Growth regimes of porous gold thin films deposited by magnetron sputtering at oblique incidence: from compact to columnar microstructures

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\textit{Abstract}

Growth regimes of gold thin films deposited by magnetron sputtering at oblique angles and low temperatures are studied from both theoretical and experimental points of view. Thin films were deposited in a broad range of experimental conditions by varying the substrate tilt angle and background pressure, and were analyzed by Field Emission Scanning Electron Microscopy (FESEM) and Grazing Incidence Small-Angle X-ray Scattering (GISAXS) techniques. Results indicate that the morphological features of the films strongly depend on the experimental conditions, but can be categorized within
four generic microstructures, each of them defined by different bulk geometrical patterns and pore percolation depth and connectivity. With the help of a growth model, a microstructure phase diagram has been constructed where the main features of the films are depicted as a function of experimentally controllable quantities, finding a good agreement with the experimental results in all the studied cases.

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I.- Introduction

It is well known that gold has endothermic oxygen chemisorption energy, thus being inert towards oxidation reactions [1]. In this aspect, nanoporous gold has attracted much attention in the science and technology for its functionality as a catalyst for the carbon monoxide oxidation. In reference [2], for instance, it is found that the presence of a high density of geometric steps and kinks in nanoporous gold is essential to activate chemical reactions with the advantage of a high thermal stability against coarsening, thus presenting advantages on the catalytic activity of gold nanoparticles. Consequently, the synthesis of gold thin films with large surface area and with valleys that penetrate deep into the material seems relevant in order to enhance these properties. Although nanoporous gold has usually been synthesized by the chemical dealloying of Au$_{35}$Ag$_{65}$ (see for instance refs. [2-3]), the possibility to use plasma-assisted deposition techniques would be desirable, not only because it might allow a better control on the surface and pore percolation features, but also from environmental and industrial points of view. This paper is aimed at theoretically and experimentally studying the growth of nanoporous gold thin films by magnetron sputtering at low temperatures, and at analyzing the percolation depth and connectivity of the surface valleys that penetrate into the film for enhanced catalytic applications.

In reference [4] we theoretically and experimentally studied the growth of gold thin films deposited by magnetron sputtering at oblique angles and low temperatures by varying the background plasma pressure. There, we found an intrinsic connection between film microstructure and the degree of thermalization of sputtered particles by interaction with gas and plasma heavy particles, described by the quantity $\Xi$ and defined as
\[ \Xi = \frac{L}{\nu \lambda} \]  

where \( L \) is the target-film distance, \( \lambda \) the mean free path of sputtered particles, and \( \nu \) the number of elastic collisions required to thermalize a sputtered atom. In this way, when \( \Xi \ll 1 \), the sputtered particles do not experience many collisions and mainly keep their original directionality and energy just after their sputtering from the target. Under these conditions, films with a tilted columnar microstructure, very similar to those obtained by electron beam assisted evaporation at oblique angles [5-7] were grown. When \( \Xi \gg 1 \), on the other hand, the sputtered particles experience enough collisions to become thermalized and arrive at the film surface with an isotropic velocity distribution function. These working conditions yielded porous films with vertical column-like structures, similar to those obtained for TiO\(_2\) deposited at the back side of the substrate holder in reference [8].

The gold microstructures obtained in reference [4] contrast with typical microstructures found at normal angle depositions where films are usually compact and homogeneous [8]. Due to the variety of microstructures found by magnetron sputtering at low temperatures, in this paper we broaden the scope of previous works [4,8] and systematically analyzed the thin films deposited by magnetron sputtering at oblique angles for a wide range of values of the substrate tilt angle, \( \sigma \), and background pressure, \( p_g \). Our aim is therefore a complete experimental and theoretical classification of the possible growth modes of gold thin films and the study of the microstructure of the films, including the porous structure, percolation depth and connectivity for catalytic applications. As a result we have found that the whole set of experimental gold thin film microstructures can be described through only four generic
microstructures, based on which we have constructed a phase diagram where the morphological features of the films are connected with the values of $\sigma$ and $\Xi$. Particular attention has been paid to the development of geometrical patterns in the bulk of the films as well as to the size and percolation depth of surface valleys, an aspect that has deserved little attention in previous studies in the literature for plasma-assisted depositions of thin films [7, 9-11].

We believe that the research presented in this paper does not only possess relevance for the fundamental knowledge regarding the microstructure formation and growth of magnetron sputtered thin films at low temperatures and oblique angles but, as evidenced in previous work dealing with the fabrication of thin films with a localized surface plasmon resonance behavior [12-14], also for their potential use for the fabrication of metal films with special optical properties. We also believe the films we analyze are of the utmost interest for applications concerning the catalytic activity of nanoporous gold and, in particular, for carbon monoxide oxidation applications [2].

II.- Experimental Setup

Gold thin films were deposited by the magnetron sputtering technique using a 3.8 cm diameter gold target and argon as sputter gas. The base pressure of the chamber is in the mid $10^{-7}$ Pa range. A 2 cm$^2$ ultrasonically cleaned Si(100) substrate was placed at $L=0.19$ m from the target, and tilted with respect to its normal (see figure 1a). The tilt angles of the substrate were set to different values ranging from $\sigma=45^\circ$ to $\sigma=87.5^\circ$. The argon gas filled the whole deposition chamber and its pressure was set from 0.15 to 4 Pa, with the power and the deposition time being kept constant at 100 W and 1800 s respectively. The visible plasma glow was always many centimeters away from the
substrate holder (the glow volume was about 50-75 mm next to the target) and the film temperature during the sputtering process was always below 350 K.

Films were characterized by Field Emission Scanning Electron Microscopy (FESEM) as well as by grazing-incidence small-angle X-ray scattering (GISAXS). Since films microstructure was rapidly altered by the electron beam during measurement when using the former technique, we used short exposure times in order to obtain reliable images. The GISAXS technique was implemented at the synchrotron beamline BW4 of the DORIS III storage ring (DESY, Hamburg) using a wavelength of 0.138 nm and a sample-to-detector distance of 2.175 m [15]. A moderate microbeam focusing was achieved using beryllium refractive lenses (beam size 42 µm x 22 µm). The scattering signal was recorded with a 2D detector (MAR CCD camera with 79.1 µm lateral pixel size). For each sample two different patterns were recorded by placing the films oriented according to the $\Delta$ and $\Pi$ configurations, defined in figure 1b. In the $\Delta$ configuration the beam does not see any possible tilting of the microstructural features, while in the $\Pi$ configuration it impinges perpendicular to the plane containing the tilting angle of the microstructural features.

**III.-Growth Model**

The Monte Carlo growth model is similar to that employed in reference [4]. It considers the deposition of gold atoms on a two-dimensional substrate that defines the $x$-$y$ plane of coordinates, whereas the $z$ axis is defined by the direction perpendicular to it. The three dimensional space is divided into a $N_L \times N_L \times N_H$ grid, where each cell has the value 1 if it contains a deposited gold atom and 0 otherwise. Each cell, therefore,
represents a gold atom in the network. Cell width is estimated by the typical distance between atoms in the material (0.4 nm).

Each deposition particle is thrown towards the substrate from an initial random position above the film, following the direction defined by the spherical angles $\theta$ and $\phi$, where $\theta \in [0, \pi/2)$ is the polar angle of incidence ($\theta = 0$ is the direction normal to the substrate) and $\phi \in [0, 2\pi)$ is the azimuthal angle. The movement of the particle continues along a straight line, assuming periodic boundary conditions, until it hits the surface, where it sticks. The angles $\theta$ and $\phi$ are randomly calculated for each deposition particle by defining an incident angle distribution function per unit time and unit surface, $I(\Omega)$, with $d\Omega = \sin \theta d\theta d\phi$ being the differential solid angle. In order to estimate the magnitude $I(\Omega)$ we have employed the SIMTRA code that allows the determination in the deposition system geometry of the angular distribution function of the deposition particles that arrive at the substrate [16]. A Molière type potential was taken to describe the interaction between Au and Ar atoms. Once the function $I(\Omega)$ is calculated, the model is solved for values of $N_L$ and $N_H$ up to 2000.

Due to the separation between the plasma glow and the substrate holder in all the experimental conditions and the absence of electronegative gases in the reactor, we have not taken into account any plasma ion/surface interaction in the growth model [17,18]. Furthermore, due to the low temperature of the films during growth, no surface mobility has been considered, as the ratio $T_s / T_m \sim 0.2$, being $T_s$ and $T_m$ the film temperature during growth and the gold melting temperature, respectively, corresponds to the so-called Zone I in the SZM model, where the deposition is dominated by surface shadowing [19-20]. These approximations will be discussed below in section IV.
The simulated microstructures were characterized by taking into account the geometrical patterns appearing in the bulk of the films, and also as a function of the size and percolation depth of the pores in the material. According to the IUPAC [21], we distinguish micropores, with typical entrance sizes smaller than 2 nm, and mesopores, with entrance sizes larger than 2 nm. Moreover, we distinguish pores occluded in the material, as well as those connected with the surface.

IV.- Results and Discussion

Theoretical Results

In our analysis, rather than the experimentally controllable quantity, \( p_g \), we employ the non-dimensional parameter \( \Xi \), defined in eq. (1), with \( L=0.19 \text{ m} \) the distance between the cathode and the film, \( \nu=12 \), the number of collisions required to thermalize the gold atom in the argon environment [22], and \( \lambda = k_B T_g / p_g \sigma_{\text{Au-Ar}} \) the mean free path of the gold atom, with \( k_B \) the Boltzmann constant, \( T_g = 600 \text{ K} \) the spatially averaged value of the gas temperature, and \( \sigma_{\text{Au-Ar}} \) the cross-section for an elastic scattering of an Au atom on an Ar atom (\( \sigma_{\text{Au-Ar}}=3.25\times 10^{-19} \text{ m}^2 \)). Consequently, under our conditions, we estimate \( \Xi \sim 0.67 \times p_g \text{ Pa}^{-1} \).

Simulated film microstructures possess different features that depend on the values of \( \Xi \) and \( \sigma \). Figure 2 shows a series of snapshots corresponding to four different calculations obtained for extreme values of these two parameters. These simulations have been selected because they are representative of whole sets of calculated thin films with similar microstructural and pore features. These four generic microstructures
depicted in figures 2a-d will be designed here as $\alpha$, $\beta$, $\gamma$ and $\delta$, and are characterized by the following features:

- **$\alpha$-type microstructure**: the film is compact without any well defined geometrical pattern in the bulk of the material, and has a very small density of pores (see figure 2a).

- **$\beta$-type microstructure**: the film is rather compact, but surface valleys percolate from the very surface of the film to near the substrate through vertical tilted mesopores (see figure 2b). This structure could also be seen as a tilted highly coalescent columnar structure (i.e., columns are not isolated from each other but are always touching), whereas mesopores can be devised as the empty space between the coalescent columns.

- **$\gamma$-type microstructure**: The film possesses similarities with the $\beta$-type microstructure, but now surface valleys and mesopores are larger and the columns appear well separated and isolated from each other or form small groups or islands (see figure 2c).

- **$\delta$-like microstructure**: this film is characterized by vertical coalescent column-like structures, with a high density of micro and mesopores occluded in the material, and with cavern-like surface patterns elongated in the vertical direction that penetrate deep into the bulk (see figure 2d).

Simulations of the growth of these microstructures are found in the form of video files as supplementary material. In order to further understand the main features of the above mentioned four generic microstructures, we have studied the connectivity of mesopores in the materials, i.e., we have determined whether a particular void within the material is
occluded (completely surrounded by material), or there is a continuum path that connects the void with the film surface (air) through mesopores. In figure 3a we have depicted the local density of surface-connected mesopores at a given depth in each of the four characteristic microstructures, calculated as follows: i) once the three dimensional map for each film was obtained, we calculate the size and connectivity of the pores and only consider those large enough to be mesopores, ii) we do not take into account those mesopores that are occluded, i.e., those not connected with the film surface (air), and iii) for each slice of material at a given depth we calculate the volume of surface-connected mesopores in comparison with the total volume of the slice. At the film surface all of them show a high surface-connected volume, which corresponds to the surface roughness region, always present in the films. After this region, the surface-connected volume of the $\alpha$-type microstructure rapidly drops to zero, indicating that pores in the bulk of the film are always occluded. Conversely, the $\beta$-type microstructure shows a surface-connected mesopore volume of about 25% after the roughness region, which remains constant up to depths near the substrate. This is more prominent in the $\gamma$-type microstructure where it reaches about 65% in the bulk of the film, a value which is reasonable due to the existence of isolated columnar structures. Finally, the $\delta$-type microstructure shows the existence of surface-connected mesopores within the material, which now amount to about 10% in the bulk of the film, i.e. a much lower accessibility to bulk features from the surface. For illustration purposes, we present the local density of occluded mesopores as a function of depth for each abovementioned characteristic microstructure in figure 3b. In general, their density is quite low, being most of the pores surface-connected. This is evident for the $\alpha$ - and $\gamma$ - type microstructures, with a local density always below 1%, whereas the $\beta$- and $\delta$ - type microstructures present a density around 2% in the bulk that increases near the substrate to values below 10%.
Once the four generic microstructures generated by the model have been characterized, we have systematically run simulations in multiple conditions in order to calculate the different microstructures as a function of $\Xi$ and $\sigma$. Results are depicted in figure 4, where we present the obtained results in the form of calculated microstructure phase diagram. Thus, when $\Xi<1$ and for the highest values of $\sigma$ we find that the highly directional deposition particle flow develops surface mounds that serve as seeds for columnar structures. These columns grow tilted from about $45^\circ$ to about $60^\circ$ with respect to the normal, being the average percolation depth of surface valleys above 80% of the total film thickness, resembling $\gamma$-type microstructures. For lower values of $\sigma$, and maintaining $\Xi<1$, surface mounds also appear at the initial stages of growth. They serve as seeds, although the lower value of the substrate tilt angle causes columns to grow closer and to merge, leaving many voids within the material, some of them connected with the film surface. These voids are tilted with respect to the normal and have an average penetration depth of about 50-70%, resembling a typical $\beta$-type microstructure. For $\Xi<1$ and even lower values of $\sigma$, the growth is characterized by the lack of formation of large surface grains in the first stages of growth, resembling a typical $\alpha$-type compact microstructure, with a penetration depth of surface features lower than 20%. Interestingly, some occluded pores may grow with a tilt angle that depends on the actual values of $\Xi$ and $\sigma$, and that is why there are solid lines in this region of figure 4.

As $\Xi$ increases, the deposition particles arrive at the film surface with higher isotropy, until the resulting microstructure becomes independent of $\sigma$, which corresponds to the region of formation of the $\delta$-type microstructure. This region is characterized by the formation of surface grains that grow vertically and that coalesce since the very early stages of growth. In the extreme cases with $\Xi>>1$, a microstructure similar to that in figure 2d is obtained, with an average penetration depth of surface features around 20%.
We have to underline here that all the simulations performed for figure 4 were done on films with thickness up to 400 nm, and that no dependence between microstructure and film thickness has been found.

The microstructure phase diagram presented in figure 4 depicts the main morphological features of the microstructures of films prepared by magnetron sputtering as a function of Ξ and σ, at low temperatures. Next, we present a thorough experimental study of multiple gold thin films deposited as described in section II that will be employed to assess its accuracy.

Comparison with experimental data

We split the analysis of the films in three sets according to the value of Ξ during the deposition. First set corresponds to films deposited under the conditions $p_g=0.15 \, Pa$, $(\Xi \sim 0.1)$, and $\sigma = 45^\circ, 60^\circ, 70^\circ, 80^\circ, 85^\circ$ and $87.5^\circ$. According to figure 4, the simulations indicate that by increasing the value of $\sigma$ a transition from an $\alpha$-type to a $\beta$-type microstructure is obtained when $\sigma \sim 60^\circ$. Similarly, a transition from a $\beta$-type to a $\gamma$-type microstructure occurs when $\sigma \sim 80^\circ$. In figure 5a-f we show the cross-sectional FESEM images of these films along the $\Pi$ direction (see scheme in figure 1b). Figure 5a corresponds to a situation with $\sigma = 45^\circ$, where we find a compact film with no apparent geometrical patterns in the bulk. For the case with $\sigma = 60^\circ$, figure 5b shows a structure similar to that in figure 5a, although now some tilted grooves appear in the microstructure, which become more evident in figure 5c, where $\sigma = 70^\circ$. In this latter case, although the structure seems compact, a coalescent column-like microstructural arrangement is depicted ranging from the very surface of the film to near the substrate. In agreement with figure 4, these experimental results confirm a transition between the $\alpha$-type and $\beta$-type microstructures for $\sigma \sim 60^\circ$. 

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In figure 5d we depict the FESEM image of the film deposited at $\sigma = 80^\circ$. In contrast with the case where $\sigma = 70^\circ$ (see figure 5c), we find a clearly tilted columnar microstructure with columns that become progressively isolated and better defined in the films deposited at $\sigma = 85^\circ$ and $\sigma = 87.5^\circ$ (figures 5e and 5f, respectively). This tendency is more evident in figures 6a-d where we show the FESEM images of the films viewed from the $\Delta$ direction for $\Xi \sim 0.1$ and $\sigma = 70^\circ$, $80^\circ$, $85^\circ$, $87.5^\circ$, respectively. The film microstructure depicted in figure 6a, ($\sigma = 70^\circ$) indicates the existence of well-packed coalescent columns, that become gradually isolated when $\sigma$ increases (figures 6b-d). Therefore, in agreement with the simulations, we have found a transition from the $\beta$-type to the $\gamma$-type microstructure for $\sigma \sim 80^\circ$. This transition is also evidenced by performing GISAXS measurements on the films: in reference [23] we have previously shown that this technique provides information on the microstructural features of tilted columnar thin films and, in some cases, on the existence of critical correlation lengths for oxide thin films prepared by e-beam evaporation. In these previous investigations we showed that an asymmetrical shape of the scattering profile was an indication of a tilted, and therefore asymmetric, arrangement of the film nanocolumns, and that the average value of these correlation distances could be deduced from the distance between the scattering maximum in the largest pattern wing and the center. In the present work, we have essayed a similar analysis for films grown under the conditions $\sigma = 60^\circ$, $70^\circ$, $80^\circ$, $85^\circ$ and $87.5^\circ$ and $p_e = 0.15$ $Pa$, ($\Xi \sim 0.1$). The corresponding patterns, gathered in figure 7a-j have been recorded with the sample oriented in the $\Delta$ and $\Pi$ configurations as explained in the experimental section. In the $\Delta$ configuration none of the films present an asymmetric GISAXS pattern, and no displacement of the maximum can be observed. By contrast, in the $\Pi$ configuration, some of the patterns are clearly asymmetric and depict well defined off-center maxima
in the largest wing. A more careful evaluation of the patterns can be done by plotting their intensity along a horizontal straight line plotted at the position of the Yoneda peak [24]. In the corresponding plots, reported in figure 8, it can be clearly appreciated that all the patterns are asymmetric and that the films prepared at $\sigma > 70^\circ$ depict a clearly defined maximum that appears more separated from the Yoneda peak as the deposition angle increases. Calculations based on the methodology presented in refs [23, 25] permit the calculation of correlation distances of 85, 61 and 64 nm for the films prepared at 80º, 85º and 87.5º, respectively. It must be stressed that the thin films prepared at 70º and 60º do not present any well defined maximum apart from the Yoneda peak. This suggests that only for deposition angles greater than 70º the tilted film microstructure presents well-formed individual elements where a clear correlation distance can be determined. We have to stress here that, in general, this distance corresponds to the size of patterns with certain periodicity within the material, and it may refer to either isolated columns or a group of them. Regarding figure 5, the calculated correlation distance is similar to the distance between two consecutive columns in the material. This result corroborates the tendency to form non-coalescent isolated columns in the material for increasing values of $\sigma$, in agreement with the simulations.

In figures 5g-l we have included the microstructure of the simulated thin films calculated for the same conditions as the experimental cases displayed on the left side (figure 5a-f). The systematic comparison between experimental and simulated microstructures confirms, in general, a good agreement, although there are however slight differences between figures 5a and 5i. In this case, the model predicts the scattered formation of some tilted occluded pores which do not appear experimentally.
This discrepancy points towards the existence of a limited mobility of gold atoms on the film surface making these small occluded voids disappear. Indeed, temperature activated processes or the impingement of plasma ions onto the surface can be responsible for such effect: our model represents a simple approximation to the actual deposition process, presenting the advantage that no calculated or fitting parameters others than the incident angle distribution function of the deposition particles must be known to run the simulations. In the literature there are numerical codes that consider more complex processes [26,27], such as thermally activated mechanisms or ion induced damage of the films during growth, which require the previous knowledge of activation energies or thresholds for the diverse processes. Although the precise values of these parameters do not appear in the literature in most of the cases, we have solved the NASCAM code in multiple conditions estimating the energy thresholds for these processes through reference [28] as a test for our model. Results of these simulations corroborate the assumptions of our model and indicate that, in our experimental conditions, surface shadowing determines the main features of the film microstructure, being the rest of processes responsible for the removal of some occluded voids inside the material. The good agreement between our model and the experimental data is confirmed in Figure 9 where we compare the experimental and theoretical values of the tilt angle of the features of the films, finding always a good match between them. Furthermore, the simulations reproduce not only the microstructure evolution but also the decrease on the film thickness when increasing \( \sigma \) for equal deposition time (i.e., same number of sputtered particles in all the cases, a fact that was considered in the simulations).
The second set of studied deposition conditions corresponds to higher values of the deposition pressure. In figures 10a-e we present the cross-sectional FESEM images of films grown at a pressure of $p_g=1\ Pa$ ($\Xi \sim 0.67$) and $\sigma=45^\circ$, 60$^\circ$, 70$^\circ$, 80$^\circ$ and 85$^\circ$. For $\Xi \sim 0.67$, figure 4 shows that for increasing values of $\alpha$ there is a transition between an $\alpha$-type to a $\beta$-type microstructure when $\sigma \sim 50^\circ$. In figure 10a we show the FESEM image for $\sigma = 45^\circ$, where a compact film is depicted. For $\sigma = 60^\circ$ (figure 10b) we find again a compact film, although the bulk possesses now some tilted features that become more isolated for $\sigma = 70^\circ$, 80$^\circ$ and 85$^\circ$ (figures 10c, 10d and 10e, respectively). The results of the model for the same deposition conditions are shown in figures 10f-j. They agree well with the experimental images, except for the compact case (figures 10a and 10f), where the model still predicts the existence of a few occluded tilted pores that are not visible experimentally. As in the lower pressure case, we believe that this discrepancy is due to the presence of a limited surface mobility, not included in the model. Except for this discrepancy, the comparison between experimental and simulated values of the tilt angle of the structural features as a function of $\sigma$ is fairly good (see figure 9).

To check the existence of the $\delta$-type microstructure, we have deposited films at higher pressures, $p_g=2.5$ and $4\ Pa$, for a substrate tilt angle of $\sigma=85^\circ$. These conditions result in $\Xi \sim 1.7$ and $\Xi \sim 2.7$, respectively, thus indicating that the deposition flow is highly thermalized by the background gas when arriving at the substrate. The FESEM image of the film for $\Xi \sim 1.7$ appears in figure 11a, where vertical coalescent structures are apparent. This microstructure becomes more evident in figure 11b, where we have depicted the FESEM image for the film deposited for $\Xi \sim 2.7$. The results of the simulations under these conditions, shown in figures 11c-d, clearly reproduce the
measured microstructure, thus confirming that the experimental cases presented in figure 11a-b fit within the predictions of the microstructure phase diagram presented in figure 4. Finally, the comparison between experimental and simulated tilt angle of the patterns appear in figure 9, finding a good agreement. Although the values $\Xi \sim 1.7$ and $\Xi \sim 2.7$ ensure the growth of a $\delta$-type microstructure, the completely vertical columnar microstructure must be understood as a limit case when $\Xi >> 1$.

As a final remark we would like to stress that we have studied the different microstructures as a function of $\sigma$ and $\Xi$, when depositions were carried out using an electromagnetic input power of 100 W. In this paper we have not explored the influence of the input power on the film microstructure: this quantity strongly determines the cathode electric potential, and indirectly the sputtering and deposition rates. This means that the influence of mechanisms linked to surface mobility processes controlled by the deposition rate, such as the amount of thermally activated atomic jumps on the surface or ions impinging on the surface per deposited particle, would change. In this way, we expect that the higher the deposition rate (i.e., the higher the input power), the lower the influence of surface mobility processes and the less compact the films grow [29]. Nevertheless, as long as that deposition takes place in Zone I of the SZM these processes should play a minor role, a fact corroborated by the good agreement between simulations and experimental data.
V.- Conclusions

In this paper we have studied the different growth regimes of gold thin films deposited by magnetron sputtering by varying the deposition angle and the background pressure as running parameters. For this purpose we have developed a theoretical model that takes into account: i) the elastic scattering of deposition particles on plasma heavy particles in their way from the cathode to the film, and ii) the surface shadowing mechanism. The model predicts that all the films features can be categorized within four generic microstructures, which we have labeled as α-, β-, γ- and δ-type. Each of them possesses different bulk geometrical patterns, pore connectivity and percolation depth. A microstructure phase diagram has been calculated that gives information on the film morphological features as a function of the experimentally controllable parameters. To check the validity of the simulations we have deposited gold thin films under carefully chosen conditions, finding that the microstructures of the synthesized films corroborate the results of the simulations and agree with the microstructure phase diagram. Finally, we would like to stress that we have focused our research on gold thin films, but the aim of this paper is general, and we expect that the results presented in this paper can be generalized to other magnetron sputtered materials.

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**Figure Caption**

Figure 1.- a) Experimental Setup, b) definition of the \( \Delta \) and \( \Pi \) directions on the films.

Figure 2.- Typical microstructures found in the simulations. a) \( \alpha \)-type (simulation conditions \( \Xi = 0.1 \) and \( \sigma = 45^\circ \)), b) \( \beta \)-type (simulation conditions \( \Xi = 0.1 \) and \( \sigma = 70^\circ \)), c) \( \gamma \)-type (simulation conditions \( \Xi = 0.1 \) and \( \alpha = 89^\circ \)), d) \( \delta \)-type (simulation conditions \( \Xi = 10 \) and \( \sigma = 0^\circ \)).

Figure 3.- (Color online) Local density of mesopores at a given depth for the generic microstructures in figure 2, as a function of depth. a) Surface-connected mesopores, b) occluded mesopores.

Figure 4.- Microstructuring regime phase map predicted by the growth model as a function of \( \Xi \) and \( \sigma \). The colors indicate the average penetration depth of the surface valleys into the film through mesopores (in %), whereas lines denote the tilt angle of the structures (columns or mesopores) in the bulk of the film (in degrees). Labels '\( \alpha \)-type ', '\( \beta \)-type', '\( \gamma \)-type and '\( \delta \)-type ' correspond to the regions where the generic microstructures depicted in figure 2 are found.

Figure 5.- FESEM cross-section images, along the \( \Pi \) direction, of films deposited in the conditions \( p_g = 0.15 \text{ Pa} \ (\Xi = 0.1) \) and: a) \( \sigma = 45^\circ \), b) \( \sigma = 60^\circ \), c) \( \sigma = 70^\circ \), d) \( \sigma = 80^\circ \), e) \( \sigma = 85^\circ \), f) \( \sigma = 87.5^\circ \), g-l) result of the simulations in the same conditions as in figures 5a-f, respectively.

Figure 6.- FESEM cross-section images, along the \( \Delta \) direction, of films deposited in the conditions, \( p_g = 0.15 \text{ Pa} \ (\Xi = 0.1) \) and: a) \( \sigma = 70^\circ \), b) \( \sigma = 80^\circ \), c) \( \sigma = 85^\circ \), and d) \( \sigma = 87.5^\circ \).
Figure 7.- (Color online) GISAXS spectra of the films for Δ and Π incidence.

Figure 8.- (Color online) Intensity of the spectra presented in figure 8a-e along a horizontal straight line plotted at the position of the Yoneda peak as a function of the wavenumber, defined as $2\pi / D$, with $D$ being the wavelength. Maximum values are also shown for films with $\sigma \geq 80^\circ$.

Figure 9.- (Color online) Experimental value of the tilt angle of the studied microstructures as a function of $\sigma$, together with the simulated values.

Figure 10.- FESEM cross-section images, along the Π direction, of films deposited in the conditions $p_g = 1 Pa \ (\Xi = 0.67)$ and: a) $\sigma = 45^\circ$, b) $\sigma = 60^\circ$, c) $\sigma = 70^\circ$, d) $\sigma = 80^\circ$ and e) $\sigma = 85^\circ$, f-j): results of the theoretical model in the same conditions as in 10a-e, respectively.

Figure 11.- FESEM cross-section images, along the Π direction, of films deposited in the conditions a) $p_g = 2.5 \ Pa \ (\Xi \sim 1.7)$ and $\sigma = 85^\circ$, b) $p_g = 4 \ Pa \ (\Xi \sim 2.7)$ and $\sigma = 85^\circ$, c-d) results of the model in the same conditions as 11a-b, respectively.
References


Figures

Fig. 1
Fig. 3

Surface-connected mesopores

Occluded mesopores

Mesopore density at a given depth (%)

α-type
β-type
γ-type
δ-type

Surface  20  40  60  80  100
Depth (%)
Fig. 4
Fig. 6
Fig. 7
Fig. 8

![Graph showing intensity vs. wavenumber for different $\sigma$ values and $D_y$ values.](image-url)
Fig. 9

![Graph showing microstructure tilt angle versus deposition angle with different symbols representing different $\varepsilon$ values.](image-url)