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A diabatic parameterization of the twofold ground state potential energy surface of the H$_2$O-OH molecular complex

E. Galbis, E. Giglio, and B. Gervais

CIMAP, unité mixte CEA-CNRS-ENSICAEN-UCBN 6252 BP 5133, F-14070 Caen, Cedex 05, France
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We present a matrix functional form to fit the nearly degenerated potential energy surface of the H$_2$O-OH molecular complex. The functional form is based on second order perturbation theory, which allows us to define two diabatic states coupled together in the field of the surrounding water molecules. The fit reproduces faithfully the fine details of the potential energy surface (PES) like the crossings and the shallow barrier between the main and secondary minima. The explicit dependence of the model on polarization ensures its transferability to systems made of several water molecules. The potential is used to investigate the structural properties of the OH radical in solution by Monte Carlo simulation. The twin surface fit shows that the second PES is shifted above the ground state by typically 1600 cm$^{-1}$ for the configurations explored at a temperature of 300 K and a density of 1.0 g/cm$^3$. The second PES has thus little influence on the structuring of water around the OH radical at such a temperature and density. Our study confirms that under these thermodynamic conditions, OH is a weak hydrogen acceptor. © 2013 AIP Publishing LLC [http://dx.doi.org/10.1063/1.4826319]

I. INTRODUCTION

The OH radical is one of the most abundant chemical species produced in water radiolysis, with hydronium and solvated electron. It is a highly reactive species, leading to oxidation reactions as a basic mechanism observed in atmospheric reaction, in radiobiology and radiotherapy, or in corrosion, for example.

To investigate the underlying mechanisms, molecular dynamics is a powerful tool, which provides detailed structural and dynamical information. The necessary input for such an investigation is of course an accurate model of the potential energy surface (PES) of the system. The Carr-Parinello Molecular Dynamics (CPMD) approach uses a global PES obtained by intensive density functional theory (DFT) calculations. It has been used recently to investigate the diffusion mechanism of OH through liquid water. Such an approach is however computationally cumbersome and thus limited regarding the sample size, propagation time, and number of trajectories. It has been shown that self-interaction correction (SIC) to DFT is mandatory to produce meaningful results, making the computation even more demanding.

To overcome these limitations, a parameterized model PES could be used. Such an approach has been widely used to investigate material properties, and in particular those of water, by means of conventional MD or by Monte Carlo (MC) sampling of the phase space. Such a method was used to investigate the solvation of OH in bulk and at the surface of water samples, but it was based on a rudimentary PES model.

The H$_2$O-OH interaction is dominated by electrostatics in the long range domain and by hydrogen bond formation around equilibrium distances. Previous works have been performed to identify the equilibrium geometries and harmonic frequencies of the complex for the main and the secondary minimum. Several recent calculations performed with different computational methods confirm the energy and geometry of these minima associated with hydrogen bond formation as donor or acceptor. Experiments were also performed to analyze finely the shape of the coupled PES around the main minimum. The transition state associated with hydrogen atom transfer from H$_2$O to OH was also identified. All these studies show that the transition gap is located relatively far above the two minima. The rest of the surface, i.e., most of the five-dimensional space associated with the geometry of the complex for rigid H$_2$O and OH remains largely unexplored. A previous attempt to obtain an analytical representation of the PES is based on an adiabatic representation of the PES and it was fitted on a limited set of data. The coupling between the two PES is simply ignored in such an approach. However, for an accurate representation of the PES, these couplings have to be taken into account, as we shall see. The existing fit is definitely accurate near the minima and can be used to investigate the stationary points of the PES, but this might not be sufficient to investigate the dynamics of the system, when its internal energy increases, as it is the case for condensed phase at high temperature or pressure and also in gas phase.

To represent accurately the PES of the H$_2$O-OH complex, the specificity of the OH radical should be taken into account. Besides the Kramers degeneracy, the X$_2$Π ground state of OH radical is doubly degenerate. The two states differ by the occupation of the π orbitals, and thus by the orientation of the quadrupole. This feature does not exist in a restricted mean field approach and a minimal approach based on two electronic configurations is necessary to restore this difference.

The aim of this work is to develop a matrix formulation of the potential energy, which is able to take into account accurately the complexity of the coupled ground states PES of
the H$_2$O-OH complex. Such kind of analytic PES has a broad range of applications. Besides standard molecular dynamics studies of systems made of hydroxyl embedded in water, it offers the possibility to investigate specifically the role of the PES coupling by spin-orbit or non-adiabatic interactions, and it allows to study the interaction of hydroxyl with other radicals in aqueous solution. In connection with H$_2$O$_2$ PES, it will afford the investigation of relaxation dynamics of water clusters following ionization.

We use the developed potential to investigate the structure of liquid water solution embedding an OH radical by means of MC sampling of the configuration space. The radial distribution function around the hydroxyl is probably difficult to obtain experimentally because of the high reaction rate between two hydroxyl radicals. To our best knowledge, only a few simulations have been performed to obtain it. Previous works in this field were based on very simple H$_2$O-OH potentials on the one hand, and on much more time consuming self-interaction-corrected density functional method, on the other hand. These very different approaches lead to a quite different picture of the OH radical solvation in liquid water. Our approach provides a third alternative, realizing a trade-off between computational efficiency and accuracy.

Atomic units ($\hbar = e = m_e = 1$) are used throughout the paper, unless otherwise stated.

II. REFERENCE POINTS GENERATION

We performed multireference configuration interaction (MRCI) calculations with Davidson correction in order to obtain the PES for the two lowest eigenstates of the H$_2$O-OH molecular complex. We used two reference wave functions generated from a complete active space self-consistent field (CASSCF) built on 15 electrons in 11 orbitals. To obtain a balanced description of the two reference states, we took an averaged mean field over the two lowest CASSCF states. All calculations were performed using the MOLCAS quantum chemistry code. We employed a small natural atomic orbital (ANO-S) basis set included in MOLCAS code for both O and H. The contraction is (10s6p3d)(7s6p3d) for oxygen (7s3p3d) and for hydrogen. The basis set superposition error (BSSE) correction was not taken into account.

Our calculations of equilibrium distance $R_e$ and depth $D_e$ for the minimum are reported in Table I, where they are compared to some values collected in the literature. Our MRCI (ANO-S) compares quite well with previous MRCI calculation. The geometries of both calculations are actually slightly different and the ANO-S basis set is slightly larger than the basis set used by Xie and Schaef. Our total energies are thus slightly deeper, though $D_e$ is slightly smaller than the result of Xie and Schaef. For comparison, we computed $R_e$ and $D_e$ with the coupled cluster with single and double excitation and perturbative triple excitation correction (CCSD(T)), which is more correlated and size-consistent. Using the CCSD(T) method with (ANO-S) basis set gives a slightly smoother potential well than our MRCI (ANO-S) calculation.

Figure 1 shows a scan of the PES for OH acting as a donor at several levels of approximation. The scan was performed at a bending angle $\theta_A = 36^\circ$, which corresponds to the geometry of the main minimum obtained by Du et al. We see that our MRCI (ANO-S) approach compares fairly well with the CCSD(T) calculation performed with the much larger aug-cc-VQZP basis set and taking into account the BSSE correction by means of the counterpoise method for each point. We are thus confident in the quality of the PES generated by using the MRCI (ANO-S) method.

The H$_2$O-OH system has nine internal degrees of freedom, corresponding to two interatomic distances for the water molecule, one interatomic distance for the hydroxyl, one bending angle for the H$_2$O, one intermolecular distance between H$_2$O and OH ($R_{OO}$) and four angular coordinates ($\theta_A$, $\phi_A$, $\theta_B$ and $\phi_B$) defining the relative orientation of the two molecules as illustrated in Figure 1 (see also Ref. 18). We fixed the interatomic distances at a common value for the water molecule and the OH radical, $r_{OH} = 1.84$ a.u. and $\alpha_{HOH} = 104.0^\circ$. For H$_2$O-OH complex, the intramolecular degrees of freedom are well decoupled from the intermolecular degrees of freedom. Moreover, for OH embedded in water at thermal energies, the internal vibrational modes have limited amplitudes. It is thus reasonable to fit separately the intermolecular potential energy. In order to scan correctly the PES, we vary $R_{OO}$, $\theta_A$, $\phi_A$, $\theta_B$, and $\phi_B$ (see Ref. 18) to obtain approximately 20 000 points for each PES. We employed 20 $R_{OO}$ values in the range $[4.0, 12.5]$ a.u. with a larger density of points at short distance, where the potential energy varies quickly with $R_{OO}$.

III. FIT FUNCTIONAL FORM

We choose conventionally ($x^2$) > ($y^2$) for the $^2\Pi_1$ state and the reverse for the $^2\Pi_3$ state. The intrinsic degeneracy between these states is lifted when an external electric field is applied on the molecule, as it is the case when OH forms a complex with additional molecules.

Following Spelsberg, we start our analysis from perturbation theory and seek for a matrix representation of the coupled PES for the two lowest energy states of the H$_2$O-OH molecular complex. Denoting H$_2$O by A and OH by B, the potential energy matrix reads

$$U(A, B) = \begin{pmatrix} U_{xx} & U_{xy} \\ U_{yx} & U_{yy} \end{pmatrix}.$$
For a system made of several H$_2$O molecules, we distinguish additive and non-additive contributions. Here, the additivity refers to matrix addition, i.e., the matrix elements are added together to form the resulting many-body interaction matrix $U$. The additive contributions are made of dispersion, electrostatic, and short range interactions as detailed below. Among them, only the dispersion was not given an off-diagonal term and is thus additive in the usual sense of pair energy additivity. The non-additive contribution comes from induction only. For additive contributions we thus evaluate the matrix elements for each pair $(A, B)$ to form $V(B) = \sum_A V(A, B)$. For induction contribution, the field created by the surrounding molecule $C$ on each molecule $D$ is first evaluated, and then the matrix elements evaluated to form the induction energy matrix $W$, as we shall see below.

The energy of one OH radical interacting with several water molecules is thus not simply the sum of the pair interaction energy of OH with each water molecule. It results from the diagonalization of the matrix $U = V + W$. For a system made of two OH radicals, the size extensivity would be obtained by increasing the rank of the matrix to take into account the 4 states asymptotically degenerated for each spin state. In such a case, a model PES could be built, like in the empirical valence bond approach, by coupling the two pairs of states. The coupling needs however to be determined from additional quantum chemistry computations.

To evaluate the interaction matrix of OH with the surrounding water molecules, we first choose a reference frame to orient the OH molecule and to define $x$ and $y$. The matrix $U$ is real and symmetric, so that the energies of the system, computed as the eigenvalues of $U$, are of course real. The energies of the system should also be independent on the frame chosen to orient the OH states $^2\Pi_1$ and $^2\Pi_5$ and invariant under the exchange of $x$ and $y$. If $\phi$ is the azimuthal angle defining the orientation of $^2\Pi_1$ in the reference frame, the symmetry constraints can be expressed as

$$U_{xx}(\phi) = U_0 + U_2 \cos(2\phi),$$

$$U_{yy}(\phi) = U_0 - U_2 \cos(2\phi),$$

$$U_{xy}(\phi) = U_2 \sin(2\phi).$$

Both $U_0$ and $U_2$ depend on the coordinates that express the relative positions of the molecules. $U_0$ is the part invariant under rotation around the OH molecular axis. It contains, for example, the dipole type matrix element common to both $^2\Pi_1$ and $^2\Pi_5$ states. $U_2$ is related to the difference between these two diabatic states and contains, for example, the asymptotic quadrupole contribution from OH, which is different for the $^2\Pi_1$ and $^2\Pi_5$ states.

From an analysis based on second order perturbation theory, the long range interaction energy can be decomposed into electrostatic, polarization, and dispersion contributions. Each contribution can be determined from individual properties of each molecules. In the short range limit, such an analysis is no longer applicable and hydrogen bonding becomes important. We thus damp the electrostatic, polarization, and dispersion interactions and introduce a short range contribution. The equivalence between the two diabatic states is however maintained, and the functional form of $U_{xx}$ and $U_{yy}$ and $U_{xy}$ uses the above decomposition.

Both molecules carry static multipoles and the electrostatic contribution dominates by far the long range interaction. Like many authors in this field, we give to each atom a set of multipoles. The matrix elements are expressed as a function

![FIG. 1. Potential energy curves of H$_2$O-OH system for different levels of calculation.](image-url)
of the atomic multipoles as follows:

$$V_{xy} = \sum_{a=1}^{A} \sum_{k} \sum_{l} \sum_{m} \sum_{n} Q_{k,l,m}^{a} \delta_{n} \langle R_{ab} \rangle T_{i,j,m}^{klm}(R_{ab}) \mathcal{Q}_{k,l,m}^{b,xy},$$

(5)

where $k = k_{a} + k_{b}, l = l_{a} + l_{b}, m = m_{a} + m_{b}$, and $Q_{k,l,m}^{a}$ are the cartesian multipoles of atom $a$ in H$_2$O expressed in the laboratory frame, $\mathcal{Q}_{k,l,m}^{b,xy}$ are the cartesian multipoles of atom $b$ in OH for the matrix element $V_{xy}$ expressed in the laboratory frame and $T_{i,j,m}^{klm}(R_{ab})$ is the corresponding Couleomb interaction tensor. The symmetry constraint regarding the rotational invariance around the OH molecular axis is automatically fulfilled by this expression. This follows from the definition of $\mathcal{Q}_{k,l,m}^{b,xy} = \langle \Pi \rangle_{x,y,z} x^{k} y^{l} z^{m} \Pi_{\gamma}$ in the molecular frame, which possesses necessarily the symmetry of the OH molecule. The function $g_{n}(r)$, with $n = k + l + m$, is a spherically symmetric damping introduced to avoid the unphysical divergence of expression (5) when $R$ approaches 0. We use $g_{n}(r) = (1 - e^{-r^{2}C^{2}})^{n}$. This function produces a shorter ranged damping than the popular Tang-Toennies damping.

The H atoms have only a monopole here, while the O atoms were given a monopole, dipole, and quadrupole. The dipole and quadrupole of each molecule were calculated at the same level of the reference points. There is of course some freedom in the choice of the multipole parameters, provided that the total multipole of each molecule is reproduced. We constrained the oxygen charge of the OH molecule to be $q_{B} = -0.36$. Since the dipole of the molecule is $d_{OH} = -0.65$ a.u., the O atom carries a small dipole $Q_{O,001} = -0.0124$ a.u. along the symmetry axis of the molecule. The oxygen charge in the H$_2$O molecule $q_{A} = -0.7622$ was fitted on a set of long range data obtained for an oxygen-oxygen distance $R_{OO} > 10.0$ a.u. This allows to mimic approximately the small contribution of the missing high-order multipole not included in the fit. The values of the multipoles are given in Table II and in the supplementary material.

The induction interaction is limited to dipole polarizability for the neutral molecules considered here. This interaction is not pairwise additive, and requires to compute the cartesian components of electric field $E_{klm}$ experienced by each molecule to form the induction matrix $\mathbf{W}$. For OH there is one polarization tensor $\alpha^{klm}$ for each matrix element $W_{xy}$.

The electric field is obtained simply as the sum of the multipole contributions from all the surrounding molecules. With the above definitions, the electric field generated at $R_{a}$ by the atom $b$ located at $R_{b}$ reads

$$E_{klm}^{xy}(R_{a}) = \sum_{b} \sum_{k} \sum_{l} \sum_{m} g_{n}(R_{ab}) T_{k,l,m}^{klm} \mathcal{Q}_{k,l,m}^{b,xy},$$

(8)

where we have introduced the same damping function $g_{n}(R_{ab})$ as for the electrostatic contribution to avoid the short range unphysical divergence. The values of the cutoff were chosen so that the polarization is cut moderately at equilibrium distance, which ensures a better transferability to condensed phase. The value of the polarizability tensor were taken from Refs. 19 and 25. They are given in cartesian form in Table III.

The dispersion interaction is limited to its leading isotropic contribution to $R^{-6}$ and $R^{-8}$. The latter was introduced because its coefficient $C_{6}$ is relatively large with respect to $C_{8}$. For the same reason, we also introduced dipolar $C_{7}$ terms. There is no higher multipole moments included in our dispersion term, and therefore $V_{xy} = 0$ and $V_{xx} = V_{yy}$. The complete expression for dispersion interaction reads

$$V_{xx} = g_{6}(R) \frac{C_{6}}{R^{6}} + g_{8}(R) \frac{C_{7}}{R^{8}} \hat{R} \cdot \mathbf{u}_{A}$$

$$+ g_{8}(R) \frac{C_{8}}{R^{8}},$$

(9)

where $R$ is taken as the oxygen-oxygen distance, $\hat{R}$ is the unit vector $R/R$, and $\mathbf{u}_{A}$ and $\mathbf{u}_{B}$ are the unit vectors oriented along the dipole of the molecules $A$ and $B$, respectively. The values

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The tables above are used for the parameterization of H$_2$O-OH interaction. For OH, $Q^{*}_{ijk}$ is given. The other cases are deduced by symmetry: $Q^{*}_{ijkl}$ = $Q^{*}_{ijlk}$ and $Q^{*}_{1100} = Q^{*}_{2000} = Q^{*}_{0200} = 1/4 (Q^{*}_{2000} - Q^{*}_{0200})$. Only non-vanishing multipoles are given. The values $Q^{*}_{ijk}$ are the actual molecular multipoles resulting from our parameterization.
of the coefficient were computed from the dynamic polarizabilities given in the works of Meyer and Spelsberg.\textsuperscript{19, 25} They are given in Table IV.

The short range part of the interaction potential is dominated by hydrogen bonding. It is far from isotropic and for the sake of accuracy, we represent it as a sum of bond functions, which depends on the orientation of the bond with respect to the body-fixed frame of the molecules A and B. The matrix element expansion of Eqs. (2)–(4) are obtained from $V_m$ defined as follows:

$$V_m = \sum_{a \in A} \sum_{l_a, m_a} \sum_{b \in B} \sum_{l_b} \sum_{k} c_{a l_a m_a b l_b m_k} f_{a b k} (R) Y_{l_a m_a} (\Omega_A) Y_{l_b m_k} (\Omega_B)$$  

(10)

with $m = 0, 2$ and $Y_{lm}$ are real spherical harmonics. For the radial functions, we use a set of gaussian functions $f_{a b k} (R) = e^{-\gamma_{a b} R^2}$. The complete parameterization is given in the supplementary material.\textsuperscript{18} The choice of index for the spherical harmonics depends on the symmetry of the molecule. In the following, the symmetry axis of the molecule is aligned along the $z$ cartesian axis. For hydroxyl (B), we can have only $m = 0, 2$ and it was sufficient to limit $l_b \leq 2$. For the water molecule (A), the $C_2v$ symmetry constrains $m_a = 0, 2$ for the bond linked to the O atom. For the bond linked to the H atom, the parity of $Y_{l_m}$ should be such that the combination of the two bonds in the water molecule respects the $C_2v$ symmetry and thus $m_a = -1, 0, 2$. It was sufficient to limit $l_a \leq 3$ for the water molecule.

The strong repulsion experienced by two very close nuclei is far above the energy of interest here and we simply represent this interaction by one repulsive function $C_{AB} e^{-\gamma_{AB} R^2} / R$ for each pair of atoms. The latter interaction avoids in particular unphysical deep wells in the PES at very short distance. The values of the parameters are given in the supplementary material.\textsuperscript{18}

It is important to note that, despite their apparent complexity, the computation of the matrix element for electrostatic, dispersion, and short range contribution reduces actually to a sum of pairwise interactions between the atoms of molecule A and those of molecule B.

### IV. FITTING PROCEDURE

Before fitting the PES, a large set made of approximately 20 000 geometries was generated and the corresponding adiabatic energies calculated. In a first step, the long range interaction potential corresponding to distances $R_{OO} \geq 10$ atomic units was fitted by adjusting the oxygen charge in water and one exponentially screened function associated with 5 spherical harmonics on H-O-H bonds, according to expression (10).

In a second step, we retained the geometries for which the energy of the first PES is located in the range $[-0.01; +0.01]$ a.u. around the asymptotic energy of the dissociated complex.

For the second PES, some of the corresponding energies are much higher, in particular for short $R_{OO}$. We retain thus approximately 16 000 geometries, associated each with one energy for each PES. The points were fitted by a standard least-square fit procedure with equal weights to ensure a correct balance between all the points retained for the fit.

The global accuracy of the fit is illustrated in Figure 2, where we plotted the energy difference $\delta = E_{\text{fit}} - E_{\text{ref}}$, as a function of the reference energies $E_{\text{ref}}$. The standard deviation is better than $10^{-4}$ a.u. (i.e., approximately 20 cm$^{-1}$). Most of the reference points lay between the two lines $\delta \pm 2 \times 10^{-4}$ a.u. The dispersion is slightly larger for the second PES for the highest energies. Such an accuracy is reached with a limited set of 242 parameters in the present case. This is rather modest regarding the complexity of the coupled PES and the relatively broad range of energy retained for the fit.

Beside its intrinsic quality, the interest of a matrix formulation to represent the surface can be observed near the PES crossings or avoided crossings. In Figure 3, we have plotted a few cuts of the PES for a planar H$_2$O-OH complex. Each PES is associated with a given symmetry $A'$ or $A''$ of the $C_2$ symmetry group and can thus cross each other. The $A'$ symmetry corresponds to the singly occupied orbital perpendicular to this plane. The relative orientation of the molecules in the plane is given by $\theta_A$ and $\Delta = \theta_A - \theta_B$, where $\theta_A$ and $\theta_B$ are, respectively, the direction of $\mathbf{R}_{OO}$ and the direction of the OH radical axis with respect to the symmetry axis of the water molecule (see Ref. 18). Thus, $\Delta = 0$, corresponds to the hydroxyl aligned along the O-O direction and the hydrogen pointing outward. The scan is taken at $R_{OO} = 5.5$ a.u., which corresponds approximately to the equilibrium distance of the main minimum. As it can be observed in Figure 3, the fit is remarkably close to the control data, though the latter points were not included in the fitting procedure. In particular, the PES crossings are faithfully reproduced by our matrix potential approach, while they would be terribly difficult to obtain with a scalar fit of the adiabatic PES.

| TABLE IV. Dispersion coefficient used in the fit. |
|---|---|---|---|
| $C_6$ | $C_7A$ | $C_7B$ | $C_8$ |
| $-40$ | $+50$ | $+50$ | $-1200$ |

FIG. 2. Energy difference between the fitted and reference PES as a function of the computed reference energy.
FIG. 3. Potential energy of the H$_2$O-OH complex as a function of $\Delta$ for some selected $\theta_A$ and $R_{OO} = 5.5$ a.u. From bottom to top: $\theta_A = 0^\circ$, $\theta_A = 38^\circ$, $\theta_A = 76^\circ$, $\theta_A = 104^\circ$. The points are calculated control data and the lines correspond to the fit.

V. PES ANALYSIS

The impact of the PES crossings is not negligible as they are located around the secondary minimum, which controls the formation of hydrogen bond when OH acts as an acceptor and thus controls the motion of the atoms in the corresponding basin. A contour plot of both PES is shown in Figure 4 for $R_{OO} = 5.8$ a.u. We can observe a series of minima in this PES cut. For both PES, the deepest minimum, on the right-bottom corner ($\Delta = 180^\circ$, $\theta_A = 0^\circ$) comes from the saddle point between the two symmetric main minima associated with OH acting as a donor. For the ground state PES, the second minimum on the upper right part of the figure ($\Delta \approx 80^\circ$, $\theta_A \approx 110^\circ$) comes from the secondary minimum associated with H$_2$O acting as a donor. The figure shows clearly that this minimum is extremely shallow. For the second PES, the trace of the secondary minimum ($\Delta \approx 20^\circ$, $\theta_A \approx 110^\circ$) is even more shallow in this plane. For this minimum, the equilibrium O-O distance is actually slightly larger than the value taken for this scan. The gap along the minimum energy path connecting the secondary minimum of a given PES to its associated main minimum is less than $5 \times 10^{-4}$ a.u. (100 cm$^{-1}$) for the lowest PES and slightly larger for the second PES. For the ground state PES, we can observe another shallow minimum on the upper left side of Figure 4 ($\Delta \approx -60^\circ$, $\theta_A \approx 120^\circ$). It is linked to the basin of the secondary minimum by rotation of the water molecule around the OH direction at constant $\theta_A$. The main penalty comes from the multipole interaction, which is less favorable for this orientation. This seeming minimum is connected, without energy barrier, to the secondary minimum on the upper right side of the figure. The secondary minimum is thus characterized by two directions of easy motion along which the deformation of the structure would be controlled essentially by steric effects in condensed phase.

Figure 4 shows also the surface crossings, which can be followed by looking at the singular points along the iso-energy curves in the PES cut. At these points, an iso-energy line on the lowest PES continues by a line on the second PES and vice versa. One such crossings is visible around $\Delta \approx 20^\circ$.

FIG. 4. Potential energy contour of the H$_2$O-OH complex as a function of $\Delta$ and $\theta_A$ for $R_{OO} = 5.8$ a.u. The red lines correspond to the lower PES and the blue lines to the upper PES. The iso-energy lines are separated by $2.5 \times 10^{-3}$ a.u.
for $\theta_A = 20^\circ$–$100^\circ$. Another one can be observed on the right hand side of the figure from $\Delta \approx 150^\circ$ and $\theta_A = 20^\circ$ up to $\Delta \approx 80^\circ$ and $\theta_A = 70^\circ$. A third crossing can also be observed on the left hand side of the figure for $-40^\circ$ to $-70^\circ$ and $\theta_A = 30^\circ$–$60^\circ$. At these crossings, the orientation of the hydroxyl quadrupole changes and thus influences the course of the dynamics in MD simulation.

VI. TRANSFERABILITY

To investigate the hydroxyl radical in solution, the $\text{H}_2\text{O}$-$\text{OH}$ intermolecular potential needs to be combined with a model for water molecule interaction. Our fit is combined here with the mobile charge density in harmonic oscillator (MCDHO) model. Many alternative models taking explicitly the polarization into account and providing accurate radial distribution functions might be used instead of the MCDHO model. The polarization in the MCDHO model is based on an electric charge harmonically bound to the O atom of the water molecule and interacting by means of screened Coulomb interaction with the other charges of the MCDHO model. We modify slightly our model to make it compliant with the MCDHO model as follows. We simply replace the polarization of the water molecule (Eq. (7)) by the interaction of the hydroxyl multipoles with the mobile charge. For the sake of simplicity, we neglect the small difference in the water molecule polarization by the two OH diabatic states by taking the trace of the electric field tensor defined in Eq. (8). The polarization of the water molecule reduces thus to a diagonal matrix equivalent to the scalar potential energy used for a single PES model. The potential energy induced by polarization of a water molecule by the hydroxyl is simply the difference $U_B(q_A) - U_B(q_B^0)$ where $q_A$ is the equilibrium position of the mobile charge associated with the water molecule A in solution, $q_B^0$ its equilibrium position for the free molecule A at the same geometry, and $U_B$ the electrostatic interaction energy of the mobile charge with the hydroxyl multipoles. The increase of internal energy by polarization comes simply from the interaction of the mobile charge with the atomic charge of the water molecule. The polarization of $\text{H}_2\text{O}$ becomes therefore the polarizability of the MCDHO model.

In the simulation, the positions of all the mobile charges are obtained by minimization of the energy with respect to their positions. The corresponding self-consistent equations are solved iteratively for each move in the MC simulation. The modification of the energy functional and water polarizability with respect to our original fit functional leads to a small energy difference of the order of $2 \times 10^{-2}$ a.u. (roughly $40 \text{ cm}^{-1}$) at the geometry of the main minimum. This difference originates partially from the difference between the water molecule polarizability tensors of the MCDHO model and the one used in our fit.

To have the possibility to study the OH deformation in solution, the hydroxyl molecule is flexible in our simulation. Its internal energy is taken from a fit to the internal OH energy which completes the representation of the two lowest PES of a system made of several water molecules. The modification of the OH length is actually very small because of the large difference in energy scale between the internal and external degrees of freedom. The resulting small perturbation of the multipoles is neglected here.

We perform a transferability test by analyzing the ($\text{H}_2\text{O})_2\text{OH}$ trimer for various geometries. We take 100 geometries made of the two closest neighbors of OH from MC sampling of the liquid as described in Sec. VII. We also take 50 configurations of the isolated trimer from MD runs of 10 ps each and starting at the equilibrium geometry with a set of velocities sampled from a Maxwell-Boltzmann distribution at a temperature $T = 300 \text{ K}$. Finally, we perform a scan by moving the OH along the direction defined by the positions of the hydroxyl oxygen and the middle of the two water oxygens at equilibrium. A common offset energy corresponding to the asymptotic position reached along this direction is subtracted to all the computed energies. We present in Figure 5, a plot of the correlation between the values of the fit and the corresponding $ab$ initio energies computed with the MRCI method and ANO-S basis set described in Sec. II.

The observed correlation is quite good for both states. We observe a small systematic deviation from perfect correlation. The fit underestimates the depth of the basin explored around the equilibrium geometry as can be observed from the points deduced from the MD runs and the scan along $\mathbf{u}_J$. The repulsion along this direction is largely overestimated for the shortest distances between the OH and the two water molecules. In this range, the PES is very steep and this large energy deviation corresponds actually to a rather small position shift, of the order of 0.02 a.u., which has thus a minor influence on the radial distribution function presented in Sec. VII. Moreover, this repulsive wall is not explored during MD simulation, as it can be deduced from the corresponding points plotted in Figure 5.

The average dispersion around the perfect correlation line is of the order of $10^{-3}$ a.u., which is comparable to the dispersion reported for the authors of the MCDHO model. The
three-body interaction is not excellent for this model according to its authors. A part of the observed deviation observed in Figure 5 comes from the water-water interaction, and the use of alternative model, with a more consistent treatment of the polarization to represent this interaction, might produce a better result. Finally, it is interesting to note that the energy difference between the two adiabatic PES is quite well reproduced by the fit. This indicates that most of the error comes from the trace of the model and that the proposed diabatic approach has the proper functional form to represent the interaction of OH with water.

VII. STRUCTURAL PROPERTIES OF OH RADICAL IN SOLUTION

We investigate the properties of OH in liquid water by means of MC sampling with the Metropolis algorithm in the $NVT$ ensemble. The density of the liquid is thus held constant at 1.0 g/cm$^3$ and the temperature is $T = 300$ K. The liquid is represented by a cubic box containing 125 molecules with periodic boundary conditions and we used the minimum image convention. We sample the molecular moves by combining a translation of the molecule center of mass and a rotation around one of the axis chosen randomly. The largest amplitude for translation and rotation were 0.3 a.u. and 0.3 radians, respectively. The internal moves are sampled by combining a translation of each atom of the molecule. Since this motion is energetically much more expensive, the largest amplitude was limited to 0.02 a.u. As usual for MC simulation, the sampling amplitude was scaled in the course of the simulation to ensure a ratio of 50% between acceptance and trial. The results were obtained by sampling $2 \times 10^8$ moves after a relaxation run of $10^7$ moves.

Since the OH radical has two degenerate electronic states, it is a priori necessary to consider both PES to sample the configuration of the liquid. Generally speaking, it is important to use a diabatic representation as we did, so that the contributions of the water molecules add coherently with each other. If only the adiabatic energy were added, the energy difference between the two PES would be unphysically too large.

Considering the isolated H$_2$O-OH complex, the energy difference between the two PES varies significantly with the geometry. In the area of the main minimum, it is of the order of $10^{-3}$ a.u. (roughly 200 cm$^{-1}$) and increases when the oxygen-oxygen distance diminishes. However, in a large portion of the configuration space, where OH acts as an acceptor, the energy difference between the two PES is significantly larger. For the configurations relevant for MC sampling in solution, it is likely to find at least one of the water molecules in such a position and the energy difference is of the order $8 \times 10^{-3}$ a.u. (approximately 1600 cm$^{-1}$). This is roughly 8 times larger than $k_B T$ at $T = 300$ K. In this case, the relative weight of the second PES is less than $10^{-4}$ and it plays thus only a minor role.

The oxygen-oxygen radial distribution function, $g_{OO}(R)$, around the OH radical is shown on top of Figure 6. It is quite similar to its counterpart for pure water. We observe a broadening and a small shift of the first peak position at 5.4 instead of 5.3 a.u. with the MCDHO model. The broadening comes from the difference of the two minima in the H$_2$O-OH PES with respect to the corresponding main minimum of the H$_2$O–H$_2$O PES. This peak does not present any sharp structure as reported in previous study based on a simplified PES. The position of the first minimum is 7.7 a.u. and we found approximately 9 oxygen atoms inside this first coordination shell. However, all these molecules are not hydrogen bonded to the OH radical.

The hydrogen-oxygen distribution function, $g_{HO}(R)$, is depicted in the middle panel of Figure 6. It corresponds to the distribution of water (A) oxygen with respect to the hydroxyl (B) hydrogen. For $R < 8.0$ a.u., the distribution is significantly different from the pure water distribution, while both distributions become identical for larger distance. We also notice a sharp contrast with the results reported by Cabral de Couto and co-workers, who observed a well-defined sharp peak at short distance ($R = 3.1$ a.u.). In our case the first peak is located around $R = 3.4$ a.u., at a slightly shorter distance than for pure water. As noted previously for water, the role of polarization is essential to ensure a correct transferability of the fitted PES from isolated bimolecular complex to condensed phase. A similar simulation neglecting the polarization produces a donor hydrogen bond centered around $R = 3.7$ a.u. instead. The first peak is higher than its counterpart for pure water. This is mainly due to the presence of the second peak in the radial distribution function. The latter is centered around $R = 6.5$ a.u. but it is significantly broader than its counterpart for pure water. The broadness reflects the shape of the H$_2$O–OH PES around the secondary minimum, in which the

![FIG. 6. Radial distribution functions for OH in solution and for pure water. Continuous line: OH radical solvated in water. Dotted-dashed line: pure water.](image-url)
motion associated with thermal fluctuations is large. The global shape of \( g_{\text{HO}}(R) \) is consistent with the distribution obtained with SIC-DFT methods. The position of the peaks and their relative displacement with respect to those of water distribution are similar. However, the SIC-DFT simulation produces a first minimum (around \( R = 4.5 \) a.u.) much deeper for both water and OH in solution and the MCDHO model is in better agreement with experiment than DFT in this aspect.

Despite the difference in the first hydration shell structure, the coordination number obtained by integration of \( g_{\text{HO}}(R) \) up to the second minimum at \( R = 8.7 \) is of the order of 13 for both hydroxyl solution and pure water. The integration of the first peak up to the first minimum at \( R = 4.5 \) a.u. yields \( n_{\text{HO}} = 1.2 \). We have thus essentially one \( \text{H}_2\text{O–HO} \) tightly bound complex in the middle of 12 water molecules.

The hydrogen-hydrogen distribution function, \( g_{\text{HH}}(R) \), is depicted in the bottom panel of Figure 6. The well defined structures observed for pure water disappear for OH in solution. This is a clear indication of a loss of directionality in the hydrogen bonding of \( \text{H}_2\text{O} \) with OH. There is no second hydrogen bond like in pure water to define a preferential solid angle around the molecule so that the donor water molecules evolve relatively freely around the O atom of the hydroxyl.

The oxygen-hydrogen distribution function, \( g_{\text{O–HO}}(R) \), is depicted in the upper panel of Figure 7 and the corresponding radial distribution for different polar sectors in its lower panel. A sector is defined by \( \theta \) such like \( \cos \theta_{n} < \cos \theta < \cos \theta_{n+1} \) with \( \cos(\theta_{n}) = -1 + 2n/9 \) so that all solid angles are equal. The hydroxyl acts here as a proton acceptor. The well defined two-peaks structure observed for water is distributed in a broad structure between \( R = 3.0 \) and \( R = 8.0 \) a.u., while the shape of \( g_{\text{O–HO}}(R) \) becomes identical for larger \( R \). The difference between \( g_{\text{HO}}(R) \) and \( g_{\text{O–HO}}(R) \) reflects the difference in the hydrogen bonds when OH acts as a donor or an acceptor. In the latter case, the hydrogen bond is significantly weaker than the hydrogen bond between two water molecules and the \( \text{H}_2\text{O–OH} \) PES is rather smooth around the second minimum, as we discussed in Sec. V. Such a broad basin has a significant statistical weight so that several water molecules can fit inside, without tight angular constraint.

Looking more specifically at the variation of \( g_{\text{O–HO}}(R) \) with the polar angle, the distribution evolves from a single peak structure at \( R = 6.2 \) in the first sector (\( \cos \theta < -0.78 \)) to a uniform distribution whose inset changes smoothly with the angle. The peaks in \( g_{\text{O–HO}}(R) \) for \( \theta \in [180^\circ, 141^\circ] \) originate from the single water molecule tightly bound to the radical. The number of molecules in the coordination shell limited by the minimum at \( R = 8.7 \) is of the order of 13 for pure water as well as for OH solution, despite the changes in the shape of \( g_{\text{O–HO}}(R) \), the number of molecules is comparable for pure water and OH in solution.

The number of hydrogen bonds with OH can be obtained by integration of \( g_{\text{HO}}(R) \) and \( g_{\text{O–HO}}(R) \) up to some given distance \( R_c \) a.u. For \( R_c = 4.5 \), we obtain \( \eta_{\text{HO}}(R_c) = 1.2 \) and \( \eta_{\text{O–HO}}(R_c) = 1.5 \). The ratio \( \eta_{\text{O–HO}}(R_c) / \eta_{\text{HO}}(R_c) \) increases continuously from 1 at \( R_c = 3.0 \) to 2 at \( R_c = 6.0 \) and then stay constant at 2 for larger \( R_c \).

VIII. CONCLUSION

We developed a model based on second order perturbation theory to fit the degenerate PES of the \( \text{H}_2\text{O–OH} \) molecular complex. The analysis leads to the definition of two diabatic states, which deduces from each other by rotation around the OH molecular axis. These states define a 2 \( \times \) 2 potential energy matrix, which is diagonalized to obtain the two PES of the complex. Each matrix element is decomposed in a standard way into short range, electrostatic, dispersion, and polarization interactions.

The fit was performed with a large set of 20 000 points for each PES and allows to reproduce the details of the PES with a limited number of parameters regarding the complexity of the surfaces. In particular, the PES for planar geometries around the secondary minimum where OH acts as an acceptor are faithfully reproduced, despite the presence of surface crossings and the existence of shallow minima and ridges. As noted by other authors, the secondary minimum of the \( \text{H}_2\text{O–OH} \) molecular complex, where the hydroxyl acts as an acceptor, is not as deep as the first minimum or the water dimer main minimum. Our study shows that this minimum has a rather broad basin and is connected by a very small energy gap to the main minimum basin. Our fit allows to compute the PES with an accuracy of the order of \( \pm 10^{-4} \) a.u. for energies ranging from the minimum up to \( 10^{-2} \) a.u. (2000 cm\(^{-1}\) = 6.27 kcal/mol) above the dissociation limit.
The model of H$_2$O-OH interaction is both flexible and polarizable. It can thus be used for geometries of H$_2$O and OH close to their equilibrium geometries and to investigate OH solvated in water clusters, or in water under various thermodynamic conditions.

The two-state approach offers unique insights about the relative role of both PES for OH in liquid water. In particular, we observe that the energy separation between the two PES is of the order of $8 \times 10^{-3}$ a.u. (1600 cm$^{-1}$) on the average at $T = 300$ K and for a density of 1.0 g/cm$^3$. The second PES contributes therefore marginally under these thermodynamic conditions. However, this result might change significantly for higher temperature and lower density.

The radial distribution function deduced from our PES by MC sampling of the configuration space at $T = 300$ K and for a density of 1.0 g/cm$^3$ reveals a structure dominated by one single strong hydrogen bond between the donor hydroxyl and an acceptor water. The HO radial distribution function shows a well defined peak at $R_{HO}$ comparable to $R_{HO}$ in the free H$_2$O-OH complex to 3.4 illustrates the significance of the polarization, which increases the molecular dipoles in solution. The broad basin around the secondary minimum of the H$_2$O-OH complex does not give rise to well defined structure in the various radial distribution functions. The well depth of this secondary minimum is actually smaller than the H$_2$O-H$_2$O complex main minimum and is thus energetically not favorable. These results are consistent with the picture provided by simulation based on SIC-DFT electronic structure.

Finally, the present PES model provides a practical mean to investigate OH in aqueous environment under various thermodynamic condition with confidence. Regarding the performance for MD simulations, the computation time is actually dominated by the polarization terms, which are by far the most time consuming terms, despite the relatively large number of parameters involved mainly in the short range function. An elementary implementation of the force evaluation without any parallelization shows that the model is practical for MD simulation.

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18. See supplementary material at http://dx.doi.org/10.1063/1.4826319 for the values of the parameters.