# Designing evacuation routes with GeoGebra 

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#### Abstract

We expose in this paper how the command ShortestDistance can be used in GeoGebra to design evacuation routes in buildings in a dynamic and interactive way. For those cases in which a legal regulation or procedure compels specific requirements in the design, we also indicate how to make use of JavaScript in order to implement a more general version of Dijkstra's algorithm that makes possible to deal with such specifications.


KEYWORDS: Evacuation route, Graph Theory, Dijkstra's algorithm.

## 1 Introduction

Nowadays, the importance of designing optimal evacuation routes in public and private buildings is unquestionable due to the fact that they guarantee, with a very high probability, the safe evacuation of all their occupants in case of any kind of emergency. In the case of buildings like schools, hospitals or hotels, all these routes have to be clearly visible to everybody and, because of
that, it is usual or even mandatory to post evacuation maps in all their rooms and corridors. The problem of these maps is that they are usually fixed and static and they could point exactly at the cause of the emergency, like the seat of a fire, for instance. In order to avoid these cases, it is interesting to have dynamic screens or LED lamps that could show in real time which is exactly the evacuation route that must be follow the person who is watching them. Keeping this idea in mind, we expose in this paper how to use GeoGebra in order to design a dynamic evacuation map that make possible a fast update of the evacuation routes of a building in case of being necessary.

The paper is organized as follows. In Section 2 we introduce the shortest path problem in Graph theory and expose how the command ShortestDistance, which is implemented by defect in GeoGebra, can be used to solve this problem. We focus specifically on the creation of a template in GeoGebra that makes possible to design a dynamic and interactive evacuation map of a building whose plan has been previously inserted in the worksheet. In Section 3 we make use of JavaScript in order to implement in GeoGebra the Dijkstra's algorithm, which is commonly used to solve the shortest path problem for any connected and weighted graphs with non-negative weights. This implementation makes possible to deal with legal regulations or procedures that compel specific requirements in the design of evacuation routes.

## 2 The shortest path problem

We start with some basic results on Graph theory that are used throughout the paper. For more details on this topic we refer to the monograph of Gross and Yellen [GY04].

A graph $G=(V, E)$ is a pair formed by a set $V$ of points called vertices and a set $E$ of segments connecting them called edges (see Figure 1). It is said to be directed if its edges has a direction from one of its vertices to the other one. Otherwise, the graph is said to be undirected. A path between two given vertices $v$ and $v^{\prime}$ in $E$ is a series of vertices $v_{0}=v_{1}, v_{l}, \ldots, v_{n}=v^{\prime}$ such that $v_{i} v_{i+1}$ determines an edge in $E$, for all $i \in\{0, \ldots, n-1\}$. The graph $G$ is said to be connected if there exists a path for any pair of its vertices. Further, if the graph $G$ is weighted, that is, if every edge $e$ in $E$ has associated a numerical label or weight $W_{e}$, then the shortest path problem consists of finding a path between two given vertices that minimizes the sum of weights of its edges. This minimum sum of weights constitutes the length of the minimal path or the graph distance between the two given vertices.

This problem can be solved in GeoGebra for weighted graphs whose weights are either constant or are determined by the Euclidean distance between connected vertices, that is, by the length of the edges. In the first case, the shortest path between two given points of the graph is a path with the minimum possible number of edges between both points. Once a weighted undirected graph $G$ has been drawn in a worksheet of GeoGebra as a set of points (vertices) and segments (edges) and the initial and final points of the path, $A$ and $B$, have been identified, it is enough to create a list $L$ containing all the segments of the graph. Then, we enter in the input bar the command

ShortestDistance [L, A, B, <Boolean Weighted $>$ ],
where the Boolean value can be true or false depending, respectively, on whether we use the Euclidean distance or the number of edges between two given points. Figure 1 shows an example in this regard. The red edges determine the shortest path between the points $B$ and $E$ according to the Euclidean distance whereas the green ones determine the path with the minimum number of edges between both points.


Figure 1: Shortest path problem in GeoGebra.

The command ShortestDistance together with the dynamical structure of the graphics view of Geogebra constitutes an especially useful tool to design dynamic and interactive evacuation maps. In this regard, let us suppose that we are interested in designing an evacuation map of the building whose plan is shown in Figure 2. It represents the ground floor of the School of Building Engineering at the University of Seville, in which we can observe the existence of three emergency exit doors. This map has conveniently been inserted in the graphic view of GeoGebra in such a way that the image respects the real scale. In this case, the real size of the plan is $720 \times 740 \mathrm{~m}^{2}$.


Figure 2: Plan of the first ground of a school.
In order to design our evacuation map in GeoGebra, it is required to determine a graph that represents the distribution of rooms, corridors and stairs. To this end we draw a series of points and edges by following the next sequential order:

- We draw a point for each door or stair in the plan (see Figure 3.a). The points related to the emergency exit doors are called Exitl, Exit2 and Exit3.
- We draw an edge for each pair of such points that are related to distinct doors in a same room (see Figure 3.b).
- In front of each door and stair, in the middle of corridors, we draw a point connected by an edge with the point of the corresponding door or stair. Adjacent points in the corridor are also connected with an edge (see Figure 3.c).

The resulting graph (see Figure 3.d and Figure 4) is called the base graph of the evacuation map. Once this graph is constructed, we click on the tool Create List in the Toolbar of GeoGebra and we create the list $L$ of edges that will be used as argument of the command ShortestDistance. After that, we define in the input bar the text Origin $=$ " $A$ ", which we hide immediately after from the graphics view and for which we create a related input box (see Figure 5). In the On Update tab of the Scripting tab of the input box, we write the next code in GeoGebra script:


Figure 3: Construction of the base graph of an evacuation map.


Figure 4: Base graph of an evacuation map.


Figure 5: Evacuation route in GeoGebra.

> Execute[\{"path1=ShortestDistance [L,"+OVigin+", Exit1, true]",
> "path $2=$ ShortestDistance $[L$, "+Origin+", Exit2, true]",
> "path $3=$ ShortestDistance[L, "+Origin+", Exit 3, true]" $\}]$
> path $=\{$ Length[path1], Length[path2], Length[path3]\}

This code involves the computation of the three possible evacuation routes from the given initial point to the three possible emergency exit doors and of their respective lengths. Since we are only interested in the evacuation route of minimum length, we have to make use of some condition to show object in the advanced properties of each one of the three paths. Specifically, we impose in pathl, path 2 and path 3 the respective conditions:

$$
\begin{aligned}
& \text { Min[RemoveUndefined[path]] } \stackrel{?}{=} \text { Length[path1] } \\
& \text { Min[RemoveUndefined[path]] } \stackrel{?}{=} \text { Length[path2] } \\
& \text { Min[RemoveUndefined[path]] } \text { Length[path3] }
\end{aligned}
$$

After that, our template constitutes a dynamical and interactive evacuation map of our building where it is enough to define in the created input box the initial point from where the shortest evacuation route is required. Moreover, the use of the command RemoveUndefined in the just exposed three conditions makes possible to delete a series of edges in the base graph of the evacuation map that, in case of an emergency, are temporally
blocked, due to fire propagation or gas leak, for example. These edges are directly eliminated from the list $L$ of edges and, after that, new alternative evacuation routes are automatically obtained (see Figure 6, where there are indicated a pair of alternative routes of the shortest path shown in Figure 5, in case of being blocked one or two of the closer emergency exit doors).


Figure 6: Alternative routes when some emergency exit doors are blocked.

Nevertheless, even if our evacuation route is automatically selected and exposed by GeoGebra as the shortest path between the initial point in question and the three possible emergency exit doors, two important remarks have to be done to our construction:

1) Real evacuation routes must facilitate paths through wide corridors and avoid, whenever is possible, to enter from one corridor to a small room as a crossing point of our path. It is due to the fact that this type of rooms could constitute bottle necks in case of an emergency. Nevertheless, since our base graph is undirected and our shortest path is obtained by taking into account the Euclidean distance, GeoGebra include these small rooms as possible crossing points of the final evacuation route (see Figure 7).
2) Depending on the type of building, there can exist a series of legal regulations or procedures that compel specific requirements in the design of an evacuation route like the minimum width or height of doors and stairs, the lengths of corridors or the maximum number of people (capacity) that can use a certain route, amongst others. Nevertheless, none of these factors can be taken into account in our previously designed evacuation route.


Figure 7: Evacuation route proposed by GeoGebra.

It is therefore necessary to generalize our construction in order to deal with more realistic evacuation routes. To this end, we propose in the next section to make use of Javascript in order to implement the Dijkstra's algorithm in GeoGebra.

## 3 The Dijkstra's algorithm

In 1959, Edsger W. Dijkstra [Dij59] established an algorithm that solves the shortest path problem for connected and weighted graphs with non-negative weights. These graphs can be directed or undirected. In the course of the algorithm, given a weighted graph $G=(V, E)$ and the initial and final vertices, $v$ and $v^{\prime}$, of the path, Dijkstra subdivides the set of vertices $V$ into three sets:

- The set $V_{l}$ of vertices $w$ for which the path of minimum length from $v$ is known.
- The set $V_{2}$ of vertices in $V-V_{l}$ that are connected by one edge to at least one vertex of $V_{l}$. If the graph is directed, then this edge must be oriented from the vertex in $V_{1}$ to the vertex in $V_{2}$.
- The set $V_{3}$ formed by the rest of vertices.

Dijkstra also subdivides the set of edges $E$ in other three sets:

- The set $E_{l}$ of edges in the minimal paths from $v$ to the vertices of $V_{1}$.
- The set $E_{2}$ of edges in $E-E_{1}$ that connect vertices of $V_{1}$ and $V_{2}$.
- The set $E_{3}$ formed by the rest of edges.

At the beginning of the algorithm, all the vertices are in $V_{3}$ and all the edges are in $E_{3}$. The vertex $v$ is then the first vertex to be included in $V_{1}$. At each step of the algorithm, it is considered all the edges $e$ that connect the last vertex $w$ included in $V_{1}$ with vertices $w^{\prime}$ in $V_{2} \cup V_{3}$.

- If the vertex $w^{\prime}$ is in $V_{3}$, then it is added to $V_{2}$ and the edge $e$ is added to $E_{2}$. The path of minimum length $l_{w}$ between $v$ and $w$ together with the edge $e$ of weight $W_{e}$ determines a provisional path between $v$ and $w^{\prime}$ of length $l_{w^{\prime}}=l_{w}+W_{e}$.
- If the vertex $w^{\prime}$ is already in $V_{2}$, then there exists exactly one edge $e^{\prime}$ in $E_{2}$ that connects w' with a vertex $w^{\prime \prime}$ in $V_{l}$ so that the path of minimum length $l_{w^{\prime \prime}}$ between $v$ and $w^{\prime \prime}$ together with the edge $e^{\prime}$ of weight $W_{e^{\prime}}$ determines a provisional path of minimum length $l_{w^{\prime}}=$ $l_{w^{\prime \prime}}+W_{e^{\prime}}$. If $l_{w^{\prime}} \leq l_{w}+W_{e}$, then the edge $e$ is rejected. Otherwise, the edge $e$ replaces the edge $e$ ' in $V_{2}$.

After that, the vertex in $V_{2}$ with the shortest provisional path from $v$ and its related edge in $E_{2}$ are respectively transferred to $V_{1}$ and $E_{1}$, and the procedure is then repeated for this new vertex in $V_{l}$. The algorithm finishes when the final vertex $v^{\prime}$ is transferred to $V_{l}$.

In practice, the $n$ vertices of the graph are initially ordered and labeled as $v_{l}, \ldots, v_{n}$. An auxiliary ordered list $L$ of cardinality $n$, initialized as $\{0, \ldots, 0\}$, can then be defined in the course of the algorithm in such a way that its $i^{\text {th }}$ element is the immediately previous vertex through which any shortest path starting in $v$ has to pass to get the vertex $v_{i}$. It coincides with the second vertex related to the edge that is transferred to $E_{l}$ at the same time that $v_{i}$ is transferred to $V_{l}$. Once the algorithm finishes, this list determines all the previous vertices through which the shortest path from $v$ to $v^{\prime}$ has to pass.

Further, since the algorithm can be repeated for any pair of vertices, it is also possible to determine the distance matrix $D=\left(d_{i j}\right)$ of the graph, where $d_{i j}$ is the length of the shortest path between the vertices $v_{i}$ and $v_{j}$ of the graph.

As an example of implementation of the Dijkstra's algorithm, we show in Figure 8 the steps that are sequentially required to determine the shortest path between two vertices, $A$ and $I$, of a given undirected graph. Orange edges determine the vertices and edges that are transferred in each step to the sets $V_{l}$ and $E_{l}$, respectively. Below each image we indicate the vertices $w$ that are in the set $V_{2}$ after each step, which are indicated as pairs $\left(w, l_{w}\right)$, where $l_{w}$ is the weight of the provisional minimum path to $w$ from the vertex $A$ by only taking into consideration the edges in $E_{2}$. The ordered auxiliary list $L$ is also
indicated in each step. We have used the lexicographical order. Let us examine the procedure in detail.

- Step 0: The initial vertex $A$ is transferred to $V_{l}$.
- Step 1: We transfer to $V_{2}$ the vertices in $V_{3}$ connected to $A$, that is, $B$ and $C$. The edges $A B$ and $A C$ are transferred to $E_{2}$. Since both edges have weight 2 , we can transfer any of the vertices $B$ or $C$ to the set $V_{l}$. We have selected $B$. The edge $A B$ is transferred to $E_{1}$.
- Step 2: We transfer to $V_{2}$ those vertices in $V_{3}$ that are connected to $B$, which are $D$ and $H$, and to $E_{2}$ the edges $B H$ and $B D$. The distances to $A$ of these two new vertices according to the edges of $E_{2}$ are, respectively, $l_{D}=6$ and $l_{H}=7$. Hence, the vertex in $V_{2}$ with minimum distance to $A$ by using the edges of $E_{2}$ is $C\left(l_{C}=2\right)$, which is transferred to $V_{l}$. The edge $A C$ is transferred to $E_{l}$.
- Step 3: We transfer to $V_{2}$ the vertex $E$, which is the only vertex in $V_{3}$ connected to $C$. The edges $C D$ and $C E$ are transferred to $E_{2}$ and hence, the distance from $A$ to $D$ by using $E_{2}$ decreases from 6 to 5 . The vertex with minimum distance to $A$ is then $E\left(l_{E}=4.5\right)$, which is transferred to $V_{l}$. The edge $C E$ is transferred to $E_{l}$.
- Step 4: We transfer to $V_{2}$ the vertex $F$, which is the only vertex in $V_{3}$ connected to $E$. The edge $E F$ is transferred to $E_{2}$. The distance from $A$ to $F$ by using $E_{2}$ is $l_{F}=6.5$. The vertex with minimum distance to $A$ in $V_{2}$ is $D\left(l_{D}=5\right)$. It is transferred to $V_{l}$ and the edge $C D$ to $E_{1}$.
- Step 5: We transfer to $V_{2}$ the vertex $I$, which is the only vertex in $V_{3}$ connected to $D$. The edges $D I$ and $D F$ are transferred to $E_{2}$. The distance from $A$ to $I$ by using $E_{2}$ is $l_{I}=7$. The vertex with minimum distance to $A$ in $V_{2}$ is $F\left(l_{F}=6.5\right)$. It is transferred to $V_{l}$ and the edge $D F$ to $E_{1}$.
- Step 6: The vertex $G$ is transferred to $V_{2}$ and the edge $F G$ to $E_{2}$. It is $l_{G}=9.5$. The minimum distance to $A$ in $V_{2}$ is $l_{H}=l_{I}=7$. We transfer to $V_{I}$ the final vertex $I$ and the edge $D I$ to $E_{1}$. The algorithm finishes here and the shortest path is formed by the edges $A C, C D$ and $D I$, with total length 7 .
- Solution: Once the final vertex $I$ is reached, the shortest path is uniquely determined by the auxiliary list $L$, which is lexicographically ordered. In our case, it can be observed in this list that $I$ is reached from $D, D$ from $C$ and $C$ from $A$.


Step 0:
$V_{2}=\varnothing$
$L=\{0,0,0,0,0,0,0,0,0\}$


Step 3:


Step 1:
$V_{2}=\{(\mathrm{C}, 2)\}$
$L=\{0, A, 0,0,0,0,0,0,0\}$


Step 4:
$V_{2}=\{(\mathrm{F}, 6.5),(\mathrm{H}, 7)\}$
$L=\{0, A, A, C, C, 0,0,0,0\}$


Step 2:
$V_{2}=\{(\mathrm{D}, 6),(\mathrm{H}, 7)\}$
$L=\{0, A, A, 0,0,0,0,0,0\}$


Step 5:
$V_{2}=\{(\mathrm{H}, 7),(\mathrm{I}, 7)\}$
$L=\{0, A, A, C, C, E, 0,0,0\}$


Shortest path

$$
\begin{gathered}
V_{2}=\{(\mathrm{G}, 9.5),(\mathrm{H}, 7)\} \\
L=\{0, A, A, C, C, E, 0,0, D\}
\end{gathered}
$$

Figure 8: Dijkstra's algorithm.

The Dijkstra's algorithm can be implemented in GeoGebra by making use of Javascript. Previously, the vertices of our weighted graph $G$ have to be ordered and its adjacency matrix defined, that is, the $n x n$ binary matrix $M=\left(m_{i j}\right)$ such that, if there exists an edge between the vertices $i$ and $j$ (from the vertex $i$ to the vertex $j$ if the graph is directed), then $m_{i j}$ coincides with the weight of such an edge. Otherwise, it is $m_{i j}=0$. The adjacency matrix of a directed graph is, therefore, symmetric, but it is not true in general if the graph is undirected.

The specific construction in GeoGebra is as follows: Let us suppose that we are interested in a directed graph of six vertices and adjacency matrix

$$
M=\left(\begin{array}{llllll}
0 & 1 & 2 & 0 & 4 & 0 \\
0 & 0 & 0 & 1 & 1 & 1 \\
1 & 0 & 0 & 2 & 1 & 0 \\
0 & 2 & 0 & 0 & 1 & 3 \\
1 & 0 & 0 & 2 & 0 & 1 \\
1 & 0 & 1 & 0 & 1 & 0
\end{array}\right)
$$

In order to draw this graph in GeoGebra, we create six points, $A, B, C$, $D, E$ and $F$, in the graphics view of GeoGebra and we enter in the input bar the next six sentences:

$$
\begin{aligned}
V= & \{A, B, C, D, E, F\} \\
& n=\text { Length }[V]
\end{aligned}
$$

$$
M=\{0,1,2,0,4,0,0,0,0,1,1,1,1,0,0,2,1,0,0,2,0,0,1,3,1,0,0,2,0,1,1,0,1,0,1,0\}
$$

Edges=Sequence[Sequence[If[Element[M, $(i-1) n+j]>0$, Vector $[$
Element [V, i], Element $[V, j]]], j, 1, n], i, 1, n]$

$$
\begin{gathered}
\text { Initial }=1 \\
\text { Final }=1
\end{gathered}
$$

The last two sentences will refer to the position in the list $V$ of the initial and final vertices of our path. In order to design an interactive template, we create two input boxes in the graphics view that are respective related to these two vertices (see Figure 9).


Figure 9: Directed graph in GeoGebra.

The next step consists of implementing the Dijkstra's algorithm in GeoGebra. To this end, we enter in the JavaScript Global tab, the next code in JavaScript:

```
function distance(){
var i, d, m,v, a,a0;
var s=0;
var n = ggbApplet.getValue("n");
var D = new Array();
var NM = new Array();
var P = new Array();
for(i=0; i<n*n; i++){
    D[i] = 100;}
for(a0 = 1;a0< n+1;a0++){
    for(i=0;i<n;i++){
        NM[i]=0;
        P[i]=-1;
        D[n*n+(a0-1)*n+i]=-1;}
    a=a0;
    D[(a0-1)*n+a-1]=0;
    NM[a-1]=1;
    while(a!=0){
        for(i=0;i<n;i++){
            m=ggbApplet.getListValue("M",(a-1)*n+i+1);
            if (NM[i]==0 & m!=0 & D[(a0-1)*n+i]>D[(a0-1)*n+a-1]+m){
                D[(a0-1)*n+i]=D[(a0-1)*n+a-1]+m;
                P[i]=a;
                D[n*n+(a0-1)*n+i]=a;}}
        d=100;
        for(i=0;i<n;i++){
            if (NM[i]==0){
                if (s==0){
                    s=i;
                    d=D[(a0-1)*n+i];}
                else{
                    if (D[(a0-1)*n+i]<d){
                        d=D[(a0-1)*n+i];
                        s=i;}}}}
        if (d==100){
            v=0;}
        else{
            v=s;}
        if (v==0){
            a=0;;
        else{
            NM[v]=1;
            a=v+1;}}}
        return(D);}
```

The output of this function is an array $D$ of cardinality $2 n^{2}$, such that its $n^{2}$ first elements determine the distances among the vertices of the graph. These first elements are initialized to 100 , which would correspond to the maximum possible weight of the graph in question. Depending on the graph, this initial value can conveniently be increased. Further, the $n^{2}$ last elements of the array $D$ determine the list of previous vertices in any shortest path from a given initial vertex.

Since $D$ is not yet an explicit object in GeoGebra, we enter the next code in JavaScript in the On Update tab of the Scripting properties of the numbers Initial and Final:
ggbApplet.evalCommand(" $d=\{$ "+distance() + " $\}$ ");
We can then press $F 9$ or to introduce a number in any of the two input boxes of our template to define automatically an auxiliary list $d$ with all the $2 n^{2}$ elements of the array $D$. In particular, the distance matrix of our graph can be explicitly defined by entering in the input bar the sentence

$$
\begin{gathered}
D M=\text { Sequence[Sequence[If[Element }[d,(i-1) n+j]=100, \infty, \\
\text { Element }[d,(i-1) n+j]], j, 1, n], i, 1, n]
\end{gathered}
$$

In our case, this distance matrix is

$$
D M=\left(\begin{array}{llllll}
0 & 1 & 2 & 2 & 2 & 2 \\
2 & 0 & 2 & 1 & 1 & 1 \\
1 & 4 & 0 & 2 & 1 & 2 \\
2 & 2 & 3 & 0 & 1 & 2 \\
1 & 4 & 2 & 2 & 0 & 1 \\
1 & 5 & 1 & 3 & 1 & 0
\end{array}\right)
$$

The next step is to define the auxiliary list of previous vertices in a shortest path with initial vertex that one that has been inserted in the corresponding input box of our template. To this end, we enter the next sequence in the input bar:

$$
\begin{aligned}
L= & \text { Sequence [Iff[Element }\left[d, n^{2}+(\text { Initial }-1) n+i\right] \stackrel{?}{=}-1,0, \\
& \text { Element } \left.\left.\left[d, n^{2}+(\text { Initial }-1) n+i\right]\right], i, 1, n\right]
\end{aligned}
$$

This list can be used to determine the shortest path from the initial to the final vertices introduced in the corresponding input boxes. This path is got by adding the next code in Javascript in the Global JavaScript tab:

```
function path(){
    var i,j,m;
    var ip = ggbApplet.getValue("Initial");
    var fp = ggbApplet.getValue("Final");
    var n = ggbApplet.getValue(" }n\mathrm{ ");
    var A = new Array();
    var C = new Array();
    for(i=0;i<n;i++){
```

$$
\begin{aligned}
& \text { m=ggbApplet.getListValue }(" L ", i+1) ; \\
& \text { A[ig=m;;\}} \\
& C[0]=A[f p-1] ; \\
& j=0 ; \\
& \text { for }(i=0 ; i<n-1 ; i++)\{ \\
& \text { if }(C[i]=0)\{ \\
& C[i+1]=0 ;\} \\
& \text { else }\{ \\
& \text { if }(C[i]!=i p)\{ \\
& C[i+1]=A[C[i]-1] ;\} \\
& \text { else }\{ \\
& C[i+1]=0 ;\}\}\} \\
& \text { return }(C) ;\}
\end{aligned}
$$

The output of this function is a list of numbers that determine the position in the list $V$ of all the vertices through which our shortest path has to pass before reaching the final vertex. In order to have this list as an explicit object in GeoGebra, we add the next code in JavaScript in the On Update tab of the Scripting properties of the numbers Initial and Final:
ggbApplet.evalCommand("path = $\{$ "+path()+" $\}$ ");
Finally, the shortest path is drawn in GeoGebra (see Figure 10) by entering the next sequence in the input bar:

Shortest=Union[Sequence[If[Element[path, i] Element[path, $i+1]>0$, Vector[Element[V, Element[path, $i+1$ 1]], Element[V, Element[path, i]]]], i, 1, n], \{If[Element[path, 1] > 0, Vector[Element[V, Element[path, 1]], Element[V, Final]I]\}]


Figure 10: Shortest path in GeoGebra by using the Dijkstra's algorithm.

The template that we have just constructed can be considered as the base worksheet from which we can elaborate any dynamic and interactive evacuation map in a similar way to the construction that we have done in Section 2. It is due to the fact that this template is completely parametric, not only with respect to the initial and final points of our path, but also with respect to the initial graph. Specifically, if we change the list $V$ of vertices of the new graph and the list $M$ that corresponds to the entries of its adjacency matrix, all the constructed objects are conveniently redefined. It is particularly useful in case of being required to eliminate some vertex or edge of the base graph of the evacuation map because of an emergency.

The advantage of this template with respect to that one constructed in Section 2 is that the new one facilitates the use of directed edges in the base graph of the evacuation map and also the use of any type of weight, not only constant weights or weights based on the Euclidean distance among vertices. It makes possible the implementation of our model in the design of evacuation routes of any type of building, with independence of the particular requirements compelled by the corresponding legal regulation.

## 4 Conclusions

In this paper we have exposed how to use GeoGebra in order to design a dynamic and interactive evacuation map that can be used in real time to optimize the evacuation plan of public and private buildings like schools, hospitals or hotels, amongst others. The use of the command ShortestDistance, which is implemented by defect in GeoGebra, is a good alternative to this end. Nevertheless, this command can only be used for weighted graphs labeled with constant weights or with weights based on the Euclidean distance among vertices. To deal with more general cases, we have made use of JavaScript to implement in GeoGebra the Dijkstra's algorithm. A more comprehensive study for possible implementation of our model in real buildings has to be further developed.

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