omega)$ determines the propagation velocity, the propagation delay, and is responsible for pulse dispersion. Unlike

most of the models proposed in the literature, which assume $\beta(\omega)$ to have a linear dependence with ω , the model proposed here assumes a quadratic dependence with ω as shown in (2).

$$\beta(\omega) = \beta_0 + \beta_1\omega + (1/2)\beta_2\omega^2, \quad (2)$$

where: $\beta_1 = \partial\beta/\partial\omega|_{\omega=0}$ and $\beta_2 = \partial^2\beta/\partial\omega^2|_{\omega=0}$.

Delay constant β_1 is responsible for the delay (also called group delay) of the initial pulse after travelling a distance L . The propagation time $t_p = \beta_1 L$ can be considered to be the mean value of the propagation delay of every spectral components in the propagated pulse. Constant β_2 , or dispersion constant, is responsible for the spreading of the initial pulse shape due to the fact that each spectral component propagates at a different speed.

2.1. Gaussian pulses

Expression (3) models an initial gaussian pulse with amplitude and deviation A_0 and σ_0 , respectively. Figure 4(a) shows this signal. Using the proposed propagation model, the resulting propagated pulse at a distance L is shown in (4), where it can be observed that: a) the resulting pulse is gaussian too; b) it has been attenuated (A_L is the resulting peak value and even if we consider a non dissipative ($\alpha_0 = 0$) medium, the peak value would be reduced due to dispersion if $\beta_2 \neq 0$); c) it has been phase delayed in an amount of θ_L radians; d) it has been time delayed t_p seconds; and e) it has been dispersed along the cable: the original deviation σ_0 has grown up to σ_L due to dispersion.

$$v(t, 0) = A_0 \exp(-t^2/2\sigma_0^2). \quad (3)$$

$$v(t, L) = A_L \exp(-j\theta_L) \exp(-(t - t_p)^2/2\sigma_L^2), \quad (4)$$

where:

$$\begin{aligned} \sigma_L &= (\sigma_0^2 + \beta_2^2 L^2 / \sigma_0^2)^{1/2}, \\ A_L &= A_0 \sigma_0 (\sigma_0^4 + \beta_2^2 L^2)^{-1/4} \exp(-\alpha_0 L), \\ \theta_L &= \beta_0 L + \arctan(\beta_2 L / 2\sigma_0^2) - \dots \\ \beta_2 L / 2 &= (\sigma_0^4 + \beta_2^2 L^2), \text{ and} \\ t_p &= \beta_1 L. \end{aligned}$$

2.2. Asymmetric pulses

The skewed nature of the PD pulse is modeled in [10] by means of a sum of delayed gaussian functions. Using N_G components, the resulting pulse waveform is given in (5), where $A_{0,k}$, $\sigma_{0,k}$, and $\tau_{0,k}$ are the peak, typical deviation, and delay values of the gaussian component k , respectively. Figure 6(a) shows the asymmetric pulse generated using this model.

$$v(t, 0) = A_p \sum_{k=1}^{N_G} A_{0,k} \exp(-(t - \tau_{0,k}) / (2\sigma_{0,k}^2)), \quad (5)$$

where:

$$\begin{aligned} A_{0,k} &= 0.2245 \exp(-k/10), \\ \tau_{0,k} &= 10^{-9}(k + 5000), \text{ and} \\ \sigma_{0,k} &= 10^{-9} \exp(k^{0.25}) / \sqrt{2}. \end{aligned}$$

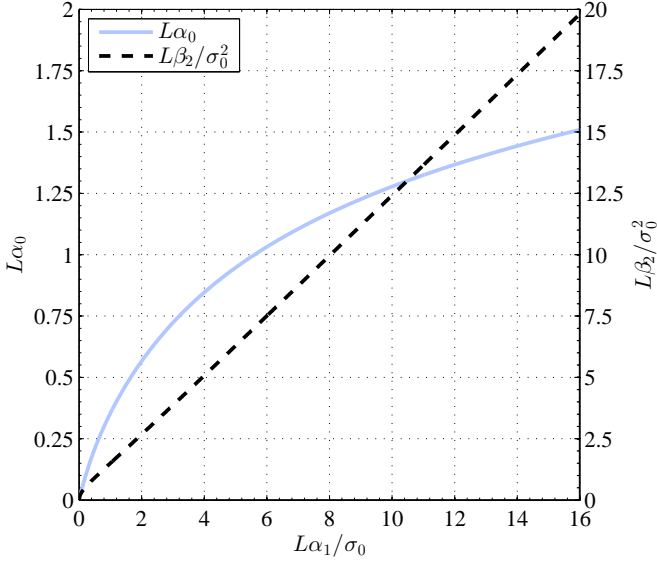


Figure 1: Relationship between the proposed and the Oussalah model: $L\alpha_0$ and $L\beta_2/\sigma_0^2$ are the adimensional attenuation and dispersion constants of the proposed model, respectively. $L\alpha_1/\sigma_0$ is the attenuation constant of the model defined in [10].

Assuming that the propagation medium is linear, the expression in (6) describes the L meter propagated asymmetric pulse, where α_0 , β_1 , and β_2 are the attenuation, delay, and dispersion constants of the proposed method. The resulting $v(t, L)$ signal is composed of N_G gaussian components, where $A_{L,k}$, $\sigma_{L,k}$, and $\tau_{L,k}$ are the amplitude, deviation, and delay of the k -th component, respectively.

$$v(t, L) = A_p \sum_{k=1}^{N_G} A_{L,k} \exp(-(t - \tau_{L,k})/(2\sigma_{L,k}^2)), \quad (6)$$

where:

$$\begin{aligned} A_{L,k} &= A_{0,k} \exp(-\alpha_0 L) \sigma_{0,k} (\sigma_{0,k}^4 + \beta_2^2 L^2)^{-1/4}, \\ \sigma_{L,k}^2 &= \sigma_{0,k}^2 + (\beta_2 L / \sigma_{0,k})^2, \\ \tau_{L,k} &= \tau_{0,k} + \beta_1 L. \end{aligned}$$

3. Model fitting

This section proposes a procedure to estimate the attenuation (α_0) and dispersion (β_2) constants of the proposed model, from the (also called) attenuation constant (α_1) of the model proposed by Oussalah *et al.* in [10]. Let's remind that the Oussalah model considers a real propagation term $\gamma(\omega) = \alpha_1 \omega$, where parameter α_1 is called the attenuation constant.

The dispersion constant β_2 of our model is computed by equalling the expressions for the deviation σ_L in both models. The numerical solution in a graphical way is shown in Figure 1, where the adimensional dispersion constant ($L\beta_2/\sigma_0^2$) of the proposed model is depicted versus the adimensional attenuation constant ($L\alpha_1/\sigma_0$) of the Oussalah model.

The expressions of the peak values (A_L) are used in both models to derive the attenuation constant α_0 . Figure 1 also

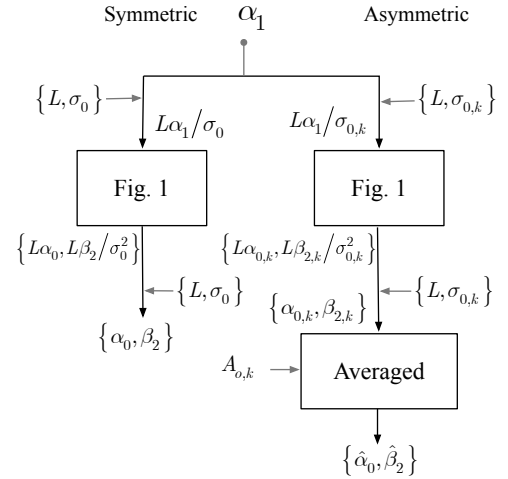


Figure 2: Flowchart to estimate the attenuation (α_0) and dispersion (β_2) constants of the proposed model from the (also called) attenuation constant α_1 proposed in [10]. Two different flows are shown for the symmetric and asymmetric pulses.

shows the adimensional attenuation constant ($L\alpha_0$) of the proposed model versus the adimensional attenuation constant ($L\alpha_1/\sigma_0$) of the reference one. Note that, in order to estimate α_0 , we need the previously estimated value of β_2 . The delay constant β_1 cannot be derived from the Oussalah model since the propagation delay is ignored in that approach.

The following subsections describes the procedure to obtain the attenuation and dispersion constants for both, symmetric and asymmetric pulses. The flow diagram of Figure 2 summarizes the proposed procedure.

3.1. Symmetric pulse

Once α_1 is known, and accounting for the initial deviation σ_0 that determines the spectral components of the original pulse, the following procedure is proposed to estimate the model parameters for the symmetric case (see Figure 2):

1. Compute the adimensional attenuation constant of the Oussalah model, choosing any value of L in the abscissa of Figure 1. For example, for a MV cable with $\alpha_1 = 4e-11 \text{ s m}^{-1}$, using a gaussian pulse with $\sigma_0 = 2 \text{ ns}$, at $L = 300 \text{ m}$, the resulting adimensional attenuation constant of the Oussalah model is $L\alpha_1/\sigma_0 = 6$. The selected value for σ_0 is especially important to estimate α_0 , and it is related to the transient phenomenon under study. The selected one is widely used for partial discharges in cables.
2. The parameters of the proposed model will be estimated using Figure 1. For the above example, the resulting value of the dispersion and attenuation adimensional constants are, respectively: $L\beta_2/\sigma_0^2 = 7.50$, and $L\alpha_0 = 1.03$. Then, the estimated model parameters are: $\alpha_0 = 3.44e-3 \text{ m}^{-1}$ and $\beta_2 = 0.10 \text{ ns}^2 \text{ m}^{-1}$.

3.2. Asymmetric pulses

As the constants α_0 and β_2 are conditioned by the initial pulse deviation σ_0 , we will derive as many values of these

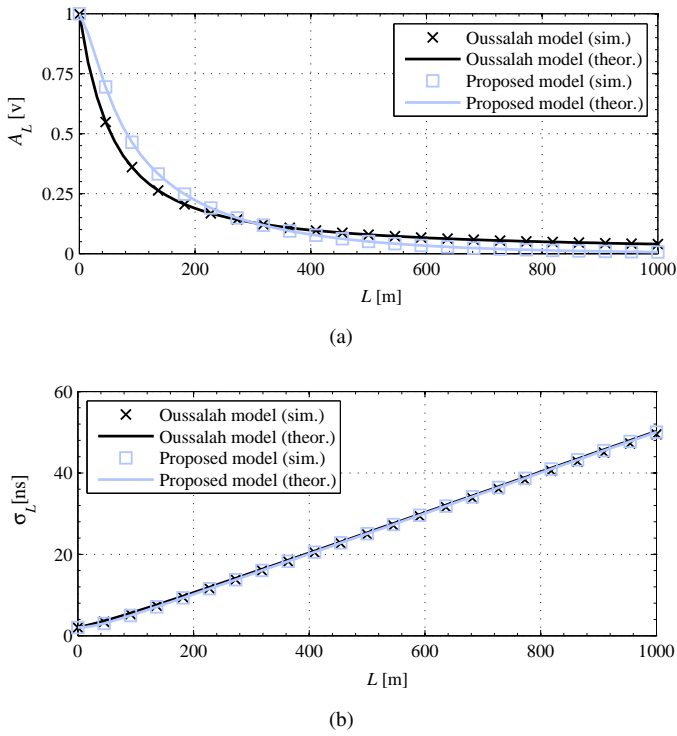


Figure 3: Simulation of: (a) peak value, and (b) deviation, versus distance for symmetric pulse propagation.

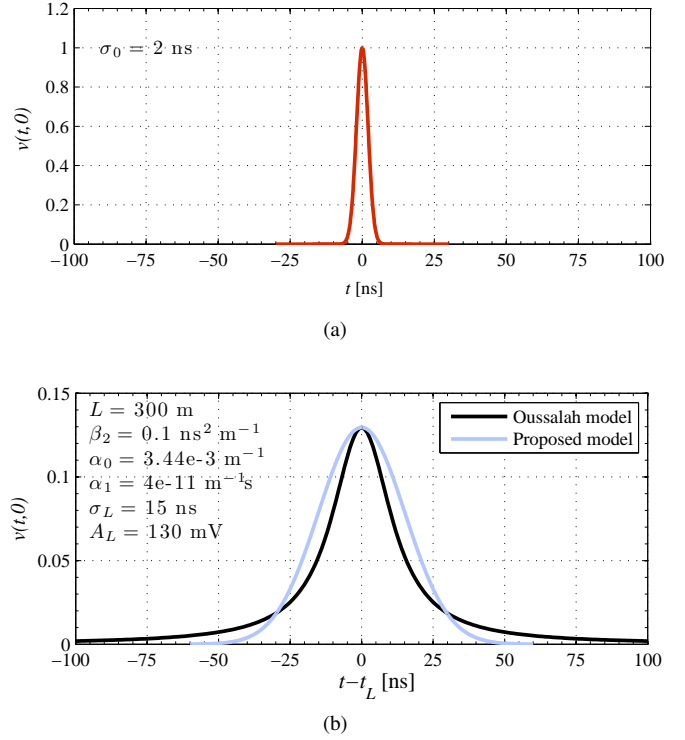


Figure 4: Example of symmetric pulse propagation: (a) initial pulse, (b) pulse shape after 300 meters of propagation. $t_L = t_p(L = 300)$ is the propagation delay.

constants as the number of gaussian components used to initially build the asymmetrical pulse. Let $\alpha_{0,k}$ and $\beta_{2,k}$ be the propagation constants for the k -th component of the proposed model derived with the same constant α_1 , and using the initial deviations $\sigma_{0,k}$. For example: using a MV cable with $\alpha_1 = 4 \text{e-}11 \text{ m}^{-1} \text{ s}$, the resulting attenuation constants are in the interval $\alpha_{0,1} = 3.5 \text{e-}3 \text{ m}^{-1}$ to $\alpha_{0,60} = 1.22 \text{e-}3 \text{ m}^{-1}$, while the dispersion constants are in the range from $\beta_{2,1} = 9.62 \text{e-}2 \text{ ns}^2 \text{ m}^{-1}$ to $\beta_{2,60} = 6.78 \text{e-}1 \text{ ns}^2 \text{ m}^{-1}$.

A simplified model for the asymmetric pulse propagation is also proposed here where the N_G pairs of propagation constants $\{\alpha_{0,k}, \beta_{2,k}\}$ are replaced by a single pair of averaged propagation constants $\{\hat{\alpha}_0, \hat{\beta}_2\}$. They are computed as shown in (7) and (8), where the propagation constants have been averaged and weighted with the component amplitude of each gaussian component $A_{0,k}$. The resulting values for the example above are: $\hat{\alpha}_0 \approx 2.54 \text{e-}3 \text{ m}^{-1}$ and $\hat{\beta}_2 \approx 0.21 \text{ ns}^2 \text{ m}^{-1}$

$$\hat{\alpha}_0 = \frac{\sum_{k=1}^{N_G} \alpha_{0,k} A_{0,k}}{\sum_{k=1}^{N_G} A_{0,k}} \quad (7)$$

$$\hat{\beta}_2 = \frac{\sum_{k=1}^{N_G} \beta_{2,k} A_{0,k}}{\sum_{k=1}^{N_G} A_{0,k}} \quad (8)$$

3.3. Simulation results

The propagation of a gaussian pulse has been simulated in a cable using both, the transfer function proposed in this paper,

and the model presented in [10]. The initial peak value of the gaussian pulse is $A_0 = 1 \text{ V}$, and its initial deviation is $\sigma_0 = 2 \text{ ns}$. The proposed model is configured with $\alpha_0 = 3.4 \text{e-}3 \text{ m}^{-1}$, and $\beta_2 = 0.1 \text{ ns}^2 \text{ m}^{-1}$. The Oussalah model uses $\alpha_1 = 4 \text{e-}11 \text{ m}^{-1} \text{ s}$. Figure 3 draws the peak value A_L and deviation σ_L versus L , for the proposed and the Oussalah models. For comparison purposes this figure also shows the theoretical behavior of those variables given in (4) and [10].

To obtain the simulated results, the value of the transfer function in every model was computed for every distance L ; this value was multiplied by the Fourier transform of the initial pulse, and the resulting function was anti-transformed to the time domain. Finally, the peak and deviation values were estimated by means of the gaussian function that fits the best the simulation results. Note that the Oussalah model provides a non-gaussian shaped function.

Simulated peak values depicted in Figure 3(a) shows that: 1) simulation and theoretical results are very similar, even though the Oussalah model provides a pulse which is symmetrical but not gaussian; and 2) both simulated models perform similarly, especially for $L > 400$ m. Furthermore, the values of the deviation σ_L for both models, obtained by simulation, are shown in Figure 3(b), along with their theoretical values. This figure shows that these four values (theoretical and simulated ones for each model) are almost equal in the distance interval analyzed here.

For the sake of visual comparison, Figure 4(b) shows the shape of the initial pulse (in Figure 4(a)) after having travelled

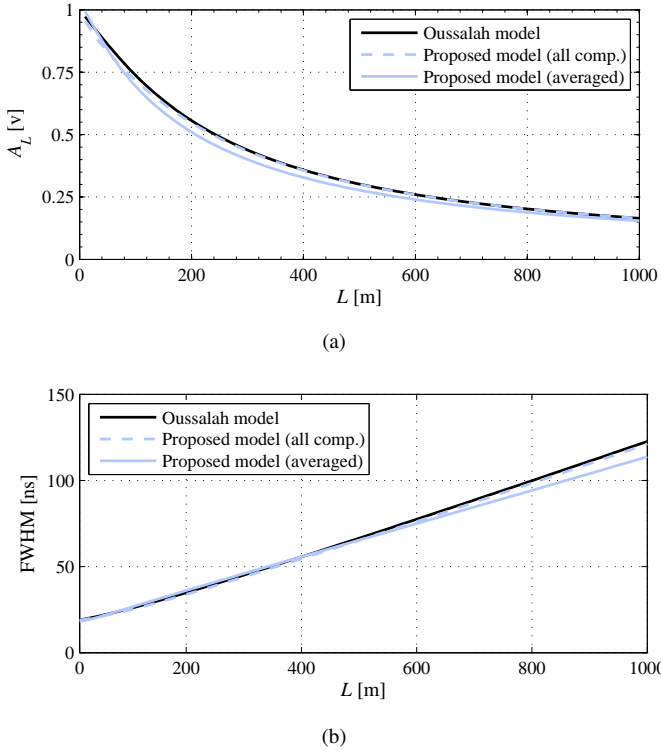


Figure 5: Simulation of: (a) peak value, and (b) FWHM, versus distance for asymmetric pulse propagation.

300 meters, for both, the proposed and the Oussalah models. In this figure we can see that both pulses have the same peak value (0.13 V), and the same deviation ($\sigma_L = 15$ ns). The pulse shape of the proposed model is gaussian while the other one is symmetric but not gaussian.

In order to validate the proposed model for asymmetric pulses, the propagated pulse is rebuilt from the resulting amplitudes and deviations of the k -th gaussian component, $A_{L,k}$ and $\sigma_{L,k}$, respectively. To obtain the propagation constants, the method proposed in Section 3 has been used with, both, a set of N_G propagation constants $\{\alpha_{0,k}, \beta_{2,k}\}$, and a single pair of averaged propagation constants $\{\hat{\alpha}_0, \hat{\beta}_2\}$. Once the pulse has been rebuilt, its peak and width values were estimated. To compute the pulse width, the FWHM (*Full Width Half Maximum*) value has been used, due to the asymmetric nature of the pulse shape. For L high enough, the pulse becomes symmetric, so that it can be approximated by a gaussian function. In that case, $\text{FWHM} \approx 2.35\sigma$, where σ is the gaussian pulse deviation.

The peak value A_L and the FWHM pulse width versus distance L are shown in Figure 5, for both, the model described in [10] and the proposed model. We can observe that both models behave almost identical, even when the averaged propagation constants $\hat{\alpha}_0$ and $\hat{\beta}_2$ are used.

Figure 6 shows the shapes of an initially asymmetric pulse that propagates according to the proposed model and the model of reference [10]. In Figure 6 (a) we can see the initial asymmetric pulse, with a FWHM pulse width of 18 ns and a peak value of 1 V. Figure 6(b) depicts the symmetric pulse shape

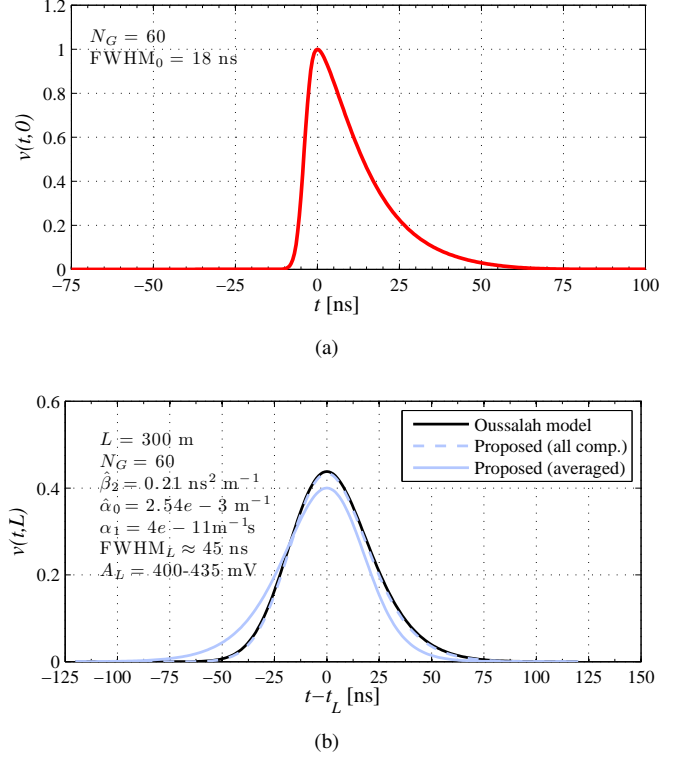


Figure 6: Example of asymmetric pulse propagation: (a) initial pulse, (b) pulse shape after 300 meters of propagation. $t_L = t_p(L = 300)$ is the propagation delay.

after having been propagated $L = 300$ m, using the proposed model with the full set of propagation constants, the proposed model with the averaged value of the propagation constants, and the Oussalah model. The proposed model provides a pulse shape similar to the results obtained in [10]. Slight differences can be found in the peak value (0.40 vs. 0.43) when the averaged model is used, but the resulting FWHM pulse widths have a similar value (44 ns) in any case.

4. Experimental results

4.1. VNA measurements

Using a VNA the scattering parameter S_{21} of a 42.5 m long new MV XLPE cable has been measured, in order to estimate the attenuation term $\alpha(f)$ and the phase term $\beta(f)$ of its transfer function. The lower bound of the frequency interval is set to 1 MHz, as the current transformers used to measure the partial discharges reject lower frequency components. Despite PD spectral components can initially reach up to GHz, propagation makes the highest components to become extinct in a few meters [8]. Setting the upper limit to 50 MHz, a proper frequency range is selected.

The experimental results have been fitted in the minimum mean squared error sense, regarding the estimation of the attenuation, delay, and dispersion constants ($\alpha_0, \beta_1, \beta_2$) for the proposed model, and the attenuation constant (α_1) for the model of reference [10]. These results are shown in Table 1. Note that

the measured dispersion constant β_2 is negative, indicating that the group propagation velocity increases with frequency.

A similar MV cable was simulated in [8], providing a velocity versus frequency curve. Selecting some points of this curve, we have estimated β_1 in the interval [5.7, 6.2] ns/m, which decreases with frequency in the spectral interval under study, and $\beta_2 = -0.796 \text{ ns}^2\text{m}^{-1}$. Simulation results obtained in that paper are close to those experimentally obtained here; moreover, the value estimated for α_1 is also similar to that reported in [10] for XLPE cables.

By following the procedure described above, the measured α_1 is now used to adjust the proposed model. Using an initial deviation $\sigma_0 = 5 \text{ ns}$, we obtain $\alpha_0 = 4.40\text{e-}3 \text{ m}^{-1}$ and $|\beta_2| = 0.491 \text{ ns}^2\text{m}^{-1}$. Note that the proposed method is unable to resolve whether the sign of the dispersion constant is positive or negative.

4.2. Partial discharge measurements

In this section we describe the results obtained in a medium voltage test bench, where a XLPE cable was stressed at operating conditions (18 kV) without load. The dielectric was artificially damaged in a small region close to one of the cable ends until partial discharges appeared. These PDs were acquired at both cable ends, and properly processed to estimate the model parameters.

4.2.1. Scheme of reference

The diagram of Figure 7 shows the scheme of reference. Two current transformers were installed at both cable ends. These components are broadband inductive sensors that are responsible for sensing the PD pulses. According to standard [12], the selected sensor was an ultra wide band coupler.

The cable was degraded by drilling holes that affected the thermoplastic sheath, the semiconducting layer, and the insulation. In Figure 7, the degraded area was located L_1 meters from one of the ends, labeled as *Near End*, and L_2 meters from the other one (labeled as *Far End*). As shown in Figure 7, $L_2 \gg L_1$ is assumed.

In Figure 7 $x(t, 0)$ is the original PD signal, and signals $x(t, -L_1)$ and $x(t, L_2)$ are the signals captured by sensors located at the near and far ends, respectively. Both signals are acquired synchronously using a digital oscilloscope triggered by the near end signal. The sample frequency was set to 500 MHz, and a proper dynamic range for each channel was selected. Captured signals were stored to be off-line processed.

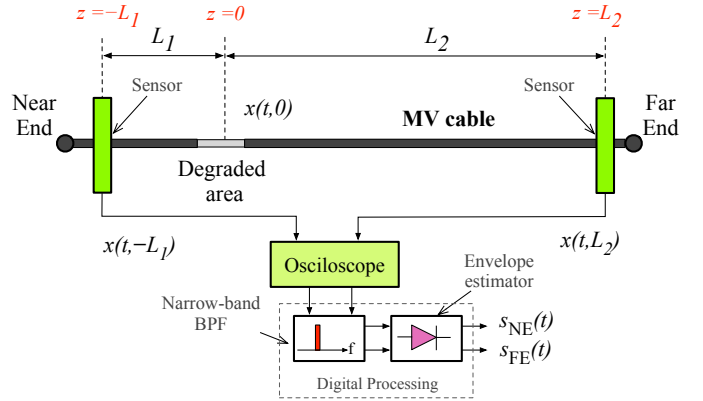


Figure 7: Test bench description, and definition of main variables

4.2.2. Digital processing

Digital processing was used to estimate the delay and dispersion due to propagation along the cable of a small spectral interval of the PD signal. A narrow band pass filter (NB-BPF) is used whose center frequency f_c is tunable. The selected impulse response is finite and gaussian, providing a linear phase response. When the wide-band signal $x(t, -L_1)$ is filtered, the resulting spectrum is also gaussian, centered in the same frequency, and with the same bandwidth as the filter. On the other hand, when the far end signal $x(t, L_2)$ is filtered, we should obtain a signal whose frequency domain spectrum is conformed by the cable response as well as by the filter. The resulting signals are shifted to the baseband from f_c by means of an envelope estimation. Thus, signals $s_{NE}(t)$ and $s_{FE}(t)$ are the baseband near end and far end envelopes, respectively.

4.2.3. Experimental estimation of α_0 , β_1 , and β_2

The attenuation, delay, and dispersion constants of the proposed model can be extracted from the baseband signals $s_{NE}(t)$ and $s_{FE}(t)$. The solution is only valid for a small frequency interval around the center frequency f_c . The linear effects coming from sensors, capture system, and digital processing are unbiased since they affect in the same way to both signals.

To compute the attenuation constant expression (9) was used, where P_{NE} and P_{FE} are the powers of signals $s_{NE}(t)$ and $s_{FE}(t)$, respectively. To estimate the delay constant, the delay between the near and far end envelopes (Δt_d) was detected using a simple cross-correlation method. Constant β_1 was calculated according to (10).

$$\alpha_0 = \ln(P_{NE}/P_{FE})/2(L_2 - L_1) \quad (9)$$

$$\beta_1 = \Delta t_d/(L_2 - L_1) \quad (10)$$

We can estimate the dispersion constant β_2 in two different ways:

1. By measuring the delay constant β_1 for each center frequency f_c . Then, β_2 can be estimated by computing the derivative of β_1 with respect to frequency. This technique is inaccurate, as β_2 has not a significant effect on

Table 1: Summary of experimental results: using a vector network analyzer, and measuring the PDs as described in section 4.2

Method	α_1 [s m ⁻¹]	α_0 [m ⁻¹]	β_1 [ns m ⁻¹]	β_2 [ns ² m ⁻¹]
VNA	5.16e-11	3.37e-3	5.72	-0.7121
Direct PD measure	n/a	3.40e-3	5.92	±0.761

the propagation delay. For example, for a 300 m long cable with $\beta_2 = 0.5\text{ns}^2\text{m}^{-1}$, and considering a spectral interval of 5 MHz, the group delay is expected to shift $\pm(0.5 \cdot 2\pi \cdot 5\text{e}6) \cdot 300 = \pm 4.7\text{ns}$. That is, less than 3 samples using the sampling frequency of our test bench.

2. We can also estimate the dispersion constant by measuring the PD dispersion, i.e. measuring the spreading of the PD pulse due to propagation along the cable. This dispersion is also observed in signals $s_{NE}(t)$ and $s_{FE}(t)$. This technique was chosen here to estimate β_2 .

Expression (11) shows the proposed formulae for the deviation of the near and far end baseband signals (σ_{NE} and σ_{FE} , respectively). In this expression, σ_0 is the initial PD deviation (assuming it is gaussian), σ_s is the dispersion due to the sensor used to capture the PD signal (we assume that its impulse response is also gaussian and similar in both ends), and σ_{NBPF} is the deviation of the gaussian impulse response of the narrow band pass filter (equal in both ends). It should be noted that the digital filters do not disperse the PD as their phase response is linear but, as its frequency response is band-limited, they will spread the incoming pulses.

Although in (11) σ_0 is unknown, it can be indirectly estimated using an additional signal measurement: the signal captured at the cable near end. The deviation of this signal (σ_1) is approximated in (13). Combining (12) and (13) we obtain an expression for the initial deviation σ_0 in (14). This approximation is valid when L_1 is large enough so as to make the captured pulse to become symmetrical, and assuming that the impulse response of the selected sensor also behaves gaussian.

$$\sigma_{NE}^2 = \sigma_0^2 + (\beta_2 L_1 / \sigma_0)^2 + \sigma_s^2 + \sigma_{NBPF}^2, \quad (11)$$

$$\sigma_{FE}^2 = \sigma_0^2 + (\beta_2 L_2 / \sigma_0)^2 + \sigma_s^2 + \sigma_{NBPF}^2.$$

$$\sigma_{FE}^2 - \sigma_{NE}^2 = (L_2^2 - L_1^2)(\beta_2 / \sigma_0)^2 \quad (12)$$

$$\sigma_1^2 = \sigma_0^2 + (\beta_2 L_1 / \sigma_0)^2 + \sigma_s^2 \quad (13)$$

$$\sigma_0^2 = \sigma_1^2 - \sigma_s^2 - (\sigma_{FE}^2 - \sigma_{NE}^2)(L_1^2 / (L_2^2 - L_1^2)) \quad (14)$$

4.2.4. Results

The test bench of Figure 7 has been built with $L_1 = 1.5$ m and $L_2 = 304$ m. The cable was artificially damaged until a high frequency activity due to PDs in the degraded area was observed. The center frequency was tuned to $f_c = 3$ MHz with a FWHM bandwidth of 1 MHz (the equivalent time response deviation is $\sigma_{BPF} = 0.37\mu\text{s}$). This center frequency was selected because the signal level measured at the far end was high enough when compared to other spectral components.

The FWHM bandwidth of the selected current transformer, measured with a VNA, was 50 MHz (the equivalent time domain deviation is $\sigma_s = 7.51$ ns). It was observed that frequency components below 1 MHz were highly attenuated.

During the test campaign, thousands of partial discharges were captured. Each test sequence provided about 4610 captures that were considered as valid, and they were later processed to estimate the proposed model parameters.

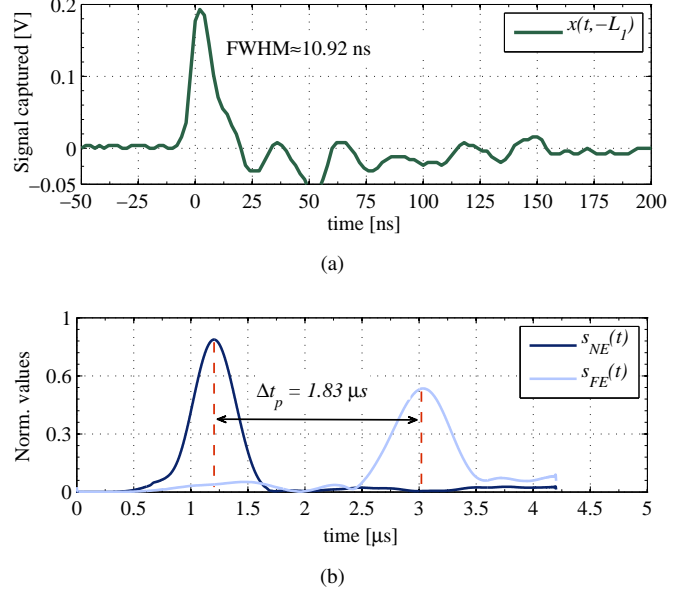


Figure 8: Example of measured PD signal: (a) near end signal, (b) baseband envelopes.

Figure 8(a) shows, as an example, the near end signal $x(t, -L_1)$, which exhibits a FWHM pulse width of 10.92 ns and a peak value of 200 mV. The resulting near and far end baseband signals are shown in Figure 8(b), where the estimated delay between them is also displayed. It is evident that $s_{FE}(t)$ is spread when compared to $s_{NE}(t)$.

The power of the baseband envelopes was estimated and, using (9), the attenuation constant was estimated to be $\alpha_0 = 3.401\text{e-}3$. The delay between these signals was also measured, and using (Δt_p), the resulting delay constant was $\beta_1 = 5.922$ ns m^{-1} . The resulting mean value of β_2 was 0.76 ns $^2\text{m}^{-1}$, with a standard deviation of 0.19 ns $^2\text{m}^{-1}$. Note that the proposed method is unable to estimate the sign of the dispersion constant, although it is easy to determine it.

Before the computation of β_2 , σ_0 was estimated using (14), and the measured values of σ_{NE} and σ_{FE} . The measured mean value of the initial deviation σ_0 was 1.79 ns with a standard deviation of 0.37 ns (see Figure 9(a)). In addition, the histograms of the measured deviation of the baseband signals shown in Figure 9(b) clearly exhibit the dispersion (or pulse spread) due to propagation. This histogram shows that the near end baseband signal is narrower (188 ns) than the far end one (229 ns).

5. Discussion

This section discusses some issues related to propagation that affect PD source location techniques accuracy in MV cables.

5.1. Excessive attenuation at certain frequencies

During the test campaign, some spectral components were observed to be highly attenuated at the far end. Additional factors, such as resonances or signal coupling, are responsible for some components to be extinguished. As a consequence, these components are not suitable to be used for PD source location.

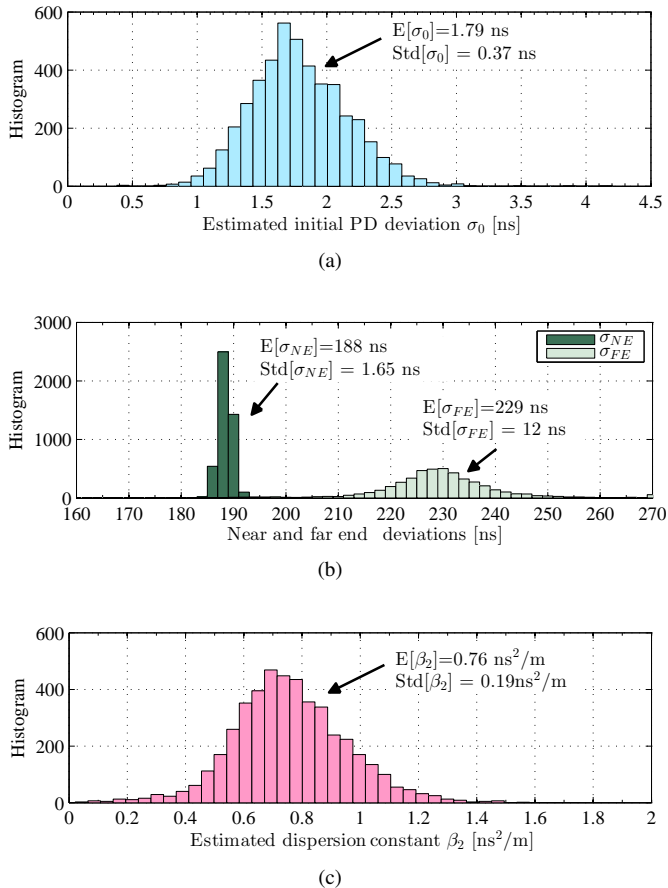


Figure 9: Experimental results: (a) histogram of the estimated PD initial deviation σ_0 ; (b) histograms of baseband signals envelope deviations σ_{NE} and σ_{FE} ; and (c) histogram of the measured dispersion constant β_2 .

The method proposed in Figure 7 allows us to select the most suitable spectral components for source location.

5.2. Attenuation and dispersion

In [10] an expression for A_L is proposed that takes into account the dissipative phenomenon that occurs in the cable. We propose an alternative expression for A_L in (4), where we can distinguish two terms: a dissipative term, that depends on the attenuation constant α_0 , and a dispersive term, that depends on the dispersion constant β_2 . Figure 10 depicts the evolution of both terms versus distance. We can observe that, when propagated distances are below 300 m (most of urban MV infrastructure), both terms are comparable. In those cases, the effect of dispersion in PD source location cannot be neglected.

5.3. Attenuation dependence with frequency

A PD is, in its early stage, a very fast phenomenon (it lasts for only a few nanoseconds, typically). Along the cable propagation, higher frequency components are attenuated due to conductor and dielectric losses, and particularly, due to the high frequency properties of the semiconducting layer. That is the reason why many papers in the literature model the real part of the propagation term as highly dependent on frequency (linear in the case of [10]).

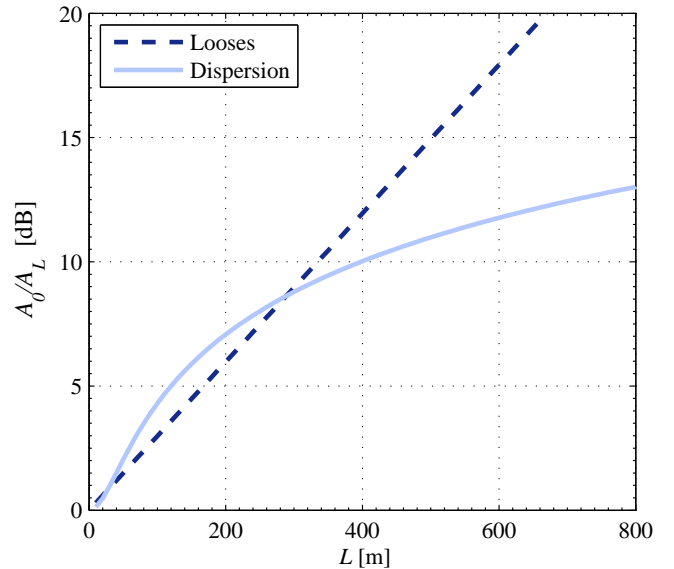


Figure 10: Peak value reduction due to attenuation and dispersion using a cable with $\alpha_0 = 3.44e-3 \text{ m}^{-1}$ and $\beta_2 = 0.10 \text{ ns}^2\text{m}^{-1}$.

The attenuation of higher frequency components due to propagation is responsible for the fact that only a small interval of the original PD spectrum reaches the cable ends where the PD sensors are installed. Although the attenuation constant is known to be dependent on frequency ([13]), an averaged value of the attenuation constant α_0 can be computed in the bandwidth of interest. This averaging process should take into account the PD spectral components and the instrumentation, if they are known from actual measurements or can be estimated from previous measurements.

For example: in a XLPE cable 500 meters long with $\alpha_1 = 4e-11 \text{ s/m}$, components located at 500 MHz, 100 MHz and 50 MHz would be attenuated 546 dB, 109 dB and 56 dB, respectively. Then, the effective bandwidth of the captured PD signal useful for post-processing is limited to something less than 50 MHz, although the bandwidth of the original signal is much greater in the origin. Even more, if the low pass behavior of the sensors is taken into account, the useful part of the spectrum will be further reduced. In this *effective* bandwidth we propose to simplify the attenuation to be frequency invariant.

5.4. Delay and dispersion constants

The VNA shows a negative dispersion constant in the measured spectral interval. Thus, the propagation velocity increases with frequency.

But the measured values for β_2 are so small that the expected variation in the propagation velocity is negligible from one spectral component to another (inside the captured bandwidth). In terms of propagation delay, two spectral components separated Δf will be relatively delayed $\Delta t_p = 2\pi L \Delta f |\beta_2|$ where L is the propagated distance. For example, using the measured β_2 in a 500 m long cable with $\Delta f = 20 \text{ MHz}$, a Δt_p of 6 ns is obtained. In terms of travelled distance, it is hardly one meter. This figure could make us to conclude that dispersion is

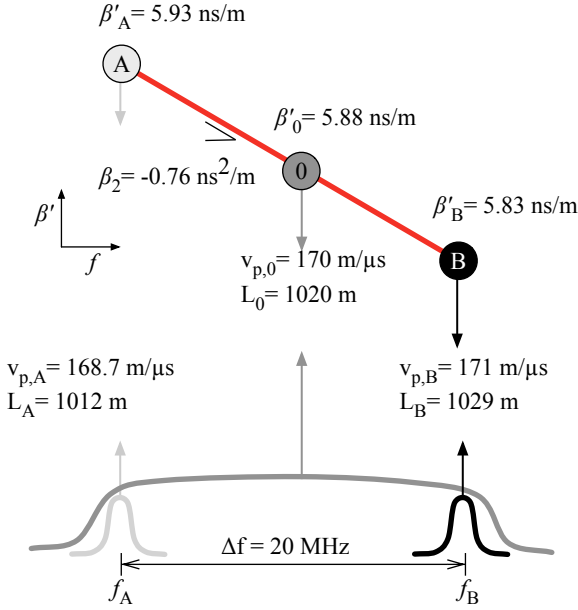


Figure 11: Example of propagation velocity variation due to non zero dispersion coefficient β_2 .

irrelevant to PD source location.

We have observed that, in some frequency components, the phase term exhibits a significant non linear behavior leading to a higher value of β_2 . Then, the variation of the propagation velocity from one frequency component to another is not as small as it was in our experiment.

5.5. Location errors due to propagation velocity variation

From the point of view of location techniques (for example to assess the cable state in order to repair the degraded area), it is critical to know the precise value of the group delay β_1 for each frequency component used to estimate the overall delay, and thus, to compute the propagated distance.

The example shown in the diagram of Figure 11 depicts how varies β' , the first derivative of the phase term β versus frequency, in a spectral interval of 20 MHz. According to the proposed model, this variation is linear, and its slope is the dispersion constant ($\beta_2 = -0.76 \text{ ns}^2 \text{ m}^{-1}$ in this example). Note that this diagram shows the group delay (inverse of the group velocity) for each frequency component.

In the frequency upper limit shown in Figure 11, labeled as f_B , β'_B is lower since the dispersion constant is negative, whereas in the lower boundary (f_A) the group delay β'_A is greater. The equivalent propagation velocity for the three frequency components under study (labeled as A, B, and 0) are also shown in Figure 11. As a first approach, we can consider that the signals captured at the cable end (or cable ends) contain significant and similar spectral components in the whole frequency interval (this case is drawn in dark gray in Figure 11). Then, the propagation velocity will be $170 \text{ m}/\mu\text{s}$ ($1/\beta'_0$), that yields to an estimated distance $L_0 = 1020 \text{ m}$ (for example for a given measured propagation delay of 6 ns). Let us consider now that only a small part of the frequency components are available

for location (in the extreme of the bandwidth, drawn in black and light gray in Figure 11). Such situation can arise either, because the rest of the components become extinct due to attenuation or destructive interference, or simply because an important amount of synchronous impulsive noise degrade these components. In these cases, the propagation velocity used to determine the estimated distance would be different ($v_{p,A}$ or $v_{p,B}$), and the corresponding estimated distances (L_A and L_B) would be, for the same measured time delay, rather different to L_0 .

The scheme proposed in Figure 7 allows us to select the most suitable frequency interval to be used for location purposes. And, for an accurate estimation of the fault location, the values of β_1 and β_2 provided by the model proposed in this paper are necessary.

6. Conclusions

This paper proposes a propagation model based on three parameters: one that models the signal attenuation, and two others that model its phase variation (the delay and the dispersion constants). When compared to other models, the proposed one exhibits similar peak and width values for both, originally symmetric and asymmetric pulses.

Two methods to estimate the model parameters are also proposed: starting from the classical frequency dependent attenuation constant described in the bibliography, or by using a vector network analyzer. Both methods provide similar results.

The main advantage of the proposed model is that the relationship between the propagation velocity and frequency, as well as the peak reduction and the PD spread due to dispersion, can be now quantified. We demonstrate that peak reduction due to dispersion cannot be underestimated, especially in urban distribution cables.

A method to estimate the dependence of the delay and dispersion constant with frequency is also proposed. In this method PD pulses are digitally processed in a narrow frequency interval. Using this technique we also obtained an estimation of the initial width of PD pulses in a XLPE cable.

The model and related techniques proposed in this paper give a more comprehensive view of PD propagation, contributing to a better understanding of this phenomenon and improving the accuracy of PD source location.

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