A Low-Voltage Floating-Gate MOS Biquad

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A second-order \(g_m\)-C filter based on the Floating-Gate MOS (FGMOS) technique is presented. It uses a new fully differential transconductor and works at 2 \(V\) of voltage supply with a full differential input linear range and a THD below 1%. Programming and tuning are performed by means of a single voltage signal. The transconductor incorporates a novel Common-Mode Feedback Circuit (CMFB) based also on FGMOS transistors.

Keywords: Analog low-voltage low-power filters; FGMOS circuits

I. INTRODUCTION

Low Power (LP) and Low Voltage (LV) circuits are nowadays extensively demanded by the market of portable applications (computers, phones, biomedical implants) [1]. This is leading the circuit design philosophy to environments where the scaling down of the power supply is continuously decreasing, but where the circuit performance must be also retained. Filters are building blocks appearing on demanded LP/LV products. Continuous Time Filters (CTF) could be a good choice versus the sampled-data filters alternatives, because they avoid the pre and post-aliasing filters. Also, they reduce the components spread (capacitors, current gains, etc.) if large time constants, as in audio-frequency applications are required. One of the main drawbacks of CTF is that tuning processes are necessary due to technological process variations, but on the contrary clock-noise is absent.

Continuous Time Filters performance is directly related to the continuous time integrator quality measured in terms of power consumption, linearity, noise, phase response and tunability as main parameters. In the context of LV/LP circuits, some contributions have been reported. Looking at the technology capabilities, a first approximation could classify them in bipolar, BiCMOS or CMOS designs. Totally bipolar realizations can work at

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until V of supply voltage [3]. The best performance in terms of power efficiency and dynamic range for LP/LV CTFs has been proved for these technological realizations in [4, 5]. This optimal performance is obtained with a non-linear integration method preserving linear input-output relationship (companding technique [6]). They seem to be a good candidate for low-voltage high-frequency operation [7], although good results have been also obtained in the audio frequency range [8]. CMOS realizations are based on biasing transistors at strong inversion, on saturation [9–11] or linear [12, 13] region, and also in weak inversion mode [14–16]. Companding realizations can be found in CMOS technologies, being possible to be ruled either by squared-root [11] or by logarithmic [15, 16] laws, unlike bipolar designs. This fact makes possible to distinguish between so called log-filters and \( \sqrt{x} \)-filters. The BiCMOS technologies make compatible the reduced voltage swing for bipolar transistors with MOST working at linear region. In Refs. [17, 18] circuit techniques are used to limit the drain-to-source voltage on MOST.

In this paper, a biquad based on a new transconductor realization is presented. The circuit is based on the FGMOS transistor principle [19–20]. The use of this technique makes easy the voltage-down process without degrading the circuit performance parameters. The specifications are focused on the audio frequency range. Large time-constants for low frequencies (some tens of Hz) need low \( g_m/C \) ratios, which forces to low transconductance values and large integrating capacitors as well as high output resistance. The transconductor has good programming and tuning characteristics. Fully balanced input-output operation has been used in order to reduce distortion, so the proposed transconductor includes a new common-mode feedback circuit (CMFB). The common-mode feedback circuit presented also exploits the processing capabilities of the FGMOS technique. The simulation results obtained are compared to other audio-frequency filter realizations.

II. FGMOS BASIC PRINCIPLE

In the FGMOS technique exposed in [19], the drain-to-source current characteristic of a MOS transistor is externally modified by adding a set of capacitors connected to the gate terminal as shown in Figure 1(a). Here, the FGMOS transistor has \( V_i \) \((i = 1, 2, \ldots, n) \) input voltages. \( C_i \) are the input capacitors, \( C_{ox} \) the floating-gate oxide capacitance, and \( C_{FD}, C_{FS} \) and \( C_{FB} \) the overlap capacitances between the floating-gate to the drain, source and bulk respectively. The equivalent circuit and schematic are shown in Figures 1(b) and (c), respectively. The drain-to-source current in saturation if \( C_{FD}, C_{FS} \ll C_T \) is given by,

\[
I_D = \beta_n \left( \sum_{i=1}^{n} w_i V_i + w_b V_b - w_s V_s - w_T V_{th} \right)^2 \tag{1}
\]

where \( \beta_n \) is the transconductance parameter, \( V_{th} \) is the nominal transistor threshold voltage, \( V_b \) and \( V_s \) the body and source voltages respectively. The weights in Eq. (1) are defined as: \( w_i = C_i/C_T \), \( w_b = C_{FB}/C_T \), \( w_s = [1 - (C_{FB}/C_T) - 2/(3(C_{ox}/C_T))] \), \( w_T = [1 - 2/(3(C_{ox}/C_T))] \), being \( C_T \) the total capacitance seen from the floating gate.

Let us consider the three-input FGMOS case, where \( V_1 \) is the input signal (\( V_{in} = V_1 \)), and \( V_2 \) and \( V_3 \) are bias voltages (\( V_{b2} = V_2 \) and \( V_{b3} = V_3 \)). For \( V_s = V_b = 0 \), the following expression results from Eq. (1),

\[
I_D = \beta_n (w_1 V_1 + w_2 V_2 + w_3 V_3 - V_{th})^2 \tag{2}
\]

in which, the drain-current is given as a quadratic dependence of input voltages’ weighted sum.
When $C_1 \gg C_{ox}$, Eq. (2) can be rewritten as,

$$I_D = \beta_n \cdot \frac{C_1^2}{C_T^2} (V_{in} - V_{th}')^2$$

(3)

where,

$$V_{th}' = V_{th} + \frac{C_2}{C_1} \cdot (V_{th} - V_{b2}) + \frac{C_3}{C_1} \cdot (V_{th} - V_{b3})$$

(4)

This expression enables the reduction of the threshold voltage seen from the input terminal ($V_1$). In order to obtain this, it must be fulfilled that $V_{b2} > V_{th}$ and/or $V_{b3} > V_{th}$. The magnitude of the reduction is controlled by the input capacitor ratios $C_i/C_1$ ($i = 2, 3$). As consequence, the requirements for voltage-down are less restrictive. If $C_1 = C_2 = C_3$ and $V_2 = V_3 = 1.5 V_{th}$, a $V_{th}' = 0$ is obtained.

Equation (2) can be also interpreted as follows: the FGMOS transistor has two inputs, $V_{in+} = V_1$ and $V_{in-} = V_2$, and a bias signal, $V_{b3} = V_3$. The inputs are symmetrical with respect to the common mode level ($V_{cm} = V_{ad}/2$), and its weights are equal, $C_1 = C_2$. The result for this selection is,

$$I_D = \beta_n \cdot \frac{C_1^2}{C_T^2} (V_{cm} - V_{th}')^2$$

(5)

where the threshold voltage,

$$V_{th}' = V_{th} + \frac{C_3}{C_1} \cdot (V_{th} - V_{b3})$$

(6)

smaller than $V_{th}$ can be obtained if $V_{b3} > V_{th}$. The operation expressed in (5) represents the calculus of the mean value of the two input signals through the gate-to-source voltage of a MOST. This gate-to-source voltage is equal to the voltage common-mode value, with a threshold voltage controlled by $V_{b3}$. This sensing method for the $V_{cm}$ voltage can be used for common-mode correction via feedback or feedforward circuits. In the following section, these two basics interpretations of the floating-gate MOS transistor operation are applied to build the transconductor used in the biquad filter we propose to show the feasibility of FGMOS-based implementations.

### III. FILTER IMPLEMENTATION

The proposed $g_m$-C integrator is shown in Figure 2 [21]. The transconductor is a pseudo-differential pair composed of $M1-M4$, with $M9-M10$ as active load and a CMFB circuit which will be described later on. The $M1-M4$ three-input FGMOS transistors work as a two cross-coupled pair, giving a current defined by $(I_B - I_2)$ or $(I_1 - I_B)$, being $I_1 + I_2 = 2I_B$, and $I_B$ the bias current. The aspect ratios and input capacitors for these transistors are the same, being different the bias voltages, $V_{b1}$ and $V_{b2}$. When transistors are in saturation region, the output current is calculated as,

$$I_L = \frac{2\beta_n C_{in} C_c (V_{b2} - V_{b1})}{C_T^2} \cdot (V_{in1} - V_{in2})$$

(7)

where $\beta_n$ is the transconductor parameter $\mu_n C_{ox} W/L$, $C_{in}$ is the input capacitance connected to $V_{in1,2}$, and $C_c$ the control capacitor connected to $V_{b1}$ and $V_{b2}$ respectively. $C_T$ is the total capacitance seen from a floating gate. The large signal transconductance,

$$G_m = \frac{2\beta_n C_{in} C_c (V_{b2} - V_{b1})}{C_T^2}$$

(8)

can be easily tuned through the $(V_{b2} - V_{b1})$ factor. Values of negative resistances can be also obtained.

![FIGURE 2 Fully-differential FGMOS integrator.](image-url)
if necessary. Capacitor and voltage biasing value are selected in agreement with Eq. (4) in order to reduce the input voltage levels and maintaining MOST on saturation and strong inversion.

The schematic of the CMFB circuit used is represented in Figure 3. It is composed of a differential pair \((M12, M13)\) with diode-connected transistors as loads \((M14, M15)\). The FG-MOS pair has the same total input capacitance \((C_{T,12} = C_{T,13})\), and all the capacitors have the same value. The constant reference voltage \((V_{DD}/2)\) is obtained from the mean value of \(V_{DD}\) and ground. According with Eq. (5), the current through \(M13\) is,

\[
I_{D13} = \beta_n \left( \frac{V_{dd}}{2} - V_{th} \right)^2
\]

(9)

where the new threshold voltage, for equal input capacitors at \(V_{DD}\) and \(gnd\) inputs is,

\[
V_{th}^{'} = V_{th} + V_s
\]

(10)

which is compared with the equivalent gate voltage at \(M12\). The \(V_s\) is the common source voltage of the differential pair. The drain current in this case is,

\[
I_{D12} = \beta_n (V_{cm} - V_{th})^2
\]

(11)

where the new threshold voltage is the same as \(M13\) given in Eq. (10). The differential pair will be unbalanced when the common-mode level is not zero (for symmetrical power supplies), sensing the common-mode voltage level. The output of this circuit is connected to the transconductor bias current and a capacitor input of the cross-coupled input pair to obtain a negative feedback. The common-mode voltage level can be easily defined by the capacitor ratios at the CMFB circuit.

The transconductor has been used as basic block for a second order Tow-Thomas filter. The schematic of this block is shown in Figure 4. The equations describing filter operation are:

\[
\frac{V_{BP}(s)}{V_{in}(s)} = -\frac{s \cdot (g_{m1}/C_1)}{s^2 + s \cdot (g_{m2}/C_1) + (g_{m3}g_{m4}/C_1C_2)}
\]

(12)

\[
\frac{V_{LP}(s)}{V_{in}(s)} = \frac{(g_{m1}g_{m3})/(C_1C_2)}{s^2 + s \cdot (g_{m2}/C_1) + (g_{m3}g_{m4}/C_1C_2)}
\]

(13)

where the typical filter parameters of a second order section are,

\[
\omega_o = \sqrt{\frac{g_{m3}g_{m4}}{C_1C_2}}
\]

(14)

\[
Q = \frac{\sqrt{g_{m3}g_{m4} \cdot C_1/C_2}}{g_{m2}}
\]

(15)

being \(\omega_o\) and \(Q\) the cut-off frequency and the quality factor, respectively. Using Eqs. (14)–(15), the \(\omega_o\) and \(Q\) tuning can be performed through control voltages \(V_{b1}\) and \(V_{b2}\) as shows Eq. (8).
IV. RESULTS

The design of a filter illustrating the circuits described before has been focused for low-voltage audio applications. The time constant required are in the range of [10 ms, 25 µs] for frequencies between 100 Hz to 40 KHz respectively. These time constants can be implemented by choosing the adequate transconductance to capacitance ratio \( \frac{g_m}{2\pi C_1} \) in Eqs. (12)-(13). The lowest time constant imposes large capacitor values, so a trade-off between capacitor area and \( G_m \) value is necessary. For \( C_i = 5 \text{ pF} \) and a frequency range between 100 Hz and 10 KHz \( g_m \) is located between 0.3 µS and 3 nS. Cascode transistor structures were used at the outputs to increase the output resistance. The \( M1-M4 \) transistors are \( W/L = 2.5 \mu\text{m}/10 \mu\text{m} \), with capacitance values of 150 fF, 250 fF and 600 fF for the inputs. The \( M12 \) and \( M13 \) aspect ratio is 2.5 µm/17 µm, with input capacitances of 133 fF, and the total capacitance is 0.533 fF.

Electrical simulations have been performed in a 0.8 µm CMOS technology, with nominal threshold voltages of \( V_{th} = 0.85 \text{ V} \) and \( V_{tp} = -0.75 \text{ V} \). BSIM3v2 models have been used for MOST. Figure 5 shows simulation results for the output current \( (I_L) \) versus the differential input voltage for several values of the control voltage \( (V_{b2} - V_{b1}) \). In both, the high linearity of the transconductor and

![Figure 5](image_url)

**FIGURE 5** \( G_m \)-tuning: (a) for \( (V_{b2} - V_{b1}) \sim 0.2, 0.3 \) and 0.4 V and (b) for \( (V_{b2} - V_{b1}) \sim 4, 14 \) and 24 mV.

![Figure 6](image_url)

**FIGURE 6** THD versus peak-to-peak input range: (a) for \( G_m = 3 \text{ nS} \) and (b) for \( G_m = 300 \text{ nS} \).
the extremely wide input voltage range can be observed. The results obtained with this graphic agree with Eq. (8). The low distortion has been confirmed by transient analysis. The THD obtained for $g_{m1} = 3 \text{nS}$ and $g_{m2} = 300 \text{nS}$ are shown in Figures 6(a) and (b) respectively. Both have been calculated at the edges of the input Common-Mode Range ($V_{cm,\text{min}} \sim 0 \text{ V}, \ V_{cm,\text{max}} \sim 0.8 \text{ V}$). The total THD is always below 1%.

Finally, in Figure 7, the bandpass and lowpass filter transfer function have been obtained for two values of the cut-off frequency and the quality

![Graph](image)

**FIGURE 7** (a) $Q$-tuning and (b) $\omega_c$-tuning for both band-pass and low-pass filter transfer-functions.
factor. Table I summarize the performance of the transconductor for the maximum and the minimum transconductance values.

### V. CONCLUSIONS

A LV/HP filter implementation based on a new \textit{FGMOS} transistor has been presented. The transconductor uses \textit{FGMOS} to decrease the supply requirements as well as to tune the filter cut-off frequency, obtaining a full range differential input voltage and two decades for frequency tuning. Harmonic distortion is always below one per cent for all input values. The voltage common-mode correction is performed also by calculating its possible swing by means an \textit{FGMOS} differential pair. The feasibility of the block has been illustrated with a second order Tow-Thomas biquad. The obtained results agree with expectations, and propose a close solution for low voltage, low frequency applications with the \textit{FGMOS} technique.

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### References


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Esther Rodríguez-Villegas received the B.S. degree in Electronics from the University of Sevilla, Spain in 1996. Since 1997 she is in the Institute of Microelectronics at Seville (IMSE) where is currently working toward the Ph.D. degree. Her main research interests are the design of Floating-Gate circuits for both digital and analog applications.

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