Voltage balancing in three-level neutral-point-clamped converters via Luenberger observer

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Abstract

This paper addresses the problems associated with the dc-link capacitor voltages of the three-level neutral-point-clamped power converter: the imbalance of the capacitor voltages as well as the presence of an ac-voltage low-frequency oscillation in the dc link of the converter. In order to cope with them, a mathematical analysis of the capacitor voltage difference dynamics, based on a direct average continuous model, is carried out, considering a singular perturbation approach. The analysis leads to a final expression where a sinusoidal disturbance appears explicitly. Consequently, the two problems can be handled together using the ordinary formulation of a problem of regulating the output of a system subject to sinusoidal disturbances, applying classical control theory to design the controller. In this way, the controller is designed including the disturbance estimate provided by a Luenberger observer to asymptotically cancel the disturbance, while keeping also balanced the capacitor voltages. Experiments for a synchronous three-level neutral-point-clamped converter prototype are carried out to evaluate the performance and usefulness of the converter working as a grid-connected inverter under the proposed control law.

Keywords: Multilevel power converter, neutral-point-clamped (NPC) converter, voltage balancing, disturbance rejection, Luenberger observer

1. Introduction

In the field of power conversion, more specifically in the three-level neutral-point-clamped (NPC) converter [1], there exists a phenomenon concerning the presence of sinusoidal disturbances: a low-frequency voltage ripple is present in the neutral point of the dc link [2, 3]. Concretely, the voltage difference of the dc-link capacitors fluctuates at three times the fundamental frequency of the ac-side voltage. Note that, in this topology, probably the most extensively applied at present multilevel topology [4, 5], the dc link consists of two capacitors. Thus, if the converter is connected to the grid, the ac-voltage fluctuation has a frequency of 150 Hz, that is, 3 × 50 Hz.

This phenomenon affects the balance of the capacitor voltages, and although, based on results reported by other researches, it does not limit the usefulness of the converter for practical applications, it represents a significant drawback since the capacitors must be designed to stand the oscillation. In this way, several strategies have been proposed [6, 7] to cope with the problem, including the use of novel modulation techniques [8], or improving the performance of others previously considered [9], to name a few. Important research is still being made in this field considering various approaches [10, 11].

In addition to the elimination of the neutral-point voltage oscillation, the balancing of the dc-link capacitor voltages, which is the main technical challenge of the NPC topology, should be guaranteed. The voltage imbalance problem, that produces a voltage difference between the capacitors causing undesirable distortion at the converter ac side, has been widely investigated for this topology [12, 13]. Some modulation strategies provide natural voltage balancing. Nevertheless, in any other case, additional control effort is required. Significant results concerning the implementation of distinct voltage balancing techniques have been achieved [14, 15, 16, 17]. Among these techniques, some are based on the exploitation of the redundant switching states of the converter [18]. In other words, they are based on the use of those different positions of the converter switches that lead to the same generated voltage, but they cause different effects on the capacitor voltages.

Therefore, there are two problems associated with the dc-link capacitor voltages of the three-level NPC converter: (i) the voltage imbalance of the dc-link capacitors and (ii) the presence of the ac-voltage low-frequency oscillation in the dc link. This paper addresses both problems, considering a continuous model of the converter [19], which includes the dynamics of the voltage difference between the dc-link capacitors. Focusing on these dynamics, a mathematical analysis of their behavior is carried out, under the assumption of different time scales, that is, adopting a singular perturbation approach\textsuperscript{1}. This analysis yields an approximated model where a sinusoidal function of time whose frequency is three times the fundamental frequency of the ac-side voltage appears explicitly. Consequently, the two problems related to the dc-link capacitor voltages can be han-

\textsuperscript{1}The authors also have worked out analysis of the converter dynamics in other multilevel topologies, e.g., in the five-level diode-clamped converter [20] and in the three-level diode-clamped back-to-back converter [21].

dled together using the conventional formulation of a problem of regulating the output of a system under the presence of sinusoidal disturbances [22, 23], applying also classical control theory to design the controller. In this manner, the analysis provides, compared with the strategies usually considered to deal with these problems, an alternative control approach.

1.1. Rejection of sinusoidal disturbances

The effectiveness of a system can be seriously deteriorated by the presence of sinusoidal disturbances. In the field of power electronics, some well-known examples are the harmonic currents generated by non-linear loads in systems that incorporate rectifiers such as variable speed drives or uninterruptible power supplies [24], and the harmonic current in the neutral conductor of four-wire three-phase dc-ac converters [25]. However, sinusoidal disturbances also appear in many other engineering applications such as active noise and vibration control systems [26], optical and hard disk drives [27], helicopter rotor blades [28], and dc and stepper motors [29], among others.

Even though the problem of identifying and asymptotically rejecting sinusoidal disturbances has been widely studied over the years, it continues attracting special interest [30, 31, 32]. In what follows, some control approaches considered to deal with this problem are mentioned:

1. One of the most popular methods is based on the internal model principle [33]. This property states that, to achieve perfect cancelation, any regulator which solves the problem in question should incorporate in the feedback a replicated model of the dynamic structure of the disturbance which must be tracked and/or rejected.

2. Adaptive control techniques are commonly used when the disturbance parameters are unknown, applying the estimate of the disturbance to reject the disturbance at the input of the plant [34, 35, 36].

3. Other approach proposed solves the posed problem by implementing an adaptive observer of the disturbance [37, 38]. This observer is then incorporated in the controller.

In this paper, considering the approximated model derived from the analysis of the converter dynamics, an asymptotic disturbance rejection approach is considered. Thus, the controller proposed implements a Luenberger observer to estimate the disturbance. Then, the disturbance estimate is used to asymptotically cancel the sinusoidal disturbance, including also in parallel another control action for ensuring the regulation of the capacitor voltages as well.

It is important to point out that this paper is an extension of the work presented in [39], showing some remarkable differences and improvements. In that paper, the mathematical analysis is formulated in a NPC rectifier for a particular operating condition. Nevertheless, in the current paper, the analysis is carried out considering the inverter operation mode, leading to a general result valid for any converter operating point. In addition, experimental results for a synchronous three-phase three-level converter prototype are included, corroborating in this manner the mathematical analysis worked out. Conclusions derived from the study of the frequency spectrum of the capacitor voltage difference also are discussed in this paper.

The outline of the paper is as follows. First, the model of the converter is described in Section 2, and the control objectives to achieve are stated in Section 3. Then, Section 4 is devoted to the analysis of the dc-link capacitor voltage difference dynamics. Afterwards, Section 5 presents the proposed controller, which is based on the disturbance estimation carried out by a Luenberger observer. Simulation and experimental results obtained with a laboratory converter prototype are discussed, respectively, in Section 6 and in Section 7. Finally, some conclusions are presented in Section 8.

2. Model of the system

Figure 1 illustrates a schematic diagram of the three-phase three-level NPC converter working as an inverter connected to
the grid, which is the setup considered in this paper. The dc-link of the converter is composed of capacitors $C_1$ and $C_2$, both of same capacitance $C$. Their respective voltages are represented by $v_{c1}$ and $v_{c2}$. Besides, the total dc-link voltage is defined by $V_{dc}$. Phase voltages are denoted by $v_{a}, v_{b}$ and $v_{c}$, and the phase currents in the inductors $L$ by $i_{a}, i_{b}$ and $i_{c}$. Notice that no fourth wire is introduced in the circuit.

The voltages generated in points $a$, $b$, and $c$, with respect to dc-link neutral point $o$, are denoted by $v_{oa}, v_{ob}$ and $v_{oc}$, respectively. These generated voltages depend on the switching states of the converter, which are determined by the set of discrete values of the gating signals $\delta^a, \delta^b$ and $\delta_c$ as follows

$$\delta^i = \begin{cases} 
1 & \rightarrow S_1' \text{ on,} \quad S_2' \text{ on} \quad \rightarrow v_i = v_{c1} \\
0 & \rightarrow S_1' \text{ off,} \quad S_2' \text{ on} \quad \rightarrow v_i = 0 \\
-1 & \rightarrow S_1' \text{ off,} \quad S_2' \text{ off} \quad \rightarrow v_i = -v_{c2},
\end{cases}$$

for $i = a, b, c$.

Considering this preliminary description, the model of the three-level NPC back-to-back converter presented in [19] is adapted to the three-level NPC inverter application of the present paper. This model is based on a direct average of the characteristics and waveforms associated with each of the components of the converter. Besides, the control inputs of the model are defined by $\delta^a, \delta^b$ and $\delta_c$, and they represent the averaged values of the gating signals (1) in a switching period. Because these control inputs are implemented through a modulator to obtain the gating signals, they should be located within the domain

$$D_{\delta_{abc}} \in \mathbb{R}^3 := D_{\delta_{a}} \times D_{\delta_{b}} \times D_{\delta_{c}},$$

where $D_{\delta_{a}} = [-1, 1]$ for $i = a, b, c$, to generate correctly the switching sequence.

As a result, the inverter model, expressed in stationary $a\beta\gamma$ orthogonal coordinates by means of the power-invariant form of the Clarke Transform, describes the dynamics of the phase currents and of the voltage difference between the dc-link capacitors. It is defined by

$$\begin{align*}
L \frac{di_a}{dt} &= -v_{o} + \delta^a \frac{v_{dc}}{2} \left( \frac{\delta^a \delta^\gamma - \delta^b \delta^\gamma}{\sqrt{3}} + \frac{\delta^2 - \delta^b}{2 \sqrt{6}} \right) v_d \\
L \frac{di_b}{dt} &= -v_{o} + \delta^b \frac{v_{dc}}{2} \left( \frac{\delta^b \delta^\gamma - \delta^c \delta^\gamma}{\sqrt{3}} + \frac{\delta^2 - \delta^c}{2 \sqrt{6}} \right) v_d \\
C \frac{dv_d}{dt} &= -\frac{2}{\sqrt{3}} \left( \delta^a i_a + \delta^b i_b \right) \delta_{\gamma} - \frac{1}{\sqrt{6}} \left( \left( \delta^2_a - \delta^2_b - \delta^2_c \right) i_a - 2 \delta^a \delta^b i_b \right),
\end{align*}$$

where $v_d$ is the dc-link capacitor voltage difference

$$v_d = v_{c1} - v_{c2}.$$  

Notice that the phase currents and the phase voltages are transformed from $abc$ into $a\beta\gamma$ coordinates, yielding the current variables $i_a$ and $i_b$, and the voltage variables $v_o$ and $v_d$, respectively. Moreover, the control inputs also are transformed into $\delta^a, \delta^b$ and $\delta_{\gamma}$. Table 1 summarizes the variables of the system.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$i_a, i_b$</td>
<td>Phase currents</td>
</tr>
<tr>
<td>$v_o, v_d$</td>
<td>Phase voltages</td>
</tr>
<tr>
<td>$\delta^a, \delta^b, \delta_{\gamma}$</td>
<td>Control inputs</td>
</tr>
<tr>
<td>$v_d$</td>
<td>DC-link capacitor voltage difference</td>
</tr>
</tbody>
</table>

3. Control objectives

As pointed out before, this paper addresses the problems associated with the dc-link capacitor voltages of the three-level NPC converter. With the aim of overcoming them, two specific control objectives are stated:

1. The dc-link capacitor voltage difference $v_d$ should be kept close to zero, remaining within a domain containing zero.

2. The low-frequency voltage ripple present in the dc-link neutral point should be reduced to an acceptable level.

Concerning the first control objective, it entails the practical stability [40] of the system. This concept, also referred to as ultimate boundedness [41], deals with the boundedness properties of the state of a dynamic system. This requirement is due to factors such as component imperfections, transients, or other imbalances in the converter [12]. Moreover, it is also related to the fact that the positions of the power switches of the converter are restricted to belong to a finite set [42].

With regard to the second control aim, it is defined to ensure a good performance of the converter. Note that if the sinusoidal disturbance is neglected and no control method is devoted to mitigate its effect, there is an increase in the power losses of the system, and the operating life of the capacitors is decreased.

It is worth stressing that there also exists another control objectives which can be defined in relation to the instantaneous powers of the three-phase circuit:

3. The instantaneous active and reactive powers, denoted by $p$ and $q$, respectively, and defined as

$$p = v_o i_a + v_o i_b + v_o i_c = v_a i_a + v_b i_b + v_c i_c$$

$$q = \frac{1}{\sqrt{3}} \left( (v_{sa} - v_{sb}) i_c + (v_{sb} - v_{sc}) i_a + (v_{sc} - v_{sa}) i_b \right)$$

$$= v_a i_b - v_b i_a,$$

should be driven to their respective references $p^*$ and $q^*$.

Remark 1. Although the rest of the paper is focused on the first two control objectives, it is necessary to design some other control loop, because the third control objective should be also fulfilled. In the following, it is assumed that there exist certain appropriate controller that deals with the regulation of the variables $p$ and $q$. Specifically, the control inputs $\delta^a$ and $\delta^b$ are used to this end. In this manner, the control input $\delta_{\gamma}$ remains as a degree of freedom for coping with the voltage imbalance problem and with the reduction of the low-frequency ripple.
4. Analysis of the converter dynamics

This section is devoted to analyze the dc-link capacitor voltage difference dynamics (5), with the purpose of studying the phenomenon of the voltage ripple that is present in the neutral point of the dc link. In order to work out this mathematical analysis, an essential assumption related to a singular perturbation approach is first posed [43].

Assumption 1. The instantaneous power dynamics are much faster than the dc-link capacitor voltage difference dynamics.

Concerning this assumption, it leads to suppose in order to study the behavior of (5) that the instantaneous powers have been correctly regulated around their respective references\(^3\)

\[
p \approx p^* \quad (9)
\]

\[
q \approx q^*. \quad (10)
\]

To that end, an appropriate controller that uses the inputs \(\delta_\alpha\) and \(\delta_\beta\) to control the instantaneous powers is assumed to be implemented in the system. Besides, since the previous assumption is related to the instantaneous powers, but the voltage difference dynamics (5) contain the current terms \(i_\alpha\) and \(i_\beta\), the analysis begins expressing these dynamics in terms of power instead of current.

Thereby, according to (9) and (10), the phase currents are approximated, considering (7) as well as (8), by

\[
i_\alpha \approx \frac{1}{|v_{\alpha\beta}|^2} (v_\alpha p^* - v_\beta q^*) \quad (11)
\]

\[
i_\beta \approx \frac{1}{|v_{\alpha\beta}|^2} (v_\beta p^* + v_\alpha q^*), \quad (12)
\]

defining in this manner a change of variables. It is important to mention that the phase voltages in \(\alpha\beta\) coordinates can be expressed as

\[
v_\alpha = |v_{\alpha\beta}| \cos (2\pi f t + \theta) \quad (13)
\]

\[
v_\beta = |v_{\alpha\beta}| \sin (2\pi f t + \theta), \quad (14)
\]

where \(f\) and \(|v_{\alpha\beta}|\) are, respectively, the frequency and amplitude of these variables. Parameter \(\theta\) is the phase.

In the same way, concerning inputs \(\delta_\alpha\) and \(\delta_\beta\), their expressions are obtained introducing (11) and (12) in the phase current dynamics, that is, in (3) and (4), and assuming that the capacitor voltage imbalance is small, i.e., \(v_d = 0\). Note that (5) also depends on these control inputs, which regulate the instantaneous powers of the system. Consequently, control inputs \(\delta_\alpha\) and \(\delta_\beta\) can be described by

\[
\delta_\alpha \approx \lambda_1 v_\alpha - \lambda_2 v_\beta \quad (15)
\]

\[
\delta_\beta \approx \lambda_1 v_\beta + \lambda_2 v_\alpha \quad (16)
\]

where \(\lambda_1\) and \(\lambda_2\) are the constant parameters defined by

\[
\lambda_1 = \frac{2}{V_{dc}} \left(1 - \frac{2\pi f L q^*}{|v_{\alpha\beta}|^2}\right) \quad (17)
\]

\[
\lambda_2 = \frac{4\pi f L p^*}{V_{dc}|v_{\alpha\beta}|^2} \quad (18)
\]

Both parameters \(\lambda_1\) and \(\lambda_2\) are included in the expressions (15) and (16) for simplifying the notation used.

Finally, moving on to the dynamics under analysis, introducing (11)-(16) in (5), and considering some trigonometric identities and the constants \(\mu_1\) and \(\mu_2\) defined by

\[
\mu_1 = \frac{|v_{\alpha\beta}|}{\sqrt{6}} (\lambda_1^2 + \lambda_2^2) \sqrt{p^* + q^2} \quad (19)
\]

\[
\mu_2 = -\frac{(\lambda_1^2 - \lambda_2^2) p^* + 2 \lambda_1 \lambda_2 q^*}{(\lambda_1^2 - \lambda_2^2) q^* + 2 \lambda_1 \lambda_2 p^*}, \quad (20)
\]

the reduced expression defined as follows

\[
C \frac{dv_d}{dt} = -\frac{4 p^*}{\sqrt{3} V_{dc}} \delta_\gamma + \mu_1 \sin (3 \cdot 2\pi f t + 3\theta + \arctan (\mu_2)), \quad (21)
\]

is derived. This result is the final expression of the analysis carried out, and it represents an approximated model of (5). In addition, notice that (21) corresponds to the dynamics that describe the internal behavior of the system when control inputs \(\delta_\alpha\) and \(\delta_\beta\) are chosen to guarantee (9) and (10). Consequently, the approximated model is related to the zero dynamics of the system [44].

4.1. Conclusions and problem statement

The final expression (21) obtained is a general result valid for any operating point of the system, i.e., for any desired value of the instantaneous power references. Furthermore, it shows that, under the assumption of a singular perturbation approach, the highly nonlinear dynamics of the dc-link capacitor voltage difference defined by (5) can be noticeably simplified. The analysis yields a linear differential equation that depends on control input \(\delta_\gamma\) and that also contains a sinusoidal function of time whose frequency is three times the frequency of the grid.

This sinusoidal function represents, in the approximated model derived from the analysis, the low-frequency voltage ripple that is present in the neutral point of the dc link and that affects the balance of the dc-link capacitor voltages. Therefore, since this sinusoidal disturbance appears explicitly in (21), it leads to rewrite this final expression as

\[
C \frac{dv_d}{dt} = -k_d \delta_\gamma + \phi(t). \quad (22)
\]

Parameter \(k_d\) is the following constant

\[
k_d = \frac{4 p^*}{\sqrt{3} V_{dc}}, \quad (23)
\]

and \(\phi(t)\) is the sinusoidal disturbance defined as

\[
\phi(t) = \mu_1 \sin (3 \cdot 2\pi f t + 3\theta + \arctan (\mu_2)). \quad (24)
\]

\(^3\)In [39], a mathematical analysis of converter model is formulated for the particular case when \(q^*\) is set to zero to guarantee a power factor close to the unity. Nevertheless, the analysis carried out in the present paper is completely general, that is, it is valid for any converter operating point.
Notice that (22) takes the form of the formulation of a problem of regulating the output of a system in presence of disturbances [22, 23], for the linear case. In this way, to achieve the control objectives in order to satisfactory cope with the problems associated with the dc-link capacitor voltages, control theory can be applied to design the controller. This result, which is a key point of the paper, provides a new approach to cope with the problems addressed in this work.

**Remark 2.** An important observation is that the classical concept of output regulation means that, for all possible initial conditions of the closed-loop state variables, the error between the system output and the tracking reference tend to zero as time tends to infinity. However, in this paper, it is not aimed for $v_d(t) \to 0$ as $t \to \infty$. The requirements are related to the practical stability of the difference between the capacitor voltages. Consequently, the control goals are related to a problem of practical output regulation [45].

### 5. Design of the controller

The design of the controller to meet the control requirements is based on the approximated model derived from the analysis of the converter dynamics. Considering (22), the control algorithm proposed adopts a disturbance rejection approach. In this way, the sinusoidal disturbance of the approximated model is estimated by a state space observer, and this estimate is then applied to asymptotically reject the disturbance. Besides, a proportional-integral (PI) controller is implemented in parallel to ensure the regulation of the capacitor voltages.

#### 5.1. Estimation of the sinusoidal disturbance

In order to estimate $\phi(t)$, i.e., the sinusoidal disturbance present in (22), the first step is to express that equation as the augmented linear system $S$ described by

$$
S : \begin{cases}
\dot{x}_d = \frac{1}{\tau} x_{\phi 1} - \frac{1}{\tau} u \\
\dot{x}_{\phi 1} = x_{\phi 2} \\
\dot{x}_{\phi 2} = -(3 \cdot 2\pi f)^2 x_{\phi 1}.
\end{cases}
$$

(25)

The capacitor voltage difference $v_d$ is represented by $x_d$, while variables $x_{\phi 1}$ and $x_{\phi 2}$ are the sinusoidal disturbance $\phi(t)$ and its derivative over time, respectively. The system input $u$ represents the control input $\delta_v$. In this manner, system $S$ describes the dynamics of (22), exploiting the knowledge and properties of the disturbance, particularly, the fact that its frequency, which is three times the frequency of the grid, is known.

Considering that the output of the system is the variable $x_d$, the state space representation of system $S$ is

$$
S : \begin{cases}
\dot{x} = Ax + Bu \\
y = Cx,
\end{cases}
$$

(26)

where $x \in \mathbb{R}^3$ is the system state vector defined by

$$
x = \begin{bmatrix} x_d & x_{\phi 1} & x_{\phi 2} \end{bmatrix}^T.
$$

(27)

Since the observability matrix of (26) is full rank, system $S$ is observable. Thus, it is possible to use the system input and output to construct an estimate of the state vector. In this way, the second step is the design of a state space observer to estimate the sinusoidal disturbance. Specifically, a Luenberger observer, denoted by $S_o$, is considered in this paper, assuming that the dc-link capacitor voltage difference is measurable. It is defined by the equations

$$
S_o : \begin{cases}
\dot{\hat{x}} = A\hat{x} + Bu + L(y - \hat{y}) \\
\hat{y} = C\hat{x},
\end{cases}
$$

(29)

where $\hat{x} \in \mathbb{R}^3$ is the estimated state vector described by

$$
\hat{x} = \begin{bmatrix} \hat{x}_d & \hat{x}_{\phi 1} & \hat{x}_{\phi 2} \end{bmatrix}^T,
$$

(30)

the estimated output is $\hat{y} \in \mathbb{R}$, and the observer gain matrix, with dimension $3 \times 1$, is represented by $L$. The rest of variables and parameters have been already defined in (26). Consequently, the estimate of the disturbance $\phi(t)$ corresponds to the variable $\hat{x}_{\phi 1}$ of the observer state vector.

The motivation for considering a Luenberger observer is the simplicity in the design and implementation of this state space observer, compared with other possible disturbance estimation approaches. Once the sinusoidal disturbance (24) is expressed as an harmonic oscillator defining system $S$, this augmented linear system is observable and the application of the observer is direct, only requiring an appropriate selection of the values of the elements of the observer gain matrix $L$. Notice that these elements should be chosen in such a way that the observation error dynamics are faster than the dynamics of system $S$.

#### 5.2. Control Law

Finally, considering the disturbance estimate provided by the observer, the proposed controller applies this estimated state variable to asymptotically cancel the sinusoidal disturbance that appears in (22). The control law is defined as follows

$$
\delta_y = -\frac{1}{k_d} \left( k \int_{t_0}^t (v_{d*} - v_d) d\tau + k_i \int_{t_0}^t (v_{d*} - v_d) d\tau - \hat{x}_{\phi 1} \right).
$$

(31)

In this way, the controller also includes a PI-type control action, where $k$ is the proportional gain and $k_i$ is the integral gain. Both gains are customary tuning parameters. Note that $k_d$ is the constant defined previously in (23), and $v_{d*}$ is the dc-link capacitor voltage difference reference, which is set to zero.

Figure 2 depicts a schematic block diagram of the system, taking into account the final expression (22) of the dc-link capacitor voltage difference dynamics, when both the controller...
and the state observer are implemented. The matrix $H \in \mathbb{R}^{1 \times 3}$ defined by
\[
H = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix},
\]
is introduced to select the estimate of the disturbance, that is, the state variable $\hat{x}_d$, of the observer.

6. Simulation results

This section is devoted to demonstrate the effectiveness of the proposed controller, which is designed with the goal of practically stabilizing the voltage difference between the dc-link capacitors, while attenuating the sinusoidal disturbance present in the neutral point of the dc link as well. For this purpose, the inverter configuration of the three-level NPC converter shown in Fig. 1 together with the proposed voltage balance controller have been implemented and executed under PSCAD environment. The modulation strategy introduced to generate the gating signals of the converter is the space vector modulation presented in [46]. The values of the system parameters considered in the simulation are summarized in Table 2.

It is worth stressing that the system requires other controller to regulate the instantaneous powers, as stated in Section 3. In view of this, the proportional-type direct power control strategy proposed in [47] is adopted, and it is also implemented and executed in PSCAD. The design parameters of this controller together with those of the proposed voltage balance controller are illustrated in Table 3. These parameters are selected in such a way that the assumption of different time scales mentioned in Section 4 is well grounded.

Besides, it should be mentioned that the values of the components of the gain matrix $L$ of the state observer (29) are chosen such that the poles of the observer are faster than the poles of the system (26). System 5 has three poles: a pair of complex conjugate poles $s_{1,2} = \pm 3 \cdot 2\pi f j$, which are pure imaginary poles, and a real pole placed at the origin, $s_3 = 0$. Because the value of the grid frequency is 50 Hz, and the simulation has been carried out with a sampling frequency of 5.6 kHz, the poles of the observer have been placed in $s^n_{1,2,3} = -9 \cdot 2\pi f$. Thus, these poles are much faster than the poles of the system, but they are slow enough to be well suited for the sampling period.

Figure 3 illustrates the behavior of the variable $v_d$, that is, the time evolution of the voltage difference between the dc-link capacitors. In this way, variable $v_d$ is kept close to zero at all times, guaranteeing a solid voltage balancing. In addition, concerning the second of the control objectives described in Section 3, that is, the attenuation of the voltage ripple at three times the fundamental frequency of the grid voltage, notice that applying the proposed controller there is no frequency content at the frequency of the disturbance, i.e., at 150 Hz, as can be seen in Fig. 4. Hence, the second control objective is also achieved.

7. Experimental verification

In order to validate the simulation results obtained before, some experiments have been worked out. To that end, the 50 kVA laboratory prototype of the three-level NPC converter shown in Fig. 5 has been used as inverter, connecting the ac
Figure 4: Single-sided amplitude frequency spectrum of the dc-link capacitor voltage difference.

Figure 5: Laboratory prototype: 50 kVA three-phase three-level NPC converter.

The experiments are focused on the analysis of the steady-state response of the system. In particular, the behavior of the dc-link capacitor voltage difference is studied, comparing the experimental results obtained when two different control algorithms are applied. The first one is the control method proposed in this paper, which is based on a disturbance rejection approach and is developed in Section 5. The second one implements the conventional PI controller defined by

$$\delta_y = -\frac{1}{k_d}[k_i \int (v_d^* - v_d) \, dt + k_f (v_d^* - v_d)]$$.

Consequently, this PI controller, which is also applied with the purpose of achieving the capacitor voltage balancing, does not include any estimate of the sinusoidal disturbance \(v_d\). Besides, identical tuning parameters \(k_i\) and \(k_f\) have been used for both controllers. They are illustrated in Table 3, together with the parameters of the instantaneous power controller also implemented in the system.

Figure 6 depicts the evolution of variable \(v_d\). The two voltage balance controllers considered show solid performance concerning the requirement of practical stability of the system, because the voltage difference is kept close to zero. The results obtained are better when the disturbance estimate of the state observer is included in the control law, since \(v_d\) remains around zero presenting lower voltage deviations with respect to the reference \(v_d^*\). These voltage deviations are lower that approximately 10 V, so they represent, in the worst of the situations, 2.5% of the reference of each dc-link capacitor voltage, denoted by \(v_d^*\). Note that, in the three-level NPC converter, there are two capacitors in the dc link, so \(v_d^*\) is defined by the half of the total dc-link voltage, which is in this case \(V_{dc} = 800\) V.

However, the main difference between the application of either the proposed controller or the conventional PI controller is related to the attenuation of the low-frequency ripple present in the dc link, which is the main benefit of the controller proposed in this paper. Figure 7 illustrates the amplitude frequency spectrums of the variable \(v_d\). Considering the controller based on the disturbance rejection approach, there is a very important reduction of the frequency content at the frequency of the disturbance, that is, at 150 Hz. In this way, there is almost an exact disturbance cancelation, as can be seen in Fig. 7(b). In contrast, when the PI controller is implemented, the frequency content at
that particular frequency is much higher, since the controller is not designed to mitigate the effects caused by the disturbance. Essentially, this result is due to the fact that the PI controller does not incorporate in the feedback any specific reduplicated model or approximation of the dynamic structure of the disturbance to reject [33]. Therefore, the proposed control method provides better results, and it is able to deal with the problems associated with the dc-link capacitor voltages of the converter.

Besides, regarding the evolution of $v_{d}$ depicted in Fig. 6(b) and the one that this variable presents in a simulation environment in Fig. 3, note that both show quite similar behaviors. The voltage deviations of $v_{d}$ with respect to its reference are some volts higher in Fig. 6(b), but this is a typical situation when comparing real and practical cases with idealised ones. Additionally, the mitigation of the dc-link voltage ripple is achieved in the experimental test as well as in the simulation. Hence, the experimental results obtained serve to validate the proposed control method but also to corroborate the mathematical analysis carried out previously in Section 4, supporting in this way the approximated model (22) valid for any converter operating point derived from this analysis.

Finally, Fig. 8 shows the phase currents of the system, when the instantaneous active and reactive power references are set to $p^* = 10$ kW and $q^* = 10$ kVar, respectively. It is worth stressing that the regulation of these variables is carried out indirectly via the adopted direct power control strategy [47]. In addition, it should be mentioned that since no fourth wire is introduced in the NPC system addressed in this paper, the effects of the low-frequency voltage ripple present in the dc link, with or without compensation, are not significant in the phase current behavior.

8. Conclusions

This paper has coped with several problems associated with the dc-link capacitor voltages of the three-level NPC converter. Specifically, it has coped with the imbalance problem of the capacitor voltages and with the problem of the presence of a low-frequency voltage ripple in the dc link. Considering a continuous model of the converter, an analysis of the converter dynamics has led to an approximated model that allows treating both problems together using the classical formulation of a problem of regulating the output of a system subject to disturbances. This key result facilitates the design of the proposed controller, which is based on an asymptotic disturbance rejection approach.

Focusing on the experiments carried out, the results obtained have proved the solid performance and usefulness of the proposed controller, which is able to carry out the balancing of the dc-link capacitor voltages, achieving almost an exact disturbance cancelation. It also has been shown that if no specific action is introduced to reduce the dc-link voltage ripple, its damaging effect is not mitigated. Besides, it should be mentioned that the implementation of the controller is not difficult and does not require additional elements, which is a relevant feature, and that the computational time is low.

Acknowledgments

This work has been funded under grants MICINN-FEDER DPI2009-09661 and Junta de Andalucía P07-TIC-02991.

References
