

# EFFECT OF NON-LINEAR SETTling ERROR ON THE HARMONIC DISTORTION OF FULLY-DIFFERENTIAL SWITCHED-CURRENT BANDPASS $\Sigma\Delta$ MODULATORS

José M. de la Rosa, Belén Pérez-Verdú, Fernando Medeiro, Rocío del Río and Angel Rodríguez-Vázquez

Instituto de Microelectrónica de Sevilla, IMSE (CNM-CSIC)  
Edif. CNM-CICA, Avda. Reina Mercedes s/n, 41012 Sevilla, SPAIN  
Phone: +34 95056666, FAX: +34 95056686, E-mail: jrosa@imse.cnm.es

## ABSTRACT

This paper presents a detailed study of the effect of the non-linear settling on the harmonic distortion of BandPass  $\Sigma\Delta$  Modulators (BP- $\Sigma\Delta$ M)s realized using Fully Differential (FD) Switched-current (SI) circuits. Based on the analysis of building blocks, closed-form expressions are derived for the third-order intermodulation distortion of BP- $\Sigma\Delta$ M)s due to defective settling, on the one hand, and to the non-linearities of the sampling process, on the other. Time-domain simulations and measurements taken from a 0.8 $\mu$ m CMOS 4th-order BP- $\Sigma\Delta$ M silicon prototype validate our approach.<sup>(\*)</sup>

## 1. INTRODUCTION

Up to now, the potential of Switched-current (SI) circuits has been barely demonstrated through actual, practical circuits. Thus, in the case of  $\Sigma\Delta$  Modulators ( $\Sigma\Delta$ M)s, performances featured by reported SI silicon prototypes are well below than those of Switched-Capacitor (SC) counterparts, even if the latter are realized in standard technologies without good passive capacitors. Such poorer performances are partly due to the larger influence of SI non-idealities, as well as to the incomplete modeling of their influence. Particularly, for BandPass  $\Sigma\Delta$ M)s (BP- $\Sigma\Delta$ M)s, and due to the necessity to cope with the frequency specifications required for modern digital wireless communication systems [1], harmonic distortion due to non-linear settling becomes one of the dominant limiting factors.

There have been several attempts to model the non-linear transient response of SI memory cells [2][3][4][5][6]. Regarding harmonic distortion, a precise study of the isolated SI memory cell was presented in [5], but its mathematical complexity precludes to extend its usage to circuits containing heavily coupled memory cells, as it happens for  $\Sigma\Delta$ M)s. The simplified model for Fully Differential (FD) memory cells presented in this paper enables hierarchical systematic analysis of SI circuits composed of memory cells, such as integrators and resonators. This analysis provides closed-form expressions for the third-order intermodulation distortion of BP- $\Sigma\Delta$ M)s caused by two non-linearities: the incomplete settling and the sampling process at the modulator front-end. The latter causes large harmonic distortion levels even for a low settling error, as confirmed by measurements from a 0.8 $\mu$ m CMOS 4th-order BP- $\Sigma\Delta$ M [7].

## 2. FD MEMORY CELLS WITH NON-LINEAR SETTling ERROR

Fig.1(a) shows a FD second-generation memory cell. In what follows, it will be assumed that the incomplete settling is the dominant non-ideality. Therefore, the effect of the charge injection error and the finite output conductance, analysed elsewhere [8], will not be considered. Besides, in most practical cases the time constant formed by the drain-source capacitance and the switch-on re-

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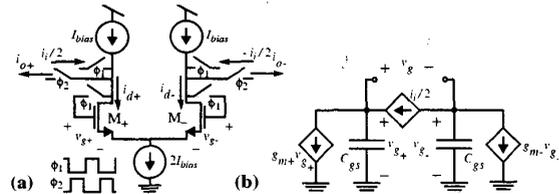


Figure 1. FD memory cell with non-linear settling error. a) Schematic. b) Equivalent circuit during the sampling phase.

istance is much smaller than that due to the gate-source capacitance,  $C_{gs}$ , and the small-signal transconductance,  $g_{mQ}$ . In such a case, the cell can be modelled by the equivalent circuit in Fig.1(b) during the sampling phase,  $\phi_1$ . In this circuit, the large-signal behaviour is modelled by  $g_{m+}$  and  $g_{m-}$ , which represent the transconductances of  $M_{+,-}$ , given by  $g_{m+,-} = g_{mQ}\sqrt{1+m_{i+,-}}$ , where  $m_{i+,-} = i_{i+,-}/I_{bias}$ ,  $i_{i+,-} = \pm i_i/2$ , and  $i_i$  is the input current [3]. Assuming that  $i_i$  keeps stationary during the sampling phase, and that the switch becomes OFF at  $(n-1/2)T_s$  ( $T_s$  is the sampling period) the differential drain current,  $i_d = i_{d+} - i_{d-}$ , can be calculated by solving the circuit in Fig.1(b) for the initial condition  $v_{g+,-} = v_{g+,-,n-1}$ <sup>†</sup>, giving:

$$i_{d,n-1/2} = i_{i,n-1/2}[1 - \Psi(m_{i,n-1/2})] + i_{d,n-1}\Psi(m_{i,n-1/2}) \quad (1)$$

where

$$\Psi(m_{i,n}) = \frac{1}{2} \left( e^{-\frac{T_s}{2\tau}\sqrt{1+m_{i,n}}} + e^{-\frac{T_s}{2\tau}\sqrt{1-m_{i,n}}} \right) \quad (2)$$

with  $\tau = C_{gs}/g_{mQ}$  and  $m_{i,n} = i_{i,n}/(2I_{bias})$ .

At the end of the  $n$ -th hold phase,  $\phi_2$ , the differential output current,  $i_o = i_{o+} - i_{o-}$ , is given by:

$$i_{o,n} = -i_{d,n-1/2} \quad (3)$$

From (1)-(3) and considering  $i_{d,n-1} = i_{d,n-3/2}$ , one obtains:

$$i_{o,n} = -i_{i,n-1/2}[1 - \Psi(m_{i,n-1/2})] + i_{o,n-1}\Psi(m_{i,n-1/2}) \quad (4)$$

To calculate the harmonic distortion, the function  $\Psi(\cdot)$  must be approximated by a polynomial inside a given interval. For that purpose, we have combined Taylor series expansion for  $m_i \ll 1$  and numerical fitting for  $-0.5 \leq m_i \leq 0.5$ ,  $0.01\% < \epsilon_s < 10\%$ , to obtain the following approximation:

$$\Psi(i_{i,n-1/2}) \cong \epsilon_s + \epsilon_{s2} i_{i,n-1/2}^2 \quad (5)$$

where  $\epsilon_s = \exp[-k_s]$  is the linear settling error,  $k_s = T_s/(2\tau)$ ,  $\epsilon_{s2} = \alpha_s \epsilon_s k_s [(1+k_s)/(32I_{bias}^2)]$ , and  $\alpha_s = 3/2$  is a fitting parameter.

<sup>†</sup>1. The notation  $v_{g,n}$  is used to represent  $v_g(nT_s)$ .

Substituting (5) into (4), yields:

$$i_{o,n} \equiv -i_{i,n}^*(1 - \varepsilon_s) + \varepsilon_s i_{o,n-1} \quad (6)$$

where

$$i_{i,n}^* = i_{i,n-1/2} - \varepsilon_s 2(i_{i,n-1/2}^3 + i_{i,n-1/2}^2 i_{o,n-1}) \quad (7)$$

Thus the analysis of a FD memory cell with non-linear settling error can be accomplished considering a memory cell with linear error,  $\varepsilon_s$ , which has an input current equal to (7). If  $i_i$  is a sinewave of amplitude  $I_i$  and frequency  $f_i$ ,  $i_o$  will contain harmonics of  $f_i$ . In FD circuits, the Total Harmonic Distortion (THD) is approximately equal to the third-order harmonic distortion,  $HD_3$ . The analysis of  $HD_3$  can be simplified if  $i_o$  is approximated by its first-order harmonic, such that  $i_{o,n} \equiv -I_o \sin(2\pi f_i n T_s)$ . Performing a Fourier series expansion of (7) it can be shown that the amplitude of the third-order harmonic is approximately given by:

$$A_{3f_i} \equiv \frac{\varepsilon_s 2^3 I_i^3}{2(1 - \varepsilon_s)} \sin\left(\frac{\pi f_i}{f_s}\right) \quad (8)$$

where  $f_s = 1/T_s$  is the sampling frequency, and  $HD_3$  is:

$$HD_3 \equiv \frac{A_{3f_i}}{I_i} \equiv \frac{\alpha_s \varepsilon_s k_s (1 + k_s)}{16(1 - \varepsilon_s)} M_i^2 \sin\left(\frac{\pi f_i}{f_s}\right) \quad (9)$$

with  $M_i = I_i / (2I_{bias})$ .

Fig.2 compares the theoretical model with HSPICE by plotting  $HD_3$  vs.  $f_i/f_s$ , using the same example as in [3] [5] with level-47 MOS models of a  $0.8\mu\text{m}$  standard CMOS technology. In that example,  $g_{mQ} = 82.8\mu\text{A/V}$ ,  $C_{gs} = 22.1\text{pF}$ ,  $I_{bias} = 20\mu\text{A}$ ,  $M_i = 0.5$  and  $f_s = 512\text{kHz}$ . Note that predictions given by (9) agree with HSPICE and with those made by the model in [5]. However, as a difference to this latter model, the new one can also be used for predicting the harmonic distortion of higher-level SI blocks, such as integrators and resonators, and finally, complete BP- $\Sigma\Delta\text{Ms}$ .

### 3. HARMONIC DISTORTION IN SI RESONATORS

Resonators are the basic building blocks of BP- $\Sigma\Delta\text{Ms}$ , playing the same role as integrators in LP- $\Sigma\Delta\text{Ms}$ . Most of BP- $\Sigma\Delta\text{Ms}$  reported in the literature obtain their architecture by applying the transformation  $z^{-1} \rightarrow -z^{-2}$  to the corresponding LP- $\Sigma\Delta\text{Ms}$  [1]. As a consequence of this transformation, the original integrators become resonators with a transfer function  $z^{-a}/(1 + z^{-2})$ , where  $0 < a \leq 2$ . This function can be realized by several filter structures [1]. Fig.3(a) shows the block diagram of one based on LD Integrators (LDI's). This structure is advantageous as compared to the

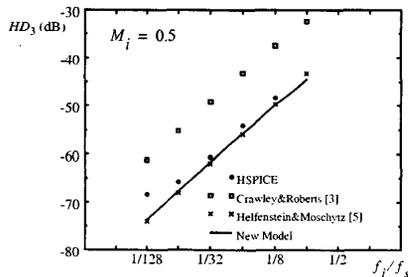


Figure 2. Comparison with HSPICE and previous models.

others because it remains stable under changes in the loop coefficients. Let us consider that the integrators are realized as shown in Fig.3(b) and analyse their isolate operation, assuming that memory cells are described by (4). After clock phase  $\phi_1$ , the differential drain current of cell 2, is:

$$i_{ds_{2,n}} \equiv i_{ds_{2,n}} - i_{ds_{2,n}} \equiv [1 - \Psi(i_{x,n})]i_{x,n} + i_{ds_{2,n-1}} \Psi(i_{x,n}) \quad (10)$$

where  $i_{x,n} = i_{i,n} - i_{ds_{1,n-1/2}}$  and  $i_{ds_{1,n}} \equiv (i_{ds_{1,n}} - i_{ds_{1,n}})$  represents the differential drain current of cell 1. After clock phase  $\phi_2$ ,

$$i_{ds_{1,n+1/2}} \equiv -[1 - \Psi(-i_{ds_{2,n}})]i_{ds_{2,n}} + i_{ds_{1,n-1}} \Psi(-i_{ds_{2,n}}) \quad (11)$$

Assuming that the output stage (represented in Fig.3(b) as a simple current mirror) is ideal, the output current of the integrator is:

$$i_{o,n+1/2} = -i_{ds_{2,n}} \quad (12)$$

From (5) and (10)-(12),

$$i_{o,n} \equiv -(1 - \varepsilon_s)i_{i,n}^* + (1 + \varepsilon_s^2)i_{o,n-1} + \varepsilon_s^2 i_{o,n-2} \quad (13)$$

with

$$i_{i,n}^* \equiv i_{i,n-1/2} - \varepsilon_s i_{i,n-3/2} - \varepsilon_s 2(i_{o,n}^2 i_{i,n-1/2} + i_{o,n-1}^2 i_{i,n-3/2}) \quad (14)$$

Thus, the analysis of a SI FD integrator formed by memory cells with non-linear settling error can be accomplished considering an integrator with linear settling error whose input is equal to (14).

Let us consider the resonator of Fig.3(a). Assuming that the integrators can be modelled by (13) and (14), the finite-difference equations that govern the behaviour of the resonator are:

$$i_{1,n} = i_{i,n} - i_{o,n} \quad (15)$$

$$i_{2,n} \equiv -(1 - \varepsilon_s)i_{1,n-1/2} + \varepsilon_s i_{1,n-3/2} + i_{2,n-1} + i_{2H,n} \quad (16)$$

$$i_{o,n} \equiv -(1 - \varepsilon_s)i_{2,n-1/2} + \varepsilon_s i_{2,n-3/2} + i_{o,n-1} + i_{oH,n} \quad (17)$$

where  $i_1$  and  $i_2$  are respectively the input and the output of the first integrator in the loop and  $i_{2H}$  and  $i_{oH}$  are non-linear terms, respectively given by:

$$i_{2H,n} \equiv \varepsilon_s 2(i_{2,n}^2 i_{1,n-1/2} + i_{2,n-1}^2 i_{1,n-3/2}) \quad (18)$$

$$i_{oH,n} \equiv \varepsilon_s 2(i_{o,n}^2 i_{2,n-1/2} + i_{o,n-1}^2 i_{2,n-3/2}) \quad (19)$$

Assuming that  $\varepsilon_s^2 \varepsilon_s 2|i_{1,2,0}|^2 \ll 1$ , solving for  $i_{2,n}$  in (17) and substituting it in (16), obtains:

$$i_{o,n} \equiv (1 - 2\varepsilon_s)i_{i,n}^* + 4\varepsilon_s i_{o,n-1} - (1 - 4\varepsilon_s)i_{o,n-2} \quad (20)$$

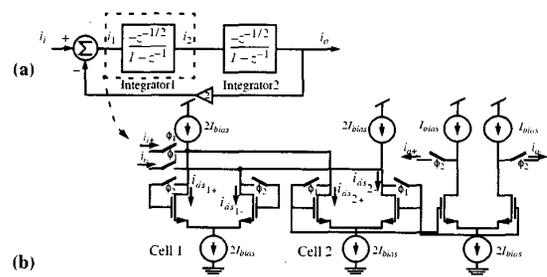
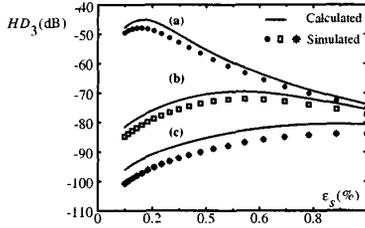


Figure 3. LDI-loop Resonator. a) Block diagram. b) SI FD LDI.



**Figure 4.**  $HD_3$  at the output of a LDI-loop resonator, with  $f_i'$ : a)  $0.001f_s/4$ . b)  $0.002f_s/4$ . c)  $0.003f_s/4$ .

where  $i'_{i,n} \equiv i_{i,n-1} + (i_{oH,n} - i_{oH,n-1} - i_{2H,n-1/2})$ .

The harmonic distortion referred to the resonator input can be calculated by analysing the harmonic content of the above expression. Therefore, assuming that  $i_i$  is a sinewave of amplitude  $I_i$  and frequency  $f_i$ , the output of the resonator will be a quasi-sinusoidal signal, with an amplitude approximately given by:

$$I_o \equiv I_i \left| \frac{(1 - 2\epsilon_s)z^{-1}}{1 - 4\epsilon_s z^{-1} + (1 - 4\epsilon_s)z^{-2}} \right|_{z=e^{j2\pi f_i T_s}} \quad (21)$$

Performing a Fourier series expansion of  $i'_{i,n}$ , it can be shown that the amplitude of the third-order harmonic at the resonator input is given by:

$$A_{H,3} = |i_{3f_i,n}| \equiv \frac{\sqrt{2}}{2} \epsilon_s I_o^3 (1 + 5\pi f_i' T_s) \quad (22)$$

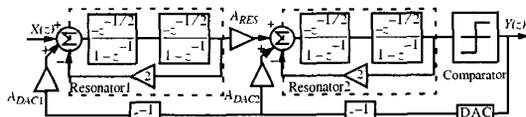
where,  $f_i' = f_i - f_s/4$  and  $f_i' T_s \ll 1$  has been assumed.

Multiplying  $A_{H,3}$  by the resonator gain (evaluated at  $3f_i$ ) and dividing the result by  $I_o$ , obtains  $HD_3$  at the resonator output. This analysis has been validated by time-domain simulation using the behavioural simulator for SI circuits reported in [9]. Fig.4 shows  $HD_3$  at the output of the resonator as a function of  $\epsilon_s$ , for different values of  $f_i'$ . This simulation was done by changing  $g_{mQ}$ , for  $C_{gs} = 1\text{pF}$ ,  $I_i = 0.5\mu\text{A}$  and  $I_{bias} = 200\mu\text{A}$ , when clocked at  $f_s = 10\text{MHz}$ . Note that  $HD_3$  does not increase with  $\epsilon_s$  because the open loop gain of the resonator is also attenuated by the linear error. Although simulated behaviour is well predicted by theory, their differences become larger when the condition  $f_i' T_s \ll 1$  is not satisfied as assumed in theory.

#### 4. HARMONIC DISTORTION IN SI BANDPASS $\Sigma\Delta$ MODULATORS

Let us consider the 4th-order BP- $\Sigma\Delta$ M shown in Fig.5, where  $A_{DAC2} = 2A_{DAC1}A_{RES}$ , and assume that LDI's are realized as in Fig.3(b). For the analysis of the harmonic distortion, the following considerations have been taken into account:

- The harmonic distortion referred to the modulator input is equal to the harmonic distortion referred to the modulator output because the signal transfer function is unity in the signal band.



**Figure 5.** Block diagram of the 4th-order BP- $\Sigma\Delta$ M.

- The contribution of the second resonator will not be considered because it is attenuated by the gain of the first resonator in the signal band.

- The quantization error, modelled as an additive white noise source, does not contribute to the harmonic distortion.

The analysis of the modulator in Fig.5 reveals that the amplitude of the first resonator output is given by:

$$I_o = A_x \left| \frac{1 + A_{DAC1}z^{-4}}{1 + z^{-2}} \right|_{z=e^{j2\pi f_i T_s}} \quad (23)$$

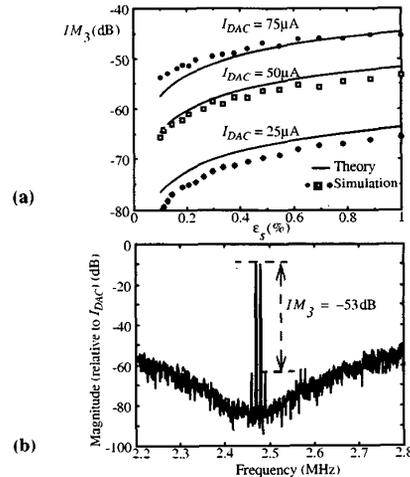
where  $A_x$  is the input amplitude. Substituting (23) into (22), assuming that  $A_{DAC1} = -1$  and dividing by  $A_x$ , obtains that  $HD_3$  at the output of the modulator is:

$$HD_3 \equiv 4\sqrt{2}\epsilon_s A_x^2 (1 + 5\pi f_i' T_s) \equiv 4\sqrt{2}\epsilon_s A_x^2 \quad (24)$$

Note that due to the oversampling, it is  $f_i' T_s \ll 1$ , and hence  $HD_3$  practically does not depend on  $f_i$ . A more appropriate parameter for characterizing the harmonic distortion in BP- $\Sigma\Delta$ Ms is the third-order intermodulation distortion, given by:

$$IM_3 \equiv 12\sqrt{2}\epsilon_s A_x^2 = 3\sqrt{2} \frac{\alpha_s \epsilon_s k_s (1 + k_s)}{8n_b^2} \left( \frac{A_x}{I_{DAC}} \right)^2 \quad (25)$$

where  $I_{DAC}$  is the DAC output current and  $n_b = I_{bias}/I_{DAC}$ . This expression has been validated by time-domain simulation as shown in Fig.6(a) by representing  $IM_3$  vs.  $\epsilon_s^{\dagger 2}$  for different values of  $I_{DAC}$  with  $A_x = I_{DAC}/2$ ,  $I_{bias} = 200\mu\text{A}$ ,  $C_{gs} = 1\text{pF}$  and  $f_s = 10\text{MHz}$ . The input signal consisted on two tones of amplitude  $A_x/\sqrt{2}$  and frequencies  $f_{i1} \equiv 0.247f_s$  and  $f_{i2} = 0.248f_s$ . As an illustration, Fig.6(b) shows the output spectrum corresponding to  $\epsilon_s = 1\%$  and  $I_{DAC} = 50\mu\text{A}$ . Note that, other intermodulation products appears – not critical since they are outside the signal band.



**Figure 6.** a)  $IM_3$  vs.  $\epsilon_s$  for different values of  $I_{DAC}$ . b) Output spectrum for  $\epsilon_s = 1\%$  and  $I_{DAC} = 50\mu\text{A}$ .

$\dagger 2$ . The simulation was carried out by varying  $g_{mQ}$  such that  $0.1\% < \epsilon_s < 1\%$ .

## 5. EFFECT OF S/H PROCESS AT THE FRONT-END OF SI BANDPASS $\Sigma\Delta$ MODULATORS

In the previous analysis it has been assumed that the input current is constant during the sampling phase. However this assumption does not apply to the memory cell connected at the input node of a BP- $\Sigma\Delta$ M. In this case, the ratio between  $f_i$  and  $f_s$  is close to unity ( $f_i/f_s = 1/4$  in the case of the modulator in Fig.5) and hence, there will be large variations of the input current during the sampling phase. As a consequence, additional harmonic distortion will appear even if  $\epsilon_s \ll 1$ , which can not be explained by (9).

The harmonic distortion in memory cells connected to continuous-time sinuswave currents was analysed in [6]. Here, we will extend that analysis to BP- $\Sigma\Delta$ Ms. Let us consider first the cell in Fig.1(a) and assume a sinuswave input current of frequency  $f_i$  and amplitude  $I_i$ . In this case,  $i_d$  can not be solved as an step-response. In order to find an explicit solution, the circuit in Fig.1(b) was solved for  $g_{m+} = g_{mQ}$ , with the initial condition  $v_{g+} = v_{g+,n-1}$ . Once the solution was found,  $g_{mQ}$  was replaced by  $g_{mQ}\sqrt{1+m_{i,n}}$ , yielding to <sup>†3</sup>:

$$i_{o,n} \cong -i_{i,n-1/2}\Phi_{n-1/2}(i_{i,n-1/2}) + [i_{i,n-1}\Phi_{n-1}(i_{i,n-1/2})\Psi(i_{i,n-1/2}) + i_{o,n-1}\Psi(i_{i,n-1/2})] \quad (26)$$

being,

$$\Phi_n(i_i) \cong \frac{1 - 2\pi f_i \tau \cot(2\pi f_i n T_s) - 6\pi f_i \tau \cot(2\pi f_i n T_s)}{1 + (2\pi f_i \tau)^2} - \frac{6\pi f_i \tau \cot(2\pi f_i n T_s)}{32I_{bias}^2} I_i^2 \quad (27)$$

where  $i_i/I_{bias} \ll 1$  has been assumed. Following the same procedure as in Section 2, it can be shown that, for  $\pi f_i \tau \ll 1$ ,

$$A_{H,3} \cong \frac{3\pi f_i \tau}{16(2I_{bias})^3} I_i^3 \quad (28)$$

In BP- $\Sigma\Delta$ Ms, only the first memory cell connected to the input signal will contain the above harmonic. To calculate  $IM_3$  at the output of the modulator, it is necessary to express  $I_i$  as a function of  $A_x$ . The analysis of Fig.5 gives  $I_i \cong 2\sqrt{2}A_x$ . Substituting this expression in (28), and dividing by  $A_x$  it can be shown that:

$$IM_3 \cong \frac{9}{8\sqrt{2}n_b} \pi f_s \tau \left(\frac{A_x}{I_{DAC}}\right)^2 \quad (29)$$

where  $f_i \cong f_s/4$  has been assumed. Fig.7(a) compares (29) with time-domain behavioural simulation by plotting  $IM_3$  vs.  $\tau$  for

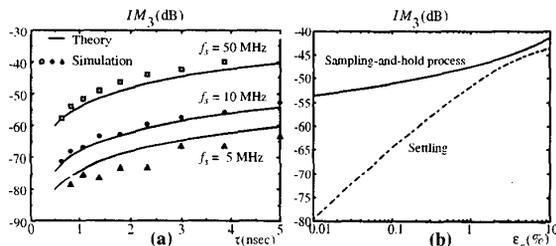


Figure 7.  $IM_3$  due to the S/H process at the front-end. a)  $IM_3$  vs.  $\tau$ . b) Comparison with  $IM_3$  due to non-linear  $\epsilon_s$ .

<sup>†3</sup>. A more rigorous analysis can be done by using the Volterra series method as we demonstrated in [8], yielding to similar results.

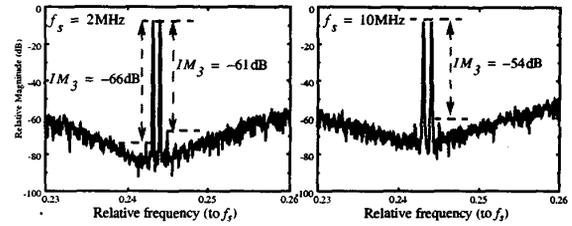


Figure 8. Measured output spectra for different values of  $f_s$ .

different values of  $f_s$ ,  $n_b = 4$  and  $A_x/I_{DAC} = 1/2$ . The theoretical model accurately predicts the simulation results except for some cases where a maximum error of 4dB occurs. In these cases a more exact analysis using the Volterra series method should be used.

To conclude this study, Fig.7(b) compares  $IM_3$  caused by the non-linear settling error and the S/H process for  $f_s = 10$  MHz and  $A_x/I_{DAC} = 1/2$ . Note that, for  $\epsilon_s > 3\%$ , both expressions approximately converge. However, for practical designs, i.e. for  $\epsilon_s < 0.1\%$ ,  $IM_3$  due to the S/H process dominates, limiting the performance of SI BP- $\Sigma\Delta$ Ms unless a S/H circuit will be used at the front-end. This fact has been confirmed by experimental results from a  $0.8\mu\text{m}$  CMOS 4th-order BP- $\Sigma\Delta$ M [7]. Fig.8 shows two measured output spectra for  $A_x/I_{DAC} = 0.42$  when clocked at  $f_s = 2$  MHz and  $f_s = 10$  MHz, obtaining  $IM_3 = -61$  dB and  $-54$  dB respectively. In this case,  $g_{mQ} = 360\mu\text{A/V}$  and  $C_{gs} = 2.8$  pF ( $\epsilon_s = 0.16\%$  at  $f_s = 10$  MHz), which according to (29) gives  $IM_3 = -64$  dB and  $IM_3 = -55$  dB respectively.

## 6. CONCLUSIONS

The effect of non-linear dynamic SI errors on the harmonic distortion of FD BP- $\Sigma\Delta$ Ms has been analysed in detail. Closed-form expressions, validated through time-domain simulation, have been derived for  $IM_3$  due to the non-linear settling and the sampling process. The latter constitutes the main source of harmonic distortion in practical designs as demonstrated by experimental results.

## REFERENCES

- [1] S.R. Norsworthy, R. Schreier, G.C. Temes: "Delta-Sigma Converters. Theory, Design and Simulation", New York, IEEE Press, 1997.
- [2] D.B. Naim: "Analytic Response of MOS Current Copiers", *IEEE Transactions on Circuits and Systems II*, pp. 133-135, February 1993.
- [3] P.J. Crawley and G.W. Roberts: "Predicting Harmonic Distortion in Switched-Current Memory Circuits", *IEEE trans. Circuits and Systems II*, pp. 73-86, February 1994.
- [4] N.Moeneclaey and A. Kaiser: "Accurate Modelling of the Non-Linear Settling Behaviour of Current Memory Circuits", *Proc. 1994 IEEE Int. Symp. Circuits and Systems (ISCAS)*, pp. 339-342.
- [5] M.Helfenstein and G. Moschytz: "Distortion Analysis of Switched-Current Circuits", *Proc. 1998 IEEE Int. Symp. Circuits and Systems (ISCAS)*, pp. 29-32.
- [6] J.M. Martins and V.F. Dias: "Harmonic Distortion in SI Cells: Settling and Clock Fall-Time Effects", *Proc. of 1998 Design of Integrated Circuits and Systems Conference (DCIS)*, pp. 292-297.
- [7] J.M. de la Rosa, B. Pérez-Verdú, R. del Río and A. Rodríguez-Vázquez: "A CMOS  $0.8\mu\text{m}$  Transistor-Only 1.63MHz Switched-Current Bandpass  $\Sigma\Delta$  Modulator for AM Signal A/D Conversion", *IEEE Journal of Solid-State Circuits*, pp. 1220-1226, August 2000.
- [8] J.M. de la Rosa: "Modelling and Design of Switched-Current Bandpass  $\Sigma\Delta$  Modulators for Digital Communication Systems", Ph.D. Dissertation, Univ. of Seville, December 2000.
- [9] J.M. de la Rosa, A. Kaiser and B. Pérez-Verdú: "Interactive Verification of Switched-Current Sigma-Delta Modulators", *Proc. of 1998 IEEE International Conference on Electronics, Circuits and Systems (ICECS)*, pp. 2.157-2.160.