

Dear Author,

Here are the proofs of your article.

- You can submit your corrections **online**, via **e-mail** or by **fax**.
- For **online** submission please insert your corrections in the online correction form. Always indicate the line number to which the correction refers.
- You can also insert your corrections in the proof PDF and **email** the annotated PDF.
- For fax submission, please ensure that your corrections are clearly legible. Use a fine black pen and write the correction in the margin, not too close to the edge of the page.
- Remember to note the **journal title**, **article number**, and **your name** when sending your response via e-mail or fax.
- **Check** the metadata sheet to make sure that the header information, especially author names and the corresponding affiliations are correctly shown.
- **Check** the questions that may have arisen during copy editing and insert your answers/ corrections.
- **Check** that the text is complete and that all figures, tables and their legends are included. Also check the accuracy of special characters, equations, and electronic supplementary material if applicable. If necessary refer to the *Edited manuscript*.
- The publication of inaccurate data such as dosages and units can have serious consequences. Please take particular care that all such details are correct.
- Please **do not** make changes that involve only matters of style. We have generally introduced forms that follow the journal's style. Substantial changes in content, e.g., new results, corrected values, title and authorship are not allowed without the approval of the responsible editor. In such a case, please contact the Editorial Office and return his/her consent together with the proof.
- If we do not receive your corrections **within 48 hours**, we will send you a reminder.
- Your article will be published **Online First** approximately one week after receipt of your corrected proofs. This is the **official first publication** citable with the DOI. **Further changes are, therefore, not possible.**
- The **printed version** will follow in a forthcoming issue.

#### **Please note**

After online publication, subscribers (personal/institutional) to this journal will have access to the complete article via the DOI using the URL: [http://dx.doi.org/\[DOI\]](http://dx.doi.org/[DOI]).

If you would like to know when your article has been published online, take advantage of our free alert service. For registration and further information go to: <http://www.link.springer.com>.

Due to the electronic nature of the procedure, the manuscript and the original figures will only be returned to you on special request. When you return your corrections, please inform us if you would like to have these documents returned.

# Metadata of the article that will be visualized in OnlineFirst

---

**Please note: Images will appear in color online but will be printed in black and white.**

---

ArticleTitle                      How did the Sovereign debt crisis affect the Euro financial integration? A fractional cointegration approach

---

Article Sub-Title

---

Article CopyRight                Springer Science+Business Media, LLC  
(This will be the copyright line in the final PDF)

---

Journal Name                      Empirica

---

Corresponding Author          Family Name                      **Golpe**  
Particle  
Given Name                        **Antonio A.**  
Suffix  
Division                            Department of Economics  
Organization                      University of Huelva  
Address                            Plaza de la Merced, 11, 21002, Huelva, Spain  
Phone                                +34 959 217 911  
Fax  
Email                                antonio.golpe@dehie.uhu.es  
URL  
ORCID                                <http://orcid.org/0000-0003-0360-1541>

---

Author                              Family Name                      **Vides**  
Particle  
Given Name                        **José Carlos**  
Suffix  
Division                            Department of Economics  
Organization                      University of Huelva  
Address                            Plaza de la Merced, 11, 21002, Huelva, Spain  
Phone                                +34 959 217 832  
Fax  
Email                                joseca.vides@gmail.com  
URL  
ORCID

---

Author                              Family Name                      **Iglesias**  
Particle  
Given Name                        **Jesús**  
Suffix  
Division                            Department of Financial Economics and Operations Management  
Organization                      University of Seville  
Address                            Avda. Ramón y Cajal 1, 41019, Seville, Spain  
Phone                                +34 959 217 832  
Fax

Email [jglesias10@us.es](mailto:jglesias10@us.es)  
URL  
ORCID

---

Schedule  
Received  
Revised  
Accepted

---

Abstract This paper examines financial integration among stock markets in the Eurozone using the prices from each stock index. Monthly time series are constructed for four major stock indices for the period between 1998 and 2016. A fractional cointegrated vector autoregressive model is estimated at an international level. Our results show that there is a perfect and complete Euro financial integration. Considering the possible existence of structural breaks, this paper also examines the fractional cointegration within each regime, showing that Euro financial integration is very robust. However, in the financial and sovereign debt crisis regime, IBEX 35 appears to be the weak link in Euro financial integration, unless Euro financial integration recovers when this period ends.

---

Keywords (separated by '-') Fractional cointegration - Eurozone - Financial integration - Financial market cointegration

---


JEL Classification (separated by '-') C32 - F41 - G15

---

Footnote Information

---

2  
3 **How did the Sovereign debt crisis affect the Euro**  
4 **financial integration? A fractional cointegration**  
5 **approach**

6 José Carlos Vides<sup>1</sup> · Antonio A. Golpe<sup>1</sup>  ·  
7 Jesús Iglesias<sup>2</sup>

8  
9 © Springer Science+Business Media, LLC 2017

10 **Abstract** This paper examines financial integration among stock markets in the  
11 Eurozone using the prices from each stock index. Monthly time series are con-  
12 structed for four major stock indices for the period between 1998 and 2016. A  
13 fractional cointegrated vector autoregressive model is estimated at an international  
14 **AQ1** level. Our results show that there is a perfect and complete Euro financial inte-  
15 gration. Considering the possible existence of structural breaks, this paper also  
16 examines the fractional cointegration within each regime, showing that Euro  
17 financial integration is very robust. However, in the financial and sovereign debt  
18 crisis regime, IBEX 35 appears to be the weak link in Euro financial integration,  
19 **AQ2** unless Euro financial integration recovers when this period ends.

20  
21 **Keywords** Fractional cointegration · Eurozone · Financial integration · Financial  
22 market cointegration

23  
24 **JEL Classification** C32 · F41 · G15

A1 ✉ Antonio A. Golpe  
A2 antonio.golpe@dehie.uhu.es

A3 José Carlos Vides  
A4 joseca.vides@gmail.com

A5 Jesús Iglesias  
A6 jiglesias10@us.es

A7 <sup>1</sup> Department of Economics, University of Huelva, Plaza de la Merced, 11, 21002 Huelva, Spain

A8 <sup>2</sup> Department of Financial Economics and Operations Management, University of Seville,  
A9 Avda. Ramón y Cajal 1, 41019 Seville, Spain

27 **1 Introduction**

28 The convergence of international markets has resulted from multiple confluences of  
 29 economic, technological and political factors that have allowed national and  
 30 international regulations to increasingly align with economic forces and globaliza-  
 31 **AQ3** tion processes. The formation of the Euro was an effort to enhance synergies of  
 32 member countries, creating highly favourable conditions in which capital markets  
 33 could develop important similarities between them (Salgado et al. 2015).

34 Relationships between stock markets have been widely studied from different  
 35 perspectives. Using techniques such as EMH (Kim et al. 2009), CAPM (Heimonen  
 36 2010) and/or GARCH (Illueca and Lafuente 2002), conclusions about relationships,  
 37 convergence or co-movements among markets have been reached. Furthermore,  
 38 several techniques have been used to apply time series data (see Brooks 2014) to  
 39 integration and cointegration among different global economic regions, mainly the  
 40 USA-EU (see Caporale et al. 2015, among others), and intraregional markets, such  
 41 **AQ4** as members of the EMU (Da Fonseca 2013).

42 The aim of this paper is to study financial integration among the four major stock  
 43 markets in the Eurozone (Germany, France, Spain and Italy) for the period of  
 44 January 1998 to September 2016 from an econometric perspective.<sup>1</sup> This paper  
 45 presents a novel approach to the integration of stock markets, filling a gap in the  
 46 literature with regard to time series analysis of market cointegration. In this sense,  
 47 our paper contributes to previous literature on the analysis of the integration of stock  
 48 markets from a fractional cointegration vector autoregressive perspective. Although  
 49 fractional cointegration had been used in previous studies, the approach proposed by  
 50 Johansen (2008a) and Johansen and Nielsen (2012) is novel to the literature. This  
 51 model, which is extended to allow for deterministic trends, has advantages when  
 52 estimating a system of fractional time series variables that are potentially  
 53 cointegrated. Additionally, the flexibility of the model allows one to determine  
 54 the number of equilibrium relations via statistical tests and jointly estimate the  
 55 adjustment coefficients and cointegrating relations while accounting for short-run  
 56 dynamics. We use data with a monthly frequency to estimate the model, then  
 57 perform statistical tests of cointegration, exclusion and weak exogeneity. We then  
 58 apply the Bai and Perron (2003) test for structural breaks and use the FCVAR model  
 59 to examine each break detected.

60 The remainder of the paper is organized as follows. Section 2 provides a review  
 61 of the literature, focusing initially on the techniques used to study stock markets and  
 62 subsequently on the application of the integration and cointegration test in different  
 63 economic regions. Section 3 presents the methodology applied. Section 4 discusses  
 64 the empirical results, and conclusions are presented in Sect. 5.

1FL01 <sup>1</sup> The stock markets studied include the German stock market, the behavior of which is reflected in the  
 1FL02 DAX index; the French stock market, reflected in the CAC 40 index; the Italian stock market, as indicated  
 1FL03 by the FTSE MIB index; and the Spanish stock market, as shown by the IBEX 35 index. The choice of a  
 1FL04 stock market is based on the size of the respective national economy and the capitalization of the stock  
 1FL05 markets, which are the major ones in the Eurozone.

65 **2 Literature review**

66 Some measure of market development is essential in making intertemporal  
 67 comparisons. For this reason, the treatment of such variables can explain the  
 68 relationship between markets in the same economic region or, conversely, whether  
 69 markets in different regions exhibit similar behaviour. As a result of computerized  
 70 trading systems, markets can operate simultaneously. This allows for the study of  
 71 the integration of stock markets, whose interrelations had previously been studied in  
 72 various ways, e.g., using financial techniques such as the Efficient Market  
 73 Hypothesis (EMH) or the Capital Asset Pricing Model (CAPM), until econometric  
 74 models such the unit root test, GARCH and cointegration tests became available.  
 75 The EMH is based on return predictability, as seen in the past price history of a  
 76 market (Fama 1970, 1991), combined with other techniques such as the unit root test  
 77 (Kim et al. 2009) or the variance ratio test<sup>2</sup> (Huang 1995; Smith 2007).

78 In contrast to previous research that has sought to explain intra-market behaviour,  
 79 new research exploring this link has emerged, using other techniques, such as the  
 80 international Capital Asset Pricing Model (CAPM) (Sharpe 1964), which proposes  
 81 that stock market returns are affected by interest rates movements. Thus, for an  
 82 investor in international markets, excess returns are related to changes in exchange  
 83 rates (Heimonen 2010). Moreover, Yang (2012) combined the CAPM and  
 84 cointegration to explain how benchmark markets are integrated with the global  
 85 market. Over the decades, researchers have found the study of integration to be a  
 86 useful approach to the study of the behaviour of inter-markets.<sup>3</sup> To illustrate the  
 87 concept of integration, we note that markets are integrated when investors can pass  
 88 from one market to another at no extra cost and when possibilities for arbitrage  
 89 ensure the equivalence of share prices in both markets (Jawadi and Arouri 2008).  
 90 Early papers, seeking to demonstrate integrated markets, proposed techniques such  
 91 as correlation tests to explain short-run portfolio diversification (Solnik 1974;  
 92 Longin and Solnik 1995).

93 Nevertheless, in reviewing the existing literature, we found that most studies  
 94 examined the integration of world stock markets only in a linear framework, using  
 95 correlation tests as a tool of data analysis. Examples include Hamao et al. (1990)  
 96 and (Markellos and Siriopoulos 1997). Hence, some researchers have confirmed the  
 97 existence of relationships using the GARCH model to explore co-movements<sup>4</sup>  
 98 among stock markets (Illueca and Lafuente (2002); Chouliaras et al. (2012); Da  
 99 Fonseca (2013) and Lee and Mercurelli (2014)), assuming that positive and negative  
 100 error terms have symmetric effects on volatility. In more recent times, some  
 101 researchers have utilized a variance of cointegration technique, specifically,  
 102 fractional cointegration. For example, Caporale et al. (2015) use this technique to

2FL01 <sup>2</sup> Lo and Mackinlay (1988) examined the predictability of time series by comparing the variances of  
 2FL02 differences in the data calculated over different intervals.

3FL01 <sup>3</sup> Henceforth, we consider the relationships denoted by inter-markets to be the relationships among  
 3FL02 markets.

4FL01 <sup>4</sup> Forbes and Rigobon (2002) explained co-movement as contagion, i.e., as a significant increase in cross-  
 4FL02 market linkages after a shock to one country or group of countries.

103 analyse linkages among US and European markets. They indicate that shocks that  
 104 affect long-run relationships vanish at a very slow rate. Gagnon et al. (2016) also  
 105 use this method to study the cointegration of risk-neutral moments of five major  
 106 stock markets in Europe, showing that there is strong financial integration and  
 107 concluding that such integration is partial when anticipations are considered.

## 108 2.1 Empirical cointegration approach for the stock market analysis

109 This section explores the targets of the cointegration analysis that has been applied  
 110 to stock markets. Research into integration and cointegration has employed several  
 111 techniques, such as unit root tests of Dickey and Fuller (1979, 1981), used to  
 112 establish the order of integration. Although in these papers, the authors provide one  
 113 of the most influential works in the field of unit root tests, the test has low power  
 114 because long memory processes cannot be explained by this test (Caporale et al.  
 115 2015). Subsequently, the cointegration of the variables was analysed, using the  
 116 multivariate cointegration test of Johansen (1988, 1991), which enables testing of  
 117 the cross-country market efficiency hypothesis. The Johansen cointegration test is  
 118 used to show common stochastic trends across stock markets, and for this purpose,  
 119 this test affords more robust results than other cointegration tests when there are  
 120 more than two variables (Gonzalo 1994). According to this idea, since the seminal  
 121 paper of Kasa (1992), who studied the financial integration of five developed  
 122 markets, applying common stochastic trends in these series. As a consequence, this  
 123 methodology has led to numerous studies that find long-run co-movements between  
 124 international stock markets, using univariate or multivariate cointegration models—  
 125 for instance, Kenourgios et al. (2009), Yang et al. (2003) and Tian (2007).

126 Stock market analysis has been applied to different regions of the world, but most  
 127 relevant studies have focused on the USA and Europe and their relations. Many  
 128 strands of research, using cointegration tests, have obtained mixed results regarding  
 129 market relationships. One strand focuses on US stock markets; Gil-Alana et al.  
 130 (2013) observed very similar patterns in US stock markets for daily prices during  
 131 the 1971–2007 period. Granger and Hyung (2004) and Mikosch and Starica (2000),  
 132 using different techniques, explained the cointegration through structural breaks,  
 133 showing long memory dependence. Conversely, Alvarez-Ramirez et al. (2008)  
 134 demonstrated a shift in long-term behaviour—that is, a random walk. Additionally,  
 135 empirical studies of relationships among international stock markets have focused  
 136 on the United States. For example, Francis and Leachman (1998) and Richards  
 137 (1995) both examined the existence of cointegration relationships between the  
 138 developed European and U.S. markets. The first demonstrated long-run equilibrium  
 139 among markets, whereas the second showed that national return indices are not  
 140 cointegrated. Caporale et al. (2015) used fractional cointegration to find linkages  
 141 between US and European stock markets, contrasting different recovery paths due to  
 142 monetary policy pursued in the two economies. Studies have also shown relations  
 143 between US or European markets and Asian markets. For example, Wong et al.  
 144 (2004) utilized fractional cointegration, reporting linkages between India, the USA,  
 145 the UK and Japan. While this approach is extensively used in the literature, another  
 146 strand in the literature focuses on stock markets within Europe. Taylor and Tonks

147 (1989) and Corhay, Rad and Urbain (1993) found strong evidence for cointegration  
 148 among several major European stock markets in the late 1970s and 1980s. In an  
 149 international context, Bessler and Yang (2003) sought to demonstrate interdepend-  
 150 ence among nine major stock markets, finding that they are not fully integrated,  
 151 and Darrat and Zhong (2005) studied cointegration between NAFTA countries,  
 152 showing stable long-run linkage between the three stock markets. In addition, Kasa  
 153 (1992) noted a common stochastic trend in the equity index prices of five developed  
 154 countries, while Dickinson (2000) found that a cointegrating relationship between  
 155 the major European stock markets exists and may be partly driven by the long-run  
 156 relationships of macroeconomic fundamentals among these countries, possibly  
 157 through indirect channels of international interaction.

158 Overall, a growing literature is emerging, one that seeks to explain the process of  
 159 market integration due the convergence, using cointegration and taking into account  
 160 endogeneity issues (Chouliaras et al. 2012; Syriopoulos 2007; Bley 2009; Mylonidis  
 161 and Kollias 2010; Lee and Mercurelli 2014) and/or structural breaks (Kim et al.  
 162 2005; Demian 2011; Karmann and Ludwing 2014). However, Da Fonseca (2013),  
 163 using a VAR model, demonstrated that the major stock markets in the Euro area  
 164 were not perfectly integrated during the first decade of the EMU. In sum, this  
 165 technique provides a mode of demonstrating different ways of explaining market  
 166 integration in different contexts. Caporale et al. (2015) recently showed that  
 167 cointegration has also been used to determine whether there are diversification  
 168 benefits from investing in different stock markets.

169 If cointegration does not hold, markets are not linked in the long run, and  
 170 therefore, it is possible to gain from diversification. For this reason, testing for  
 171 cointegration and any changes over time in its degree is important. For example,  
 172 Richards (1995) demonstrated a lack of cointegration among various stock markets  
 173 and hence the existence of diversification benefits for investors. From a theoretical  
 174 perspective, applying the fractional cointegration technique (FCVAR model), which  
 175 is an expansion of the CVAR approach (see Johansen 1995), is adequate to provide  
 176 more information about the cointegrating rank, the adjustments of the coefficients  
 177 and long-run relationships among different variables—which in the present case are  
 178 financial markets [see, Gagnon et al. (2016)].

### 179 3 Methodology

180 Our econometric strategy involves analysis of stock price data at monthly  
 181 frequency. Once we have our model estimation, we perform statistical tests of  
 182 cointegration, exclusion and weak exogeneity. We then apply the Bai and Perron  
 183 (2003) test for structural breaks and use the FCVAR model to examine each break  
 184 detected.<sup>5</sup>

5FL01 <sup>5</sup> An alternative to our application is to take into account structural breaks, aiming to control the  
 5FL02 dynamics. As suggested by Johansen (2014), in practice, it is important to check the breaks in the  
 5FL03 dynamics. From this perspective, Hansen and Johansen (1999) proposed the theory of recursive  
 5FL04 estimation in the standard cointegration model.



### 185 3.1 Fractional cointegration model: FCVAR methodology

186 Our objective is to study the interdependence of the major Euro stock markets. In  
 187 this paper, the FCVAR model allows us to study the common long-run equilibrium  
 188 relationship between market indices. The model is a generalization of Johansen's  
 189 (1995) cointegrated vector autoregressive (CVAR) model to allow for fractional  
 190 processes of order  $d$  that co-integrate to order  $d-b$ . This model has the advantage of  
 191 being used for stationary and non-stationary time series. This model is presented in  
 192 Johansen (2008a, b) and further developed in Johansen and Nielsen (2012) and  
 193 Nielsen and Popiel (2016), and is gaining traction in finance (Bollerslev et al. 2013  
 194 and Gagnon et al. 2016).

195 To introduce the FCVAR model, we begin with the well-known, non-fractional,  
 196 CVAR model. Being  $Y_t = 1, \dots, T$  a  $p$ -dimensional  $I(1)$  time series. So, the CVAR  
 197 model is:

$$\Delta Y_t = \alpha \beta' Y_{t-1} + \sum_{i=1}^k \Gamma_i \Delta Y_{t-i} + \varepsilon_t = \alpha \beta' L Y_t + \sum_{i=1}^k \Gamma_i \Delta L^i Y_t + \varepsilon_t \quad (1)$$

198 The fractional difference operator introducing persistence in the model is  $\Delta$  and  
 199 the fractional lag operator is  $\Delta = (1 - L)$ . Replacing lags operators in by their  
 200 fractional counterparts  $\Delta^b$  and  $\Delta^b = (1 - L_b)$ , we obtain:

$$\Delta^b Y_t = \alpha \beta' L_b Y_t + \sum_{i=1}^k \Gamma_i \Delta^b L_b^i Y_t + \varepsilon_t, \quad (2)$$

204 we apply to  $Y_t = \Delta^{d-b} X_t$ , such that:

$$\Delta^d X_t = \alpha \beta' L_b \Delta^{d-b} X_t + \sum_{i=1}^k \Gamma_i \Delta^d L_b^i X_t + \varepsilon_t. \quad (3)$$

205 As always,  $\varepsilon_t$  is  $p$ -dimensional independent and identically distributed with mean  
 206 zero and covariance matrix  $\Omega$ . The parameters  $\alpha$  and  $\beta$  are  $p \times r$  matrices, where  
 207  $0 \leq r \leq p$ . In matrix  $\beta$  the columns are the cointegrating relationships and  $\beta' X_t$  are  
 208 the stationary combinations, i.e., the long-run equilibrium. We follow the  
 209 assumption derived from the seminal paper of Kasa (1992) about linearity in the  
 210 relationship. However, on this linearity in our approach, once we are subject to this  
 211 condition, seeks the study of changes in the behavior of the series through the  
 212 analysis of structural breaks proposed by Bai and Perron (2003) as above  
 213 mentioned, which allows us measure possible non-linearity in the time horizon of  
 214 the relationship. The coefficients in  $\alpha$  correspond the speed of adjustment unto  
 215 equilibrium. Therefore,  $\alpha \beta'$  is the adjustment long-run and  $\Gamma_i$  represents the short-  
 216 run behavior of the variables.

217 Considering  $d = b$  as an assumption of no persistence in the cointegration  
 218 vectors and a constant mean term for the cointegrating relations, we reach an  
 219 intermediate step before the final model. That is:



$$\Delta^d X_t = \alpha(\beta' L_d X_t + \rho') + \sum_{i=1}^k \Gamma_i \Delta^d L_d^i X_t + \varepsilon_t. \quad (4)$$

We consider the simple model as:

$$\Delta^d(X_t - \mu) = L_d \alpha \beta' (X_t - \mu) + \sum_{i=1}^k \Gamma_i \Delta^d L_d^i (X_t - \mu) + \varepsilon_t, \quad (5)$$

where the variable  $\mu$  is a level parameter that shifts each of the series by a constant in the way to avoid the bias related to the starting values in the sample (Johansen and Nielsen 2016).  $\beta' \mu = -\rho'$  defines the mean stationary cointegrating relations.

Johansen and Nielsen (2012) show that the maximum likelihood estimators ( $d, \alpha, \Gamma_1, \dots, \Gamma_k$ ) are asymptotically normal and the maximum likelihood estimator of  $(\beta, \rho)$  is asymptotically mixed normal.

For testing the hypotheses on the model parameters we use FCVAR model which is almost equal to CVAR (Johansen 1995). We test if a market is a part of a cointegrating relationship and is included in a long-run equilibrium. Hypotheses on  $\beta$  can be formulated:

$$\beta = H\varphi, \quad (6)$$

where  $H$  is a matrix of dimension  $p \times s$  and contains the restrictions and  $\varphi$  is a matrix of free parameters with dimension  $s \times r$ . The degrees of freedom are given by  $df = (p - s)r$ . If  $r > 1$ , the degrees of freedom of the test is  $df = \sum_{i=1}^r (p - r - s_i + 1)$  (Jones et al. 2014).

With the test of hypotheses  $\alpha$ , we test the weak exogeneity as:

$$\alpha = A\psi, \quad (7)$$

where  $A$  is a matrix of dimension  $p \times m$  and  $\psi$  is a  $m \times r$  matrix of free parameters with  $m \geq r$  (Jones et al. 2014). The degree of freedom of the test is given by  $df = (p - m)r$ . If a row of  $\alpha$  is zero, the associated variable is weakly exogenous.

Note that matrix  $\alpha$  and  $\beta$  are normalized separately in the same way for the CVAR model because the degrees of freedom are non-standard.

To sum up, by estimating the CFVAR model, we extract richer information from what was mentioned in previous sections. Importantly, by separately parameterizing the long-run and the short-run dynamics of the series, the model is able to accommodate empirically realistic  $I(d)$  long-memory and their fractional cointegration, while maintaining that the returns are  $I(0)$  (Bollerslev et al. 2013).

## 4 Empirical analysis

*Data description* For our empirical analysis, we use a sample of closing stock market prices of the four major stock markets of the Eurozone, namely, Germany (DAX), France (CAC), Spain (IBEX) and Italy (FTSE MIB). The data are collected from Yahoo! Finance. Our series are monthly and run from January 1998 to



258 November 2016 (amounting 227 observations). Our analysis begins after converting  
 259 all series to natural logarithms.

260 In Table 1 and Fig. 1, we present descriptive statistics and the dynamics of our  
 261 series. The descriptive statistics associated with the closing prices of each index,  
 262 shown in Table 1, reveal that the FTSE MIB index has the highest volatility, while  
 263 the CAC40 has the lowest, and IBEX and DAX have similar volatility coefficients.  
 264 For its part, Fig. 1 presents the time series dynamics for all indices in terms of how  
 265 the series move; a common trend emerges among the monthly closing prices of  
 266 these indices.

**Table 1** Descriptive statistics for the options data

	DAX	CAC 40	IBEX 35	FTSE MIB
Mean	6440.8	4283.2	9797.4	27,678.0
Median	6123.3	4229.4	9741.5	25,919.0
Min	2423.9	2618.5	5431.7	12,874.0
Max	11,966.0	6625.4	15,890.0	48,479.0
SD	2131.0	891.35	2071.5	9137.1

From 01/1998 to 11/2016



**Fig. 1** Time series plot for used variables

267 **4.1 Testing for fractional cointegration**

268 This section analyses the fractional cointegration of two paths: Univariate analysis  
 269 is presented as an introduction to the second, multivariate analysis.

270 *4.1.1 Univariate analysis*

271 To determine whether the FCVAR model is appropriate to our data, we examine  
 272 each of our series individually before conducting the multivariate analysis. In  
 273 general, if both stationarity tests and unit root tests of a time series are rejected, that  
 274 implies that the time series is likely a fractional time series. Therefore, before  
 275 obtaining estimates of  $d$ , we perform augmented Dickey–Fuller (ADF) and Ng–  
 276 Perron (2001) tests for unit roots on each of our individual series. The results are  
 277 shown in Table 2. All tests reject stationarity, and tests of stock markets do no reject  
 278 the presence of a unit root.

279 There are several procedures for estimating the fractional differencing parameter  
 280 in semiparametric contexts. Although the semiparametric log-periodogram regres-  
 281 sion proposed by Geweke and Porter-Hudak (1983) is the most used, this method  
 282 was modified and further developed by Robinson (1995) and has been analysed by  
 283 Velasco (1999) and Phillips and Shimotsu (2002), among others. Next, we proceed  
 284 to the estimation of the fractional parameter  $d$  for each univariate series, with results  
 285 presented in Table 3. The first three columns are semiparametric log-periodogram

**Table 2** Ng–Perron and Augmented Dickey–Fuller unit root tests for the stock markets

	Parameter	DAX	CAC	FTSE	IBEX	
Ng–Perron	$\overline{MZ}_\alpha^{GLS}$	-7.079	-5.552	-7.458	-8.617	
	$\overline{MZ}_1^{GLS}$	-1.854	-1.166	-1.195	-2.046	
	$\overline{MSB}^{GLS}$	0.262	0.300	0.257	0.237	
	$\overline{MPT}^{GLS}$	12.919	16.411	12.256	10.687	
ADF	Statistic	-1.891	-2.313	-2.457	-2.236	
Critical values (%)	Ng–Perron				ADF	
		$\overline{MZ}_\alpha^{GLS}$	$\overline{MZ}_1^{GLS}$	$\overline{MSB}^{GLS}$	$\overline{MPT}^{GLS}$	$\tilde{t}_\alpha$
1		-23.800	-3.420	0.143	4.030	-3.999
5		-17.300	-2.910	0.168	5.480	-3.413
10		-14.200	-2.620	0.185	6.670	-3.139

The critical values for the Ng–Perron test are tabulated in Ng and Perron (2001). The MAIC information criteria is used to select the autoregressive truncation lag,  $k$ , as proposed in Perron and Ng (1996)

- \*\*\* Rejects null hypothesis at 1% significance level
- \*\* Rejects null hypothesis at 5% significance level
- \* Rejects null hypothesis at 10% significance level

Author Proof

**Table 3** Univariate analysis

	GPH estimates		
	$m = T^{0.4}$ $d$	$m = T^{0.5}$ $d$	$m = T^{0.6}$ $d$
DAX	1.051 (0.223)	1.056 (0.108)	1.165 (0.132)
CAC 40	0.912 (0.555)	0.909 (0.260)	0.968 (0.153)
IBEX 35	1.021 (0.383)	1.000 (0.212)	0.941 (0.128)
FTSE MIB	1.189 (0.169)	1.050 (0.168)	1.170 (0.195)

GPH denotes the Geweke and Porter-Hudak semiparametric log-periodogram regression estimator. Standard errors are given in parenthesis beneath estimates of  $d$ . The sample size is 227

286 regression estimates from Geweke and Porter-Hudak (1983), here labelled GPH,  
287 computed with bandwidths  $m = T^{0.4}$ ,  $m = T^{0.5}$ , and  $m = T^{0.6}$ , respectively.<sup>6</sup>

#### 288 4.1.2 Statistical and hypothesis test

289 First, we determine the number of stationary cointegrating relations, following the  
290 hypotheses of the rank test based on a series of LR tests:  $H_0 : rank = r$ , against the  
291 alternative:  $H_1 : rank = p$  for  $r = 0, 1, \dots$  (See Johansen 1995).

292 The LR test statistics are provided in Johansen and Nielsen (2012), and the  
293  $P$  values are available from MacKinnon and Nielsen (2014), based on their  
294 numerical distribution functions. The estimated rank is the first non-rejected value  
295 of the test, and when this rank is different from zero, we can also conclude that there  
296 exists a long-run equilibrium in the stock markets.

297 Once the rank cointegration test is established, we estimate the model  
298 parameters, using several hypothesis of interest<sup>7</sup> (Table 4). The first hypothesis is  
299  $H_1^d$ , which examines whether fractional integration is more appropriate than  
300 traditional cointegration. The null hypothesis is  $d = 1$ , and its rejection implies that  
301 the FCVAR model is more suitable than a CVAR model. The remaining hypotheses  
302 can be divided into tests of a cointegrated relationship ( $\beta$  parameters) and tests for  
303 weak exogeneity of the variables ( $\alpha$  parameters). The parameters in  $\alpha$  and  $\beta$  are not  
304 identified without additional normalization restrictions; see Johansen (1995).

305 Our primary interest in the cointegrating vectors concerns whether our variables  
306 form a stationary long-run equilibrium. The hypotheses  $H_1^\beta, H_2^\beta, H_3^\beta, H_4^\beta$  are used to  
307 test whether a given stock market is part of a cointegrating relationship and existing  
308 long-run equilibrium. If we reject these hypotheses, we can conclude that a long-run  
309 equilibrium relationship does not exist. The hypotheses  $H_1^\alpha, H_2^\alpha, H_3^\alpha, H_4^\alpha$  are used to  
310 test whether each variable is individually weakly exogenous. If a row of  $\alpha$  is zero,

6FL01 <sup>6</sup> In order to test the presence of unit roots, the estimates were obtained using first-differenced data,  
6FL02 because the original series might be above 0.5 and this test requires that the results are limited to the  
6FL03 interval  $-0.5 < d < 0.5$ , then adding 1 to obtain the proper estimates of  $d$ .

7FL01 <sup>7</sup> Hypothesis testing is explained in paragraph 3, Methodology.

**Table 4** Key for hypothesis test

$H_1^d$	The fractional parameter, $d$ , is equal to one
$H_1^\beta$	FTSEMIB index does not enter the cointegrating relation(s)
$H_2^\beta$	IBEX 35 index does not enter the cointegrating relation(s)
$H_3^\beta$	CAC 40 index does not enter the cointegrating relation(s)
$H_4^\beta$	DAX index does not enter the cointegrating relation(s)
$H_1^\alpha$	FTSEMIB index is weakly exogenous
$H_2^\alpha$	IBEX 35 index is weakly exogenous
$H_3^\alpha$	CAC 40 index is weakly exogenous
$H_4^\alpha$	DAX index is weakly exogenous

311 the variable does not respond to disequilibrium in the relationship. A rejection of the  
 312 null hypothesis implies that a market index adjusts towards the long-run equilibrium  
 313 after a shock.

#### 314 4.1.3 Multivariate analysis

315 To complete our econometric strategy, we apply a multivariate analysis that allows  
 316 us to estimate the possible relations among the variables used and test the different  
 317 hypotheses. At the same time, the univariate analysis provides the value of the  
 318 fractional integer. In this sense, Table 5 presents the estimation results for the  
 319 FCVAR model applied to stock market prices. The null hypothesis of standard  
 320 cointegration  $H_1^d$  is rejected with a  $P$  value of 0.000, suggesting that a fractional  
 321 cointegration model is more appropriate. First, to establish the lag selection, we apply  
 322 BIC criteria (see the “Appendix”, Table 11), selecting a lag length of one. To  
 323 determine whether there is a long-run relationship among the stock markets  
 324 selected, we test the cointegration rank before testing the hypotheses and find that  
 325 the number of cointegrating vectors is three. We test hypotheses  $H_1^\beta$ ,  $H_2^\beta$ ,  $H_3^\beta$ , and  $H_4^\beta$   
 326 to verify that our variables are in the cointegrating relations, using the 10% level of  
 327 significance to reject a given null hypothesis (Jones et al. 2014). The results  
 328 presented for  $\beta$  confirm that we strongly reject the null hypothesis of the non-  
 329 existence of a long-run equilibrium, with a  $P$  value of 0.000, except in the cases of  
 330 the FTSE MIB and IBEX 35, which do not share a long-run relationship. Indeed,  
 331 stock markets that are cointegrated have a long-run relationship, so long-run  
 332 correlations are higher than short-run correlations. If  $n$  variables have  $p$  cointegrating  
 333 relationships, they have  $n - p$  common trends. When  $n - p = 1$ , as in the case  
 334 studied, the individual stock markets are completely and perfectly integrated.  
 335 Moreover, the test of weak exogeneity suggests that the selected stock markets are  
 336 not weakly exogenous.<sup>8</sup>

8FLL01 <sup>8</sup> If a stock market is weakly exogenous, anticipations in this stock market do not adjust to shifts in  
 8FLL02 anticipations for other markets.

**Table 5** Estimated result for FCVAR

Lags	1		
Coint. relation ( $\beta$ )	1	2	3
FTSE MIB	1.000	0	0
IBEX 35	0	1.000	0
CAC 40	0	0	1.000
DAX	0.380	1.143	-0.612
Adjustment matrix ( $\alpha$ )			
FTSE MIB	-0.169	0.008	0.014
IBEX 35	-0.129	-0.002	0.091
CAC 40	-0.082	-0.025	-0.046
DAX	-0.323	0.073	0.308
Hypothesis test	df	LR statistics	<i>P</i> value
$H_1^d$	1	25.422	0.000
$H_1^\beta$	3	4.798	0.187
$H_2^\beta$	3	3.719	0.237
$H_3^\beta$	3	27.186	0.000
$H_4^\beta$	3	97.504	0.000
$H_1^z$	3	17.904	0.000
$H_2^z$	3	31.168	0.000
$H_3^z$	3	9.730	0.021
$H_4^z$	3	30.797	0.000

The top part of the table indicates the optimal number of lags representing the short run dynamics and the estimations of  $\beta$  and  $\alpha$  as well as their associated standard error in parenthesis. The bottom part of the table reports the *P* values for the test of exclusion and weak-exogeneity tested in the Hypothesis test. Following Jones et al. (2014), the significance level is set to 10% for exclusion and weak-exogeneity tests. The sample size is 227

## 337 4.2 Testing the fractional cointegration by structural breaks

338 We consider the possibility that the existence of structural breaks would provide a  
 339 better empirical description of the European market integration. We now apply the  
 340 test for structural breaks proposed by Bai and Perron (2003) with a 15% trimming,  
 341 which limits the maximum number of breaks allowed under the alternative  
 342 hypothesis to 3. Among the breaks identified, the first regime (1998:01 until  
 343 2001:04) is in the way to the introduction of the single currency thus the markets  
 344 were regulating to the new financial context. The second regime (2001:05–2007:06)  
 345 would correspond to the economic growth and expansion period of the countries of  
 346 the stock markets selected. In the third regime (2007:07 until 2012:04), according to  
 347 the European Area Business Cycle Dating Committee, there was the financial crisis  
 348 and the sovereign debt crises. Finally, the fourth regime (2012:05–2016:11) would  
 349 be the end of the sovereign crisis until today. Tables 6, 7, 8, 9 and 10 shows the  
 350 results for each regime.

**Table 6** Bai–Perron tests of multiple structural changes in the relationship between the European stock markets

Statistics						
$UD_{max}$	$WD_{max}$	$SupF_t(1)$	$SupF_t(2)$	$SupF_t(3)$	$SupF_t(4)$	$SupF_t(5)$
256.711***	493.187***	125.278***	246.153***	221.508***	214.213***	256.711***
$SupF_t(2/1)$	$SupF_t(3/2)$	$SupF_t(4/3)$	$SupF_t(5/4)$			
231.393***	42.498***	44.156*	13.411			
Break dates estimates						
$T_1$	2001:4		[2000:03–2001:11]			
$T_2$	2007:6		[2007:05–2007:10]			
$T_3$	2012:4		[2012:01–2012:05]			

\*, \*\*, and \*\*\* denote significance at the 10, 5 and 1% levels, respectively. The critical values are taken from Bai and Perron (1998), Tables 1 and 2; and from Bai and Perron (2003), Tables 1 and 2. The number of breaks has been determined according to the sequential procedure of Bai and Perron (1998), at the 1% size for the sequential test. 90% confidence intervals for  $T_1$  in square brackets

**Table 7** Estimated result for FCVAR (Regime 1)

Lags	1		
Coint. relation ( $\beta$ )	1	2	3
FTSE MIB	1.000	0	0
IBEX 35	0	1.000	0
CAC 40	0	0	1.000
DAX	-1.497	-0.234	-1.609
Hypothesis test	df	LR statistics	<i>P</i> value
$H_1^d$	1	42.259	0.000
$H_1^\beta$	3	17.304	0.001
$H_2^\beta$	3	9.679	0.022
$H_3^\beta$	3	13.822	0.003
$H_4^\beta$	3	10.378	0.016
$H_1^\alpha$	3	9.837	0.020
$H_2^\alpha$	3	6.058	0.109
$H_3^\alpha$	3	4.582	0.205
$H_4^\alpha$	3	7.626	0.054

The top part of the table indicates the optimal number of lags representing the short run dynamics and the estimations of  $\beta$  as well as their associated standard error in parenthesis. The bottom part of the table reports the *P* values for the test of exclusion and weak-exogeneity tested in the Hypothesis test. Following Jones et al. (2014), the significance level is set to 10% for exclusion and weak-exogeneity tests. The sample size is 41



**Table 8** Estimated result for FCVAR (Regime 2)

Lags	1		
Coint. relation ( $\beta$ )	1	2	3
FTSE MIB	1.000	0	0
IBEX 35	0	1	0
CAC 40	0	0	1
DAX	2.263	-1.758	1.234
Hypothesis test	df	LR statistics	<i>P</i> value
$H_1^d$	1	29.503	0.000
$H_1^\beta$	3	15.874	0.001
$H_2^\beta$	3	20.799	0.000
$H_3^\beta$	3	22.958	0.000
$H_4^\beta$	3	52.133	0.000
$H_1^z$	3	39.118	0.000
$H_2^z$	3	17.714	0.001
$H_3^z$	3	36.883	0.000
$H_4^z$	3	38.889	0.000

The top part of the table indicates the optimal number of lags representing the short run dynamics and the estimations of  $\beta$  as well as their associated standard error in parenthesis. The bottom part of the table reports the *P* values for the test of exclusion and weak-exogeneity tested in the Hypothesis test. Following Jones et al. (2014), the significance level is set to 10% for exclusion and weak-exogeneity tests. The sample size is 74

351 Once the structural breaks are defined, we proceed to use the FCVAR model to  
 352 test each regime for cointegration and weak exogeneity. As can be seen in Table 7,  
 353 the *P* value indicates that the null hypothesis of standard cointegration is rejected,  
 354 suggesting that a fractional cointegration model is more appropriate. Applying the  
 355 rank test (which is at most three), the number of cointegrating vectors is three; in  
 356 other words, DAX, CAC 40, IBEX 35 and FTSE MIB are fully integrated. In view  
 357 of the Hypothesis test, the results confirm a long-run equilibrium relationship among  
 358 these variables. Based on the weak-exogeneity test, we accept the null hypothesis,  
 359 with the IBEX 35 index and the CAC 40 index having *P* values of 0.109 and 0.205,  
 360 respectively. Indeed, anticipations in these stock markets do not adjust to shifts that  
 361 occur in the long-run relationship. The empirical results suggest that some linkage  
 362 has existed over time, i.e., there is strong integration among the selected stock  
 363 **AQ5** indices.

364 Turning to the second regime, Table 8 shows the results of the FCVAR model. It  
 365 is observed that the null hypothesis of standard cointegration is strongly rejected.  
 366 The behaviours of the cointegrating vectors match the results of the model applied  
 367 to the original time series; we choose one lag to test the rank of the cointegrating  
 368 vectors, finding three. Testing the  $\beta$  hypotheses, we determine that the null  
 369 hypothesis of the non-existence of a long-run equilibrium is rejected in all cases,  
 370 and we also reject the hypothesis of weak exogeneity. In sum, in this regime, the

**Table 9** Estimated result for FCVAR (Regime 3)

Lags	1		
Coint. relation ( $\beta$ )	1		2
FTSE MIB	1.000		0
IBEX 35	0		1.000
CAC 40	-1.842		-1.963
DAX	0.719		-0.146
Hypothesis test	df	LR statistics	P value
$H_1^d$	1	21.353	0.000
$H_1^\beta$	3	8.673	0.013
$H_2^\beta$	3	1.255	0.534
$H_3^\beta$	3	7.738	0.021
$H_4^\beta$	3	6.762	0.024
$H_1^z$	3	31.754	0.000
$H_2^z$	3	15.369	0.000
$H_3^z$	3	32.219	0.000
$H_4^z$	3	15.353	0.000

The top part of the table indicates the optimal number of lags representing the short run dynamics and the estimations of  $\beta$  as well as their associated standard error in parenthesis. The bottom part of the table reports the  $P$  values for the test of exclusion and weak-exogeneity tested in the Hypothesis test. Following Jones et al. (2014), the significance level is set to 10% for exclusion and weak-exogeneity tests. The sample size is 58

371 cointegrating vectors exhibit the same behaviour as in the original sample, implying  
 372 that the stock indices are fully and perfectly integrated.

373 For the third regime (Table 9), which corresponds to the financial and European  
 374 sovereign debt crisis period, we also strongly reject the null hypothesis of standard  
 375 cointegration, with a  $P$  value of 0.000. Additionally, using the rank test, we find that  
 376 there are two cointegrating vectors. Therefore, following Kasa (1992), the market  
 377 integration is neither complete nor perfect. An explanation of this result is that this  
 378 was a convulsive and uncertain period, and as we can see, the IBEX 35 index does  
 379 not belong to the long-run relationship, perhaps owing to the observed integration  
 380 weakness. Thus, the weak-exogeneity test shows that all markets adjust to shifts in  
 381 anticipation of other markets. With respect to the IBEX 35 index, we appreciate that  
 382 unless this market is not in the long-run relation, it is affected by such a relationship.

383 To complete our review of the regimes, the application of the FCVAR model to  
 384 the fourth regime is shown in Table 10. First, as we have done previously, we test  
 385 the hypothesis of standard cointegration, which is strongly rejected, with a  $P$  value  
 386 of 0.000. Then, we test the rank of the cointegrating vector, finding three, which  
 387 means that once the sovereign debt crisis ended, Euro market integration again  
 388 became complete. In the case of the weak-exogeneity test, we observe that in none  
 389 of the cases of the selected markets is the null hypothesis rejected, which means that

**Table 10** Estimated result for FCVAR (Regime 4)

Lags	1		
Coint. relation ( $\beta$ )	1	2	3
FTSE MIB	1.000	0	0
IBEX 35	0	1.000	0
CAC 40	0	0	1.000
DAX	0.014	0.129	-0.694
Hypothesis test	df	LR statistics	<i>P</i> value
$H_1^d$	1	34.563	0.000
$H_1^\beta$	3	14.667	0.002
$H_2^\beta$	3	22.645	0.000
$H_3^\beta$	3	7.039	0.071
$H_4^\beta$	3	8.971	0.030
$H_1^z$	3	27.253	0.000
$H_2^z$	3	26.205	0.000
$H_3^z$	3	24.059	0.000
$H_4^z$	3	16.717	0.001

The top part of the table indicates the optimal number of lags representing the short run dynamics and the estimations of  $\beta$  as well as their associated standard error in parenthesis. The bottom part of the table reports the *P* values for the test of exclusion and weak-exogeneity tested in the Hypothesis test. Following Jones et al. (2014), the significance level is set to 10% for exclusion and weak-exogeneity tests. The sample size is 54

390 anticipations in these stock markets do not adjust to shifts in the long-run  
391 relationship. The results obtained are similar to those for regime 2.

## 392 5 Conclusion

393 In this paper, we have studied European stock market cointegration, using a  
394 fractionally cointegrated vector autoregressive (FCVAR) model applied to the  
395 closing prices of the major four stock market indices in the Eurozone. Despite  
396 controversy in the existing literature regarding treatment of this issue, the fractional  
397 cointegration model avoids most of the problems raised in the literature.  
398 Additionally, this model allows us to identify financial integration and weak  
399 exogeneity in our monthly time series.

400 Our equilibrium is characterized by three cointegrating vectors, which, following  
401 Kasa (1992), suggests that the individual stock markets are fully and perfectly  
402 integrated. However, to improve the analysis, we consider the existence of structural  
403 breaks, applying the Bai–Perron test and then testing the FCVAR model in each of  
404 four regimes—regimes that correspond to the introduction of the Euro currency, the  
405 financial crisis, the end of the sovereign debt crisis and a final period that runs  
406 through November 2016. The FCVAR model indicates some significant differences

407 in patterns of convergence throughout the original sample as a function of the  
 408 regime studied. The results for the different regimes show that, for the most part,  
 409 integration of the European markets has been complete but also that, during the  
 410 sovereign debt crisis, full integration of these indices disappeared. The reason for  
 411 this development is that the IBEX 35 index went out of long-run equilibrium, which  
 412 could mean that this index was more sensitive during this quarrelsome period, while  
 413 the other markets were more robust—i.e., that the IBEX 35 index is the weak link in  
 414 the integration. We therefore wish to emphasize the case of the Italian market  
 415 (FTSE MIB), which, like the others, suffered from a sovereign debt crisis but, in  
 416 contrast to the others, remained in the long-run relationship. Once this turbulent  
 417 period ended, full Euro financial integration resumed, as we see in the fourth  
 418 regime, although interest rates spreads, notably those of Italy, started to increase  
 419 again in the second half of 2016. Financial integration is attributable to techno-  
 420 logical advances during recent decades, which has reduced transaction costs and  
 421 allowed for greater access to information, notably reducing differences between  
 422 national and international financial transactions. It has thus contributed to more  
 423 sustainable economic growth.

424 The findings of the paper have important implications for investors and policy-  
 425 makers. For investors, the high degree of integration implies a more attractive place  
 426 for investment. However, this equilibrium also implies that portfolio diversification  
 427 will be less effective. As stock market prices are interrelated, the possibility of  
 428 strong impacts from external shocks is not reduced. In this line, cointegration is not  
 429 the same as contagion. This is because cointegration may imply perfect spillover or,  
 430 alternatively, no spillover at all if the variables are driven by a common third factor,  
 431 which may be a global factor (Belke et al. 2017). For policy makers, market  
 432 integration in the Eurozone has led to various debates. Market integration has  
 433 increased competition and market efficiency and led to greater interdependence  
 434 between the Eurozone markets; this may require increased supervision and  
 435 securities market oversight, as Mylonidis and Kollias (2010) and Fratzscher  
 436 (2002) find in their studies. Therefore, investors will prefer to invest in markets  
 437 characterized by increasing growth, which will give them more investment options  
 438 and risk diversification opportunities (e.g., buying stocks in two submarkets). There  
 439 is thus potential gain through a focus on local rather than global factors. Future  
 440 research into long-run relationships among the selected stock markets may focus on  
 441 cycles to find possible synchronicity among markets. In addition, testing for breaks  
 442 in the dynamics may be a new analytical approach to understanding the integration  
 443 of markets. That is, future research could be oriented to the study of breaks in the  
 444 dynamics of a Fractional Cointegration Approach, for instance, applying recursive  
 445 **AQ6** estimation or rolling cointegration.

## 446 Appendix

### 447 Original sample

448 See Tables 11 and 12.

**Table 11** Lag length selection

K	LR statistics	AIC	BIC
0	0.00	-3512.62	-3440.70
1	56.88	-3537.50	<b>-3410.78</b>
2	27.76	-3533.27	-3351.75
3	87.67	-3588.94	-3352.62
4	36.42	-3593.36	-3302.24
5	-2.01	-3559.35	-3213.43
6	108.55	-3635.90	-3235.18

The table shows lag length selection and bold indicates lag order selected. The sample size is 227

**Table 12** Cointegration rank test

Rank	Log-likelihood	LR statistics	<i>P</i> value
0	1779.254	52.996	0.060
1	1788.489	34.525	0.033
2	1792.018	27.468	0.003
3	1805.231	1.042	0.307
4	1805.752	-	-

The table shows the rank test. Following Jones et al. (2014), the significance level is set to 10% for exclusion. The sample size is 227

449 **Regime 1**

450 See Table 13.

**Table 13** Cointegration rank test

Rank	Log-likelihood	LR statistics	<i>P</i> value
0	294.552	56.201	0.000
1	307.954	29.397	0.001
2	317.988	9.330	0.053
3	321.685	1.934	0.164
4	322.652	-	-

The table shows the rank test. Following Jones et al. (2014), the significance level is set to 10% for exclusion. The sample size is 41

451 **Regime 2**

452 See Table 14.

**Table 14** Cointegration rank test

Rank	Log-likelihood	LR statistics	<i>P</i> value
0	583.557	84.570	0.000
1	598.455	54.774	0.000
2	617.983	15.718	0.003
3	625.788	0.109	0.741
4	625.842	–	–

The table shows the rank test. Following Jones et al. (2014), the significance level is set to 10% for exclusion. The sample size is 74

453 **Regime 3**

454 See Table 15.

**Table 15** Cointegration rank test

Rank	Log-likelihood	LR statistics	<i>P</i> value
0	436.957	37.846	0.001
1	442.765	26.231	0.001
2	454.411	2.939	0.568
3	455.608	0.545	0.460
4	455.880	–	–

The table shows the rank test. Following Jones et al. (2014), the significance level is set to 10% for exclusion. The sample size is 58

455 **Regime 4**

456 See Table 16.

**Table 16** Cointegration rank test

Rank	Log-likelihood	LR statistics	<i>P</i> value
0	442.787	51.266	0.000
1	444.708	47.425	0.000
2	462.616	11.608	0.020
3	467.517	1.806	0.178
4	468.420	–	–

The table shows the rank test. Following Jones et al. (2014), the significance level is set to 10% for exclusion. The sample size is 54

459 **References**

- 460 Alvarez-Ramirez J, Alvarez J, Rodriguez E, Fernandez-Anaya G (2008) Time-varying Hurst exponent for  
 461 US stock markets. *Phys A Stat Mech Appl* 387(24):6159–6169
- 462 Bai J, Perron P (2003) Computation and analysis of multiple structural change models. *J Appl Econom*  
 463 18(1):1–22
- 464 Belke A, Gros D, Osowski T (2017) The effectiveness of the Fed's quantitative easing policy: new  
 465 evidence based on international interest rate differentials. *J Int Money Financ* 73:335–349
- 466 Bessler DA, Yang J (2003) The structure of interdependence in international stock markets. *J Int Money*  
 467 *Financ* 22(2):261–287
- 468 Bley J (2009) European stock market integration: fact or fiction? *J Int Financ Mark Inst Money*  
 469 19(5):759–776
- 470 Bollerslev T, Osterrieder D, Sizova N, Tauchen G (2013) Risk and return: long-run relations, fractional  
 471 cointegration, and return predictability. *J Financ Econom* 108:409–424
- 472 Brooks C (2014) *Introductory econometrics for finance*. Cambridge University Press, Cambridge
- 473 Caporale GM, Gil-Alana LA, Orlando JC (2015) Linkages between the US and European stock markets: a  
 474 fractional cointegration approach. *Int J Financ Econ* 21:143–153
- 475 Chouliaras A, Christopoulos AG, Kenourgios D, Kalantonis P (2012) The PIIGS stock markets before and  
 476 after the 2008 financial crisis: a dynamic cointegration and causality analysis. *Int J Bank Acc Financ*  
 477 4(3):232–249
- 478 Corhay A, Rad AT, Urbain JP (1993) Common stochastic trends in European stock markets. *Econ Lett*  
 479 42(4):385–390
- 480 Da Fonseca JS (2013) Innovations in return transmission and performance comparison between the five  
 481 biggest Euro area stock markets. *IIEP* 10(3):393–404
- 482 Darrat AF, Zhong M (2005) Equity market linkage and multinational trade accords: the case of NAFTA.  
 483 *J Int Money Financ* 24(5):793–817
- 484 Demian CV (2011) Cointegration in Central and East European markets in light of EU accession. *J Int*  
 485 *Financ Mark Inst Money* 21(1):144–155
- 486 Dickey D, Fuller WA (1979) Distribution of the estimators for autoregressive time series with a unit root.  
 487 *J Am Stat Assoc* 74(366a):427–431
- 488 **A07** Dickey DA, Fuller WA (1981) Likelihood ratio statistics for autoregressive time series with a unit root.  
 489 *Econom J Econom Soc* 1057–1072
- 490 Dickinson DG (2000) Stock market integration and macroeconomic fundamentals: an empirical analysis,  
 491 1980–95. *Appl Financ Econ* 10(3):261–276
- 492 Fama EF (1970) Efficient capital markets: a review of theory and empirical work. *J Financ* 25(2):383–417
- 493 Fama EF (1991) Efficient capital markets: II. *J Financ* 46(5):1575–1617
- 494 Forbes K, Rigobon R (2002) No contagion, only interdependence: measuring stock market comovements.  
 495 *J Financ* 7(5):2223–2261
- 496 Francis BB, Leachman LL (1998) Superexogeneity and the dynamic linkages among international equity  
 497 markets. *J Int Money Financ* 17(3):475–492
- 498 Fratzscher M (2002) Financial market integration in Europe: on the effects of EMU on stock markets. *Int*  
 499 *J Financ Econ* 7(3):165–193
- 500 Gagnon MH, Power GJ, Toupin D (2016) International stock market cointegration under the risk-neutral  
 501 measure. *Int Rev Financ Anal* 47:243–255
- 502 Geweke J, Porter-Hudak S (1983) The estimation and application of long memory time series models.  
 503 *J Time Ser Anal* 4(4):221–238
- 504 Gil-Alana L, Cunado J, de Gracia FP (2013) Salient features of dependence in daily US stock market  
 505 indices. *Phys A* 392:3198–3212
- 506 Gonzalo J (1994) Five alternative methods of estimating long-run equilibrium relationships. *J Econom*  
 507 60(1):203–233
- 508 Granger C, Hyung N (2004) Occasional structural breaks and long memory with an application to the S&P  
 509 500 absolute stock returns. *J Empir Financ* 11:399–421
- 510 Hamao Y, Masulis RW, Ng V (1990) Correlations in price changes and volatility across international  
 511 stock markets. *Rev Financ Stud* 3(2):281–307
- 512 Hansen H, Johansen S (1999) Some tests for parameter constancy in cointegrated VAR-models. *Econom*  
 513 *J* 2(2):306–333



- 514 Heimonen K (2010) Stock market integration: evidence on price integration and return convergence. *Appl*  
 515 *Financ Econ* 12(6):415–429
- 516 Huang BN (1995) Do Asian stock market prices follow random walks? Evidence from the variance ratio  
 517 test. *Appl Financ Econ* 5(4):251–256
- 518 Illueca M, Lafuente J (2002) International stock market linkages: a factor analysis approach. *J Asset*  
 519 *Manag* 3(3):253–265
- 520 Jawadi F, Arouri ME (2008) Are American and French stock markets integrated? *Int J Bus Financ Res*  
 521 2(2):107–116
- 522 Johansen S (1988) Statistical analysis of cointegration vectors. *J Econ Dyn Control* 12(2):231–254
- 523 Johansen S (1991) Estimation and hypothesis testing of cointegration vectors in Gaussian vector  
 524 autoregressive models. *Econom J Econom Soc* 1551–1580
- 525 Johansen S (1995) Likelihood based inference on cointegration in the vector autoregressive model.  
 526 Oxford University Press, Oxford
- 527 Johansen S (2008a) A representation theory for a class of vector autoregressive models for fractional  
 528 processes. *Econom Theory* 24:651–676
- 529 Johansen S (2008b) Representation of cointegrated autoregressive processes with application to fractional  
 530 processes. *Econom Rev* 28:121–145
- 531 Johansen S (2014) Time series: cointegration. Centre for Research in Econometric Analysis of Time  
 532 Series, Aarhus
- 533 Johansen S, Nielsen MØ (2012) Likelihood inference for a fractionally cointegrated vector autoregressive  
 534 model. *Econometrica* 80(6):2667–2732
- 535 Jones ME, Nielsen MØ, Popiel MK (2014) A fractionally cointegrated VAR analysis of economic voting  
 536 and political support. *Can J Econ* 47(4):1078–1130
- 537 Karmann A, Ludwing A (2014) A two-step approach to examine the dynamics of market convergence.  
 538 *Appl Econ Lett* 21(4):284–288
- 539 Kasa K (1992) Common stochastic trends in international stock markets. *J Monet Econ* 29:95–124
- 540 Kenourgios D, Samitas A, Paltalidis N (2009) Financial market dynamics in an enlarged European union.  
 541 *J Econ Integr* 24(2):197–221
- 542 Kim SJ, Moshirian F, Wu E (2005) Evolution of international stock and bond market integration:  
 543 influence of the European Monetary Union. *J Bank Financ* 30:1507–1534
- 544 Kim H, Stern LV, Stern ML (2009) Nonlinear mean reversion in the G7 stock markets. *Appl Financ Econ*  
 545 19(5):347–355
- 546 Lee KS, Mercurelli F (2014) Convergence in the core Euro zone under the global financial crisis. *J Econ*  
 547 *Inter* 29(1):20–63
- 548 Lo AW, MacKinlay AC (1988) Stock market prices do not follow random walks: evidence from a simple  
 549 specification test. *Rev Financ Stud* 1(1):41–66
- 550 Longin F, Solnik B (1995) Is the correlation in international equity returns constant: 1960–1990? *J Int*  
 551 *Money Financ* 14(1):3–26
- 552 MacKinnon JG, Nielsen MØ (2014) Numerical distribution functions of fractional unit root and  
 553 cointegration tests. *J Appl Econom* 29:161–171
- 554 Markellos RN, Siriopoulos C (1997) Diversification benefits in the smaller European stock markets. *Int*  
 555 *Adv Econ Res* 3(2):142–153
- 556 Mikosch T, Starica C (2000) Limit theory for the sample autocorrelations and extremes of a GARCH (1,  
 557 1) process. *Ann Stat* 28(5):1427–1451
- 558 **AQS** Mylonidis N, Kollias C (2010) Dynamic European stock market convergence: evidence from rolling  
 559 cointegration analysis in the first euro-decade. *J Bank Financ* 34:2056–2064
- 560 Ng S, Perron P (2001) Lag length selection and the construction of unit root tests with good size and  
 561 power. *Econometrica* 69(6):1519–1554
- 562 Nielsen MØ, Popiel MK (2016) A Matlab program and user's guide for the fractionally cointegrated VAR  
 563 model. In: QED working paper, p 1330
- 564 Phillips PCB, Shimotsu K (2002) Pooled log periodogram regression. *J Time Ser Anal* 23(1):57–93
- 565 Richards AJ (1995) Comovements in national stock markets returns: evidence of predictability, but not  
 566 cointegration. *J Monet Econ* 36(3):631–654
- 567 Robinson PM (1995) Log-periodogram regression of time series with long range dependence. *Ann Stat*  
 568 23:1048–1072
- 569 Salgado RJS, Escobar Saldivar LJ, Gurrola Ríos C (2015) Cointegración entre las principales bolsas de  
 570 Europa continental en presencia de rompimientos estructurales (1999–2014). *Contad Adm*  
 571 60:83–105





- 572 Sharpe WF (1964) Capital asset prices: a theory of market equilibrium under conditions of risk. *J Financ*  
 573 19(3):425–442
- 574 Smith G (2007) Random walks in Middle Eastern stock markets. *Appl Financ Econ* 17(7):587–596
- 575 Solnik B (1974) An equilibrium model of the international capital market. *J Econ Theory* 8(4):500–524
- 576 Syriopoulos T (2007) Dynamic linkages between emerging European and developed stock markets: has  
 577 the EMU any impact? *Int Rev Financ Anal* 16(1):41–60
- 578 Taylor MP, Tonks I (1989) The internationalisation of stock markets and the abolition of UK exchange  
 579 control. *Rev Econ Stat* 332–336
- 580 Tian G (2007) Are Chinese stock markets increasing integration with other markets in the greater China  
 581 region and other major markets? *Aust Econ Pap* 46(3):240–253
- 582 Velasco C (1999) Nonstationary log-periodogram regression. *J Econom* 91:299–323
- 583 Wong WK, Agarwal A, Du J (2004) Financial integration for India stock market: a fractional co-  
 584 integration approach. *Financ India* 18(4):1581
- 585 Yang F (2012) A note on cointegration methodology in studying stock markets integration. *Appl Econ*  
 586 *Lett* 19(16):1583–1586
- 587 **AQ9** Yang J, Kolari JW, Min I (2003) Stock market integration and financial crises: the case of Asia. *Appl*  
 588 *Financ Econ* 13:477–486

Journal : 10663

Article : 9386



the language of science

## Author Query Form

**Please ensure you fill out your response to the queries raised below and return this form along with your corrections**

Dear Author

During the process of typesetting your article, the following queries have arisen. Please check your typeset proof carefully against the queries listed below and mark the necessary changes either directly on the proof/online grid or in the 'Author's response' area provided below

Query	Details Required	Author's Response
AQ1	Kindly check and confirm whether the corresponding author is correctly identified and amend if necessary.	
AQ2	Please check and confirm the authors given name and family name are correctly identified.	
AQ3	Please confirm the section headings are correctly identified.	
AQ4	Caporale et al. (2016) has been changed to Caporale et al. (2015), Wong et al. (2005) has been changed to Wong et al. (2004), Bai and Perron (2003b) has been changed to Bai and Perron (2003), Johansen (1996) has been changed to Johansen (1995), Velasco (1999b) has been changed to Velasco (1999), Shimotsu and Phillips (2002) has been changed to Phillips and Shimotsu (2002) so that these citations match the list.	
AQ5	Reference Bai and Perron (1998) is cited in text but not provided in the reference list. Please provide references in the list or delete this citation.	
AQ6	Kindly check and confirm whether the appendix tables are correctly processed.	
AQ7	Kindly provide volume number for Refs. Dickey and Fuller (1981), Johansen (1991) and Taylor and Tonks (1989).	
AQ8	Kindly check and confirm the inserted volume number in Ref. Mylonidis and Kollias (2010).	
AQ9	Kindly check and confirm the inserted volume number and page range in Ref. Yang et al. (2003).	