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1 **IMPACT OF THE VARIATION OF THE RECEIVER GLASS ENVELOPE**
2 **TRANSMITTANCE AS A FUNCTION OF THE INCIDENCE ANGLE IN THE**
3 **PERFORMANCE OF A LINEAR FRESNEL COLLECTOR**

4
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12 **Abstract**

13 In this paper, we focus on the variation of the transmittance of the receiver glass envelope as a
14 function of the incidence angle and we measure its impact on the annual optical efficiency of a
15 LFR plant using ray-tracing techniques. For this purpose, we draw up a detailed model of the LFR
16 collector installed on the roof of the School of Engineering of the University of Seville, Spain. We
17 also calculate the optical efficiency with and without a secondary reflector and with constant or
18 variable transmittance receiver glass envelope properties.

19 We run simulations using a clear-sky annual 1-min synthetic data set as input and calculate an
20 average annual optical efficiency using efficiency matrices and Incidence Angle Modifiers (IAM)
21 obtained from ray-tracing simulations. We find that the effect of the variation of the receiver
22 glass envelope optical properties, as a function of the incidence angle, reduces the annual optical
23 efficiency by 2.5% when the LFR plant has a basic secondary reflector and by 0.7% when there is
24 no secondary reflector, according to the results obtained when using constant optical
25 properties. We also evaluate the performance of the system with an optimised secondary
26 reflector design.

27 **Glossary**

28 LFR: Lineal Fresnel Reflector

34 I_{CS} : Solar Constant

29 IAM: Incidence Angle Modifiers

35 E_0 : Correction due to Earth-Sun distance

30 PTC: Parabolic Trough Collectors

36 °N: North

31 Θ : Incidence angle

37 °W: West

32 DNI: Direct Normal Irradiance

38 LiBr: Lithium Bromide

33 m_R : Relative Air Mass

39 P_{abs} : Power impinging on the absorber tube

- 40 η_{opt} : Optical efficiency
- 41 A_{cap} : Solar field aperture
- 42 ψ : Solar azimuth
- 43 α : Solar elevation
- 44 IAM : Incident Angle Modifier
- 45 IAM_l : Longitudinal Incident Angle Modifier
- 46 IAM_t : Transversal Incident Angle Modifier
- 47 η_o : Optical efficiency when the sun is at the
- 48 zenith
- 49 τ : Transmissivity
- 50 E_{rec} : Total energy impinging the receiver
- 51 DNI_{CSY} : Clear sky DNI
- 52 $\eta_{opt\,average}$: Annual average optical
- 53 efficiency

54 **Keywords**

55 Linear Fresnel, Optical properties, Ray tracing.

56 **1 Introduction**

57 A Linear Fresnel Reflector (LFR) is a solar collector that reflects the sun rays onto a fixed linear
 58 receiver that stands along and above the reflectors. It uses long, flat or slightly curved mirrors
 59 to reflect the sunlight. The LFR is a promising technology and an attractive option because of its
 60 simplicity and its relatively low construction cost [1]. Usually, Fresnel solar collectors are
 61 compared with Parabolic Trough Collectors (PTC) for medium temperature applications. Many
 62 researchers state the advantages of using the LFR over the PTC [2-5], identifying the elimination
 63 of the problems derived from the movement of the receiver [6] and the reduction on the
 64 operation and maintenance costs [7] as the most significant advantages. However, the optical
 65 efficiency of the LFR is lower than the optical efficiency of the PTC [8].

66 LFR collectors provide thermal energy in the medium temperature range (100-300 °C), making
 67 it a promising technology in fulfilling the demand of the majority of industrial processes [9].
 68 Other applications of thermal energy in the medium temperature range are electricity
 69 production [10], solar cooling [11] and solar desalination [12].

70 In recent years, some studies related to the optimisation of the optical, thermal and geometrical
 71 parameters of different LFR configurations have been carried out [13-14]. Optical optimisation
 72 can be performed using analytical methods [15], integral methods, nonimaging optics
 73 techniques [16] and especially Monte Carlo-based ray-tracing techniques that provide great
 74 accuracy and flexibility [17-18].

75 Ray-tracing methods are widely used to analyse and optimise the geometrical performance of
 76 LFR. Zhu evaluates the impact of adjusting the tilt of the collector according to the solar elevation
 77 angle [19] and designs a stretched parabolic linear Fresnel reflector [20] using Tracepro ray-
 78 tracing software [21]. Pulido-Iparraguirre et al. [22] develop a ray-tracing code to optimise the
 79 solar collector size, tilt and orientation, and the receiver design. However, none of the methods
 80 used consider the impact of the variation of the optical properties such as the reflectance and
 81 transmittance of the receiver glass envelope as a function of the incidence angle (θ). It is
 82 common practice to adopt a constant value of reflectance and transmittance, but this

83 assumption may lead to significant errors in the estimation of the optical efficiency of a LFR
84 system.

85 In this research paper, we use Tonatiuh, an open source ray-tracing code specifically developed
86 for the optical simulation of solar concentrators [23], to evaluate the impact of the angular
87 dependence of the receiver glass envelope transmittance in a LFR plant. To that end, we model
88 a real plant [24] installed on the roof of the School of Engineering of the University of Seville
89 (Spain) and we run several ray-tracing simulations with constant and variable optical properties.
90 We use a clear-sky DNI annual set and the average optical efficiency as a weighting factor for
91 the location of Seville as a performance indicator. This research justifies the importance of using
92 efficiency matrices and variable optical properties of the receiver glass envelope when
93 simulating the performance of LFR plants.

94 This paper is structured as follows: section 2 presents the solar irradiation data used for the
95 calculations, details the modelled LFR plant and describes the simulations. Section 3 shows the
96 main results in terms of the optical efficiency on a monthly and annual basis, and a comparison
97 with an improved secondary reflector design. Conclusions are then presented in Section 4.

98 **2 Data and Methodology**

99 This section includes the data used and the steps followed for simulating the optical
100 performance of the modelled LFR plant.

101 **2.1 Meteorological data**

102 In this study, we use an annual set of clear-sky 1-min Direct Normal Irradiation (DNI) data. We
103 perform an envelope method which is widely used for the estimation of the direct fraction index
104 [25]. Any of the well-known clear-sky DNI models could be used; in this case, we use the A-B
105 clear-sky model.

$$106 \quad I_{bn_{cs}} = I_{CS} \cdot E_0 \cdot \frac{A}{1 + B \cdot m_R} \quad , \quad (1)$$

107 where m_R is the relative air mass I_{CS} is the solar constant, E_0 the correction due to Earth-Sun
108 distance and A and B are empirical parameters intended to model the state of transparency or
109 turbidity of the atmosphere. We calculate the A and B parameters by using an empirical fit from
110 fourteen years of DNI measurements at the location of Seville (Spain) [26]. In Table 1 we present
111 the main climatic characteristics of the selected location and the estimated couple of
112 parameters defining the clear-sky envelope.

113 **Table 1.** Main climatic characteristics and couple of parameters defining the clear-sky envelope
114 estimated for the location of Seville

Location	Latitude (°N)	Longitude (°W)	Altitude (m)	Climate	A	B
Seville	37.4	6	12	Mediterranean	0.862	0.136

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2.2 Plant description

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The LFR plant is a real hybrid solar cooling plant, which was installed in 2008 at the School of Engineering of the University of Seville in partnership with Gas Natural (Spanish natural gas and electrical energy utilities company) as a long-term project to boost the integration of both natural gas and solar energy in refrigeration applications (Fig. 1) [15]. The solar plant is coupled with a double effect LiBr + water absorption chiller with an auxiliary gas burner.

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122 **Fig. 1.** General view of the modelled plant

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The solar field longitudinal axis has a deviation of 12.05° with respect to the East-West direction and a total collector area of 352 m^2 . It has 11 rows separated by a spacing of 20 cm, with 16 mirrors, $4 \times 0.5 \text{ m}^2$ each, per row, and the total number of mirrors is 176. Each row is equipped with a solar tracking system.

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The length of the solar field, as well as the receiver, is 64 m. The mirrors, with curvature radii between 8.6 and 10.6 m, have a nominal specular reflectance of 0.92. The receiver, a SCHOTT PTR[®] 70, is placed 4 m above the mirror plane. It is composed of a steel tube with a nominal absorptance of 0.94 and a glass envelope with a nominal transmittance of 0.96¹. The secondary reflector is a thin metal parabola with a nominal reflectance of 0.77. We model the optical errors of the reflecting surfaces assuming a normal distribution with a standard deviation of 3.38 mrad. The working fluid is slightly subcooled liquid water at a nominal operating temperature of 180°C and a pressure of 13 bar.

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The main characteristics of the solar field and the receiver are presented in Table 2. The main optical parameters of the solar facility are presented in Table 3.

136

137 **Table 2.** Main dimensional characteristics of the modelled LFR plant

Characteristic	Value	Unit
Solar field aperture	352	m^2

¹ This value is used in simulations with constant optical properties. In the case of simulations with variable optical properties, we use a value dependent on the incidence angle of the ray to the tube (Fig.3).

Solar field length	64	m
Orientation	East–West (approx.)	-
Number of rows	11	-
Mirror dimension	4 x 0.5	m ²
Mirror reflectance	0.92	-
Mirror curvature	8.6-10.6	m
Receiver length	64	m
Height of the receiver	4	m
Receiver model	SCHOTT PTR©70	-

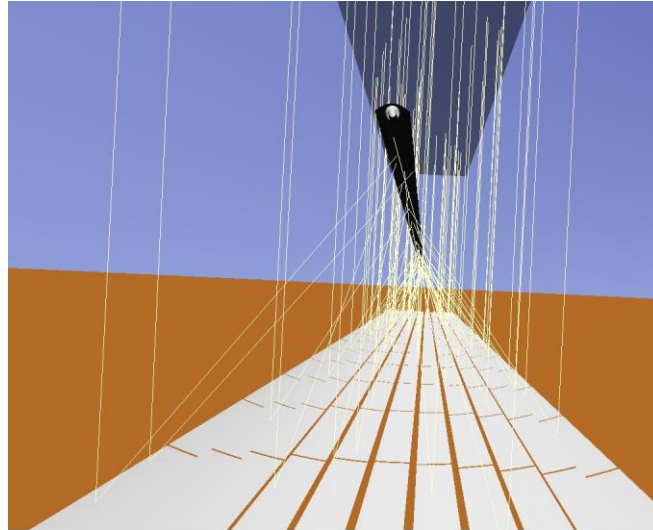
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139 **Table 3.** Main optical characteristics of the modelled LFR plant

Characteristic	Value	Unit
Solar field mirror reflectance	0.92	-
Secondary reflector reflectance	0.77	-
Absorber tube absorptance	0.94	-
Receiver glass tube transmittance	0.96 ¹	-
Solar field sigma slope	3.38	mrad

140 **2.3 Ray-tracing model**

141 We run several ray-tracing simulations of the LFR collector using the Tonatiuh code [27]. This
142 Monte Carlo-based ray-tracing program for the optical simulation of solar concentrators has
143 been experimentally validated in different plants [28-29]. In Tonatiuh, the rays are randomly
144 thrown from a focus emulating the sun disk, and then are reflected, absorbed or refracted,
145 depending on the optical characteristics of the elements of the system. Tonatiuh has an object-
146 oriented graphical interface providing an extensive palette of surfaces. The geometry of the
147 simulated system can be built up from a combination of simple elements defined by their
148 geometrical and optical properties. Fig.2 shows the modelled plant seen through the Tonatiuh
149 interface in the simulation for several stochastically distributed rays.



150

151 **Fig. 2.** Layout of the modelled LFR plant, seen through the Tonatiuh interface

152 The transmittance of the receiver glass envelope and the absorptance of the absorber tube are
153 incidence angle dependent, although they are generally modelled as constant values. We can
154 theoretically calculate the variation of the glass envelope transmittance as a function of the
155 incidence angle following Snell's law and Fresnel equations. As can be observed in

156 **Fig. 3.** Theoretical values of transmittance and reflectance of the receiver glass envelope as a
157 function of the incidence angle.

158 , the theoretical results show that the transmittance and reflectance remain almost constant for
159 solar incidence angles lower than 60° but drop drastically for incidence angles between 60° and
160 90° . We have considered a Buie sunshape [30] with a nominal value of 1000 W/m^2 and a
161 circumsolar ratio of 2% for modelling purposes.

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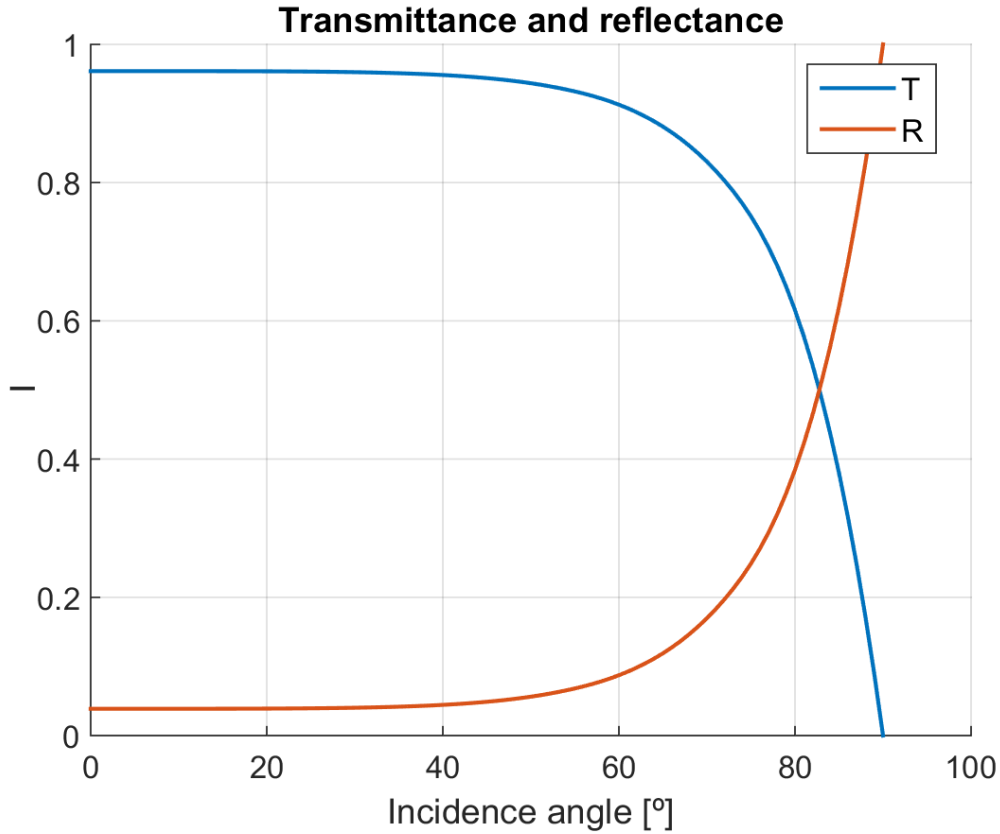
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169 **Fig. 3.** Theoretical values of transmittance and reflectance of the receiver glass envelope as a
 170 function of the incidence angle.

171 From the simulations, we obtain the power impinging on the absorber tube², P_{abs} . The optical
 172 efficiency of the solar plant can be calculated as the ratio of P_{abs} to the available power on the
 173 solar field (primary):

$$174 \quad \eta_{opt} = \frac{P_{abs}}{DNI \cdot A_{cap}} \quad , \quad (2)$$

175 Where DNI is the direct normal irradiance and A_{cap} is the solar field aperture (352 m²).

176 In this study, we use two different methods to describe the dependence of the optical efficiency
 177 on the sun's position. In the first method, the simulations cover the range of all possible solar
 178 positions, defined by the solar azimuth (ψ) and elevation (α) angles to obtain an optical
 179 efficiency matrix (see in **Fig. 7**). The second method is based on the concept of Incident Angle
 180 Modifier, IAM . The IAM is a practical and faster method to obtain the optical efficiency. The
 181 longitudinal IAM (IAM_l) is calculated by simulating the plant when the transverse angle is null,
 182 and the transverse IAM (IAM_t) is calculated by simulating the plant when the longitudinal angle
 183 is null. The optical efficiency can then be calculated for any solar position as:

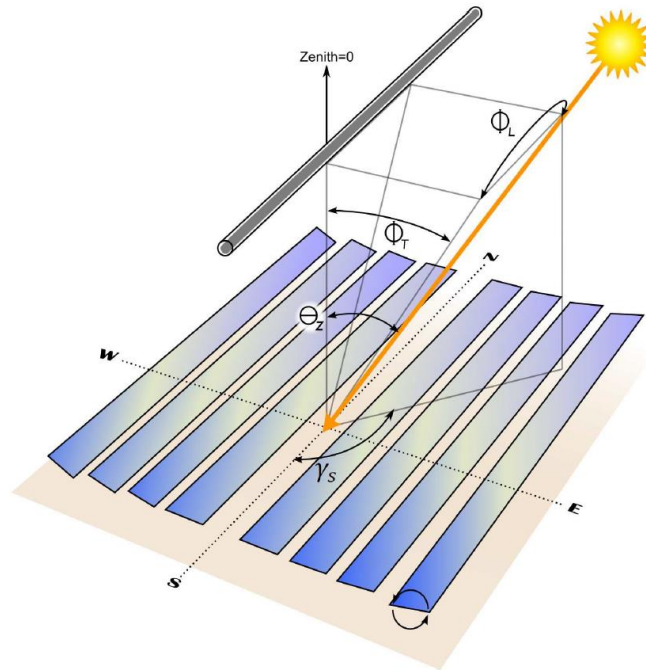
$$184 \quad \eta_{opt_{FIELD}} = \eta_o * IAM_l * IAM_t \quad . \quad (3)$$

² The optical properties of the absorber tube are also angular-dependent, but we have not considered this effect in our study. Therefore P_{abs} does not include the absorptance of the absorber tube.

185 Where η_o is the optical efficiency when the sun is at the zenith angle.

186 In Fig. 4, we present an illustration of the solar-position-dependent collector at longitudinal and
 187 transversal angles [31].

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189

190 **Fig. 4.** Simple diagram of the solar-position-dependent collector at longitudinal and transversal
 191 angles [31].

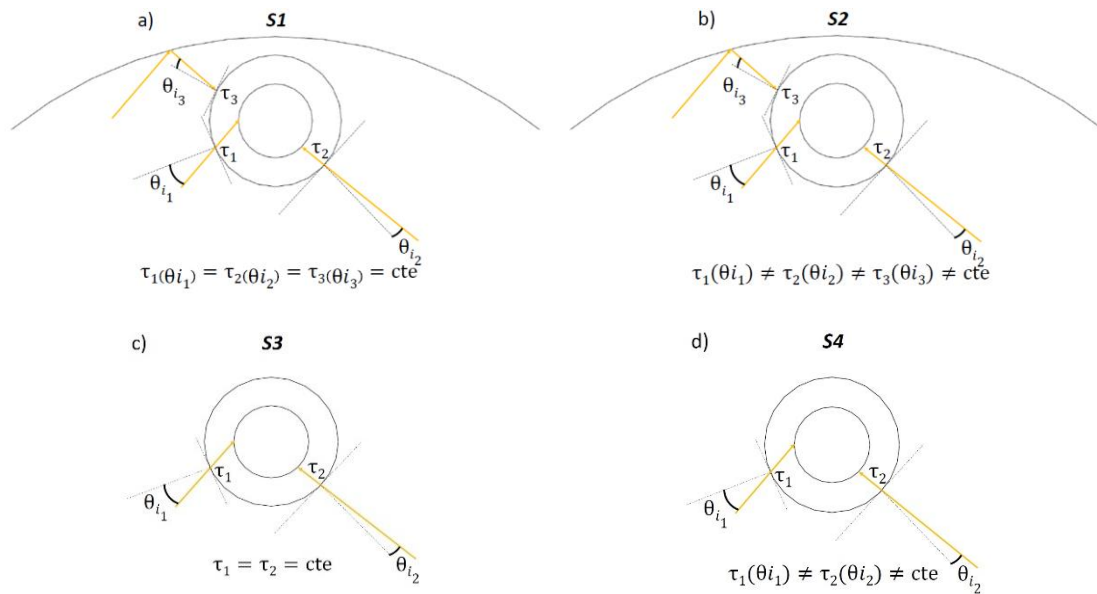
192 **3 Results**

193 We run two different sets of simulations: one which takes into account a constant value of the
 194 receiver transmittance of 0.96 and another using an incidence angle-dependent transmittance
 195 value as shown in Fig.3. We also run simulations of the solar field including or removing the
 196 secondary reflector, leading to the four cases summarised in Table 4 and illustrated in Fig. 5.

197 **Table 4.** LFR simulations taken into account in this research

LFC simulations			
With secondary reflector		Without secondary reflector	
Constant receiver transmittance	Variable receiver transmittance	Constant receiver transmittance	Variable receiver transmittance
S1	S2	S3	S4

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Fig. 5. Illustration of the LFR simulations modelled in this research.

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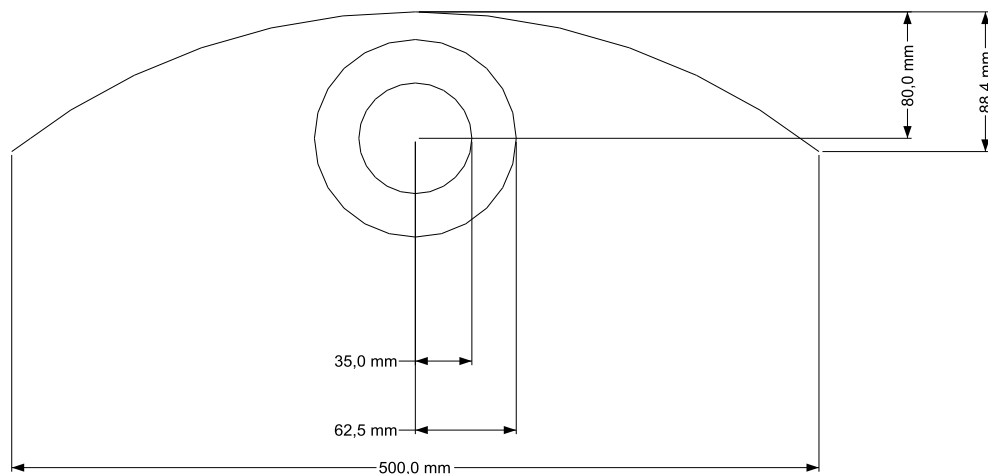
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S1 is the system with the secondary reflector and a constant value of the receiver transmittance. S2 is the system with the secondary reflector and considering an incidence angle-dependent transmittance value on the receiver. S3 is the system without the secondary reflector and a constant value of the receiver transmittance. S4 is the system without the secondary reflector and considering an incidence angle-dependent transmittance value on the receiver. The modelled secondary reflector is a perfect parabola with a width of 0.5 m and a focal length of 0.0884 m. The distance between the parabola vertex and the focal point is 0.08m. The inlet and outlet radii are 0.035 m and 0.0625 m respectively (Fig. 6).



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Fig. 6. Illustration of the modelled secondary reflector and receiver.

212

3.1 Annual optical efficiency

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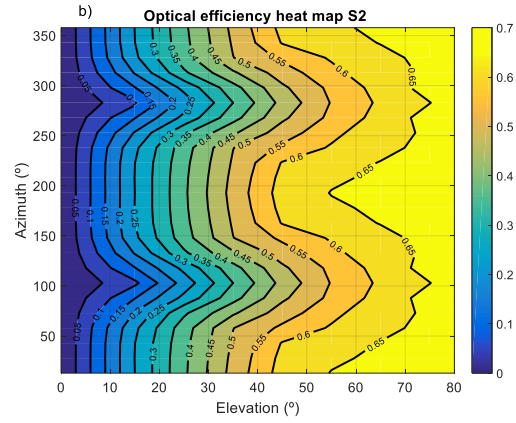
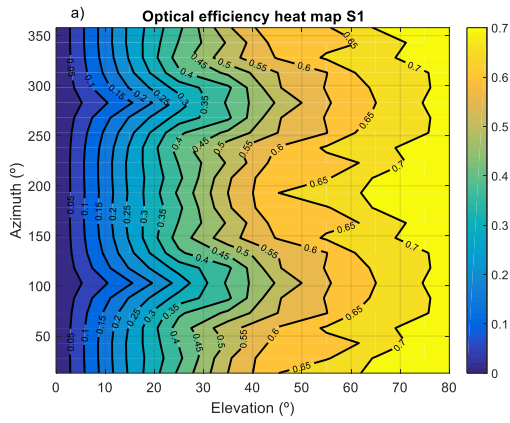
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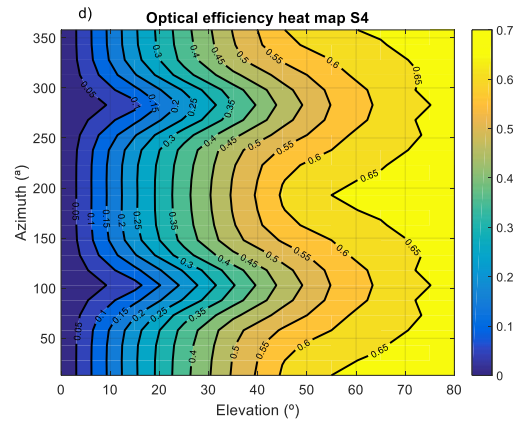
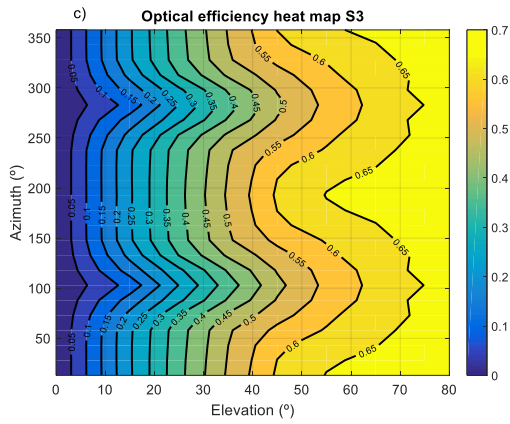
We calculate the optical efficiency for a number of solar positions defined by the solar azimuth and elevation angles, obtaining the efficiency matrix and the IAM profiles. In Fig. 7 and 8, we present the optical efficiency matrices as heat maps and the IAM curves for the four evaluated

216 cases. The solar azimuth value of 90° corresponds to the East and 180° corresponds to the South.
217 A solar elevation of 90° indicates that the sun is at the zenith angle.

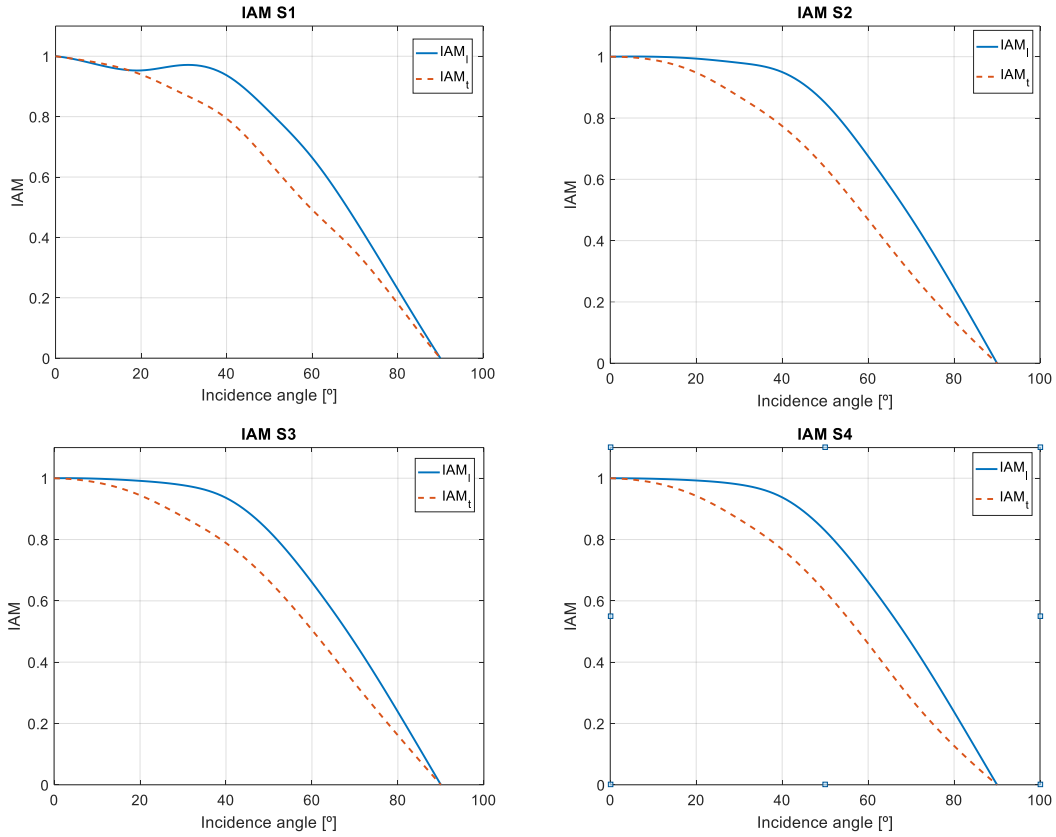
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219



220 **Fig. 7.** Optical efficiency matrices presented as heat maps depending on the solar azimuth and
221 elevation angles for the four evaluated cases.



222

223

224 **Fig. 8.** Estimated IAM profiles for the four evaluated cases.

225 We then calculate the solar position for the location under study (Seville) in 1-min resolution for
 226 the entire year, and an optical efficiency value (η_{opt}) is assigned to each instant (i) from the
 227 efficiency matrix or the IAM profiles. The average optical efficiency is calculated as the quotient
 228 of the total energy impinging on the receiver (E_{rec}) to the total energy available in the solar field
 229 (E_{sf}). For a clear-sky year:

$$230 \quad E_{rec} = \sum_{i=1}^n \left(\eta_{opt_i} \cdot DNI_{CSY_i} \cdot A_{cap} \right) , \quad (4)$$

$$231 \quad E_{sf} = \sum_{i=1}^n \left(DNI_{CSY_i} \cdot A_{cap} \right) , \quad (5)$$

232 Where DNI_{CSY} is the clear-sky DNI and i is the time of the year in minutes ($n=525600$ for one
 233 year in the 1-min resolution).

$$234 \quad \eta_{opt_{average}} = \frac{E_{rec}}{E_{sf}} . \quad (6)$$

235 We calculate the annual average optical efficiency ($\eta_{opt_{average}}$) using the estimated efficiency
 236 matrices and the IAM profiles. The results for the annual optical efficiency obtained for the 4
 237 cases considered are summarised in Table 5.

238 **Table 5.** Annual optical efficiency of the four evaluated cases calculated with the efficiency
 239 matrix and IAM methods.

	Annual optical efficiency ($\eta_{opt\ average}$) [%]			
	With secondary concentrator		Without secondary concentrator	
	S1 $\tau=cte$	S2 $\tau= \tau(\theta)$	S3 $\tau=cte$	S4 $\tau= \tau(\theta)$
Efficiency matrix method	44.95	41.76	42.36	40.20
IAM method	42.40	39.29	39.91	38.58

240

241 The IAM method results in lower optical annual efficiency compared to the efficiency matrix
 242 method (\approx -2.5%) for all the cases.

243 The use of a secondary concentrator implies an annual optical efficiency increase of 3.2% when
 244 taking into account constant receiver properties (S2 to S1) and 1.2% when taking into account
 245 the variation of the receiver properties (S4 to S3).

246 The impact of the use of variable optical properties of the receiver in the optical performance
 247 of the modelled systems is greater for the system with a secondary concentrator. The annual
 248 average optical efficiency decreases by approximately 2.5% from S1 to S3 and by 0.7% from S2
 249 to S4.

250 These results suggest that a significant number of rays reflected on the secondary reflector
 251 impinge on the receiver glass envelope with a high incidence angle. We have calculated the
 252 distribution of the energy on the receiver discretizing into three intervals depending on the
 253 incidence angle ($\theta \leq 30^\circ$; $30^\circ < \theta \leq 60^\circ$; $60^\circ < \theta \leq 90^\circ$). Calculations have been carried out for systems
 254 with variable optical properties, with and without a secondary reflector (S2 and S4 respectively).
 255 Results are summarised in Table 6.

256 **Table 6.** Distribution of the energy on the receiver depending on the incidence angle for cases
 257 S2 and S4.

	Energy on the receiver (%)		
	$\theta \leq 30^\circ$	$30^\circ < \theta \leq 60^\circ$	$60^\circ < \theta \leq 90^\circ$
S2	31.1	52.1	16.8
S4	31.5	51.9	16.6

258

259 In the case of the system with a secondary reflector, there is more energy on the receiver for
 260 large incidence angles and less energy for incidence angles lower than 30° .

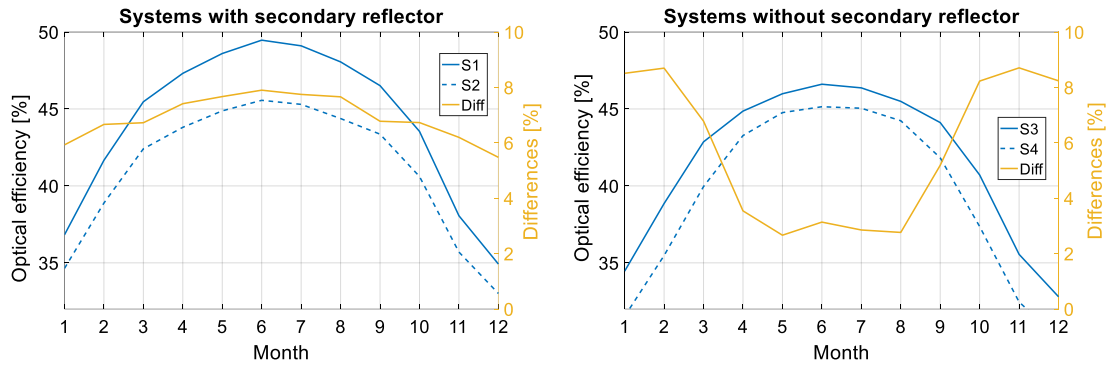
261 3.2 Monthly optical efficiency

262 In the following, we will use the efficiency matrices for the calculations. We have calculated the
 263 average optical efficiency per month for the four evaluated cases. In Fig 9. We present the
 264 monthly optical efficiency for the constant properties (continuous blue line) and variable

265 properties (dotted blue line) cases with a secondary reflector (left) and without a secondary
 266 reflector (right). In the secondary y-axes, we present the percentage differences calculated
 267 according to equations 6 and 7 (yellow lines).

$$268 \quad Differences_{S1-S2} (\%) = \frac{S1 - S2}{S1} \cdot 100 \quad (6)$$

$$269 \quad Differences_{S3-S4} (\%) = \frac{S3 - S4}{S3} \cdot 100 \quad (7)$$



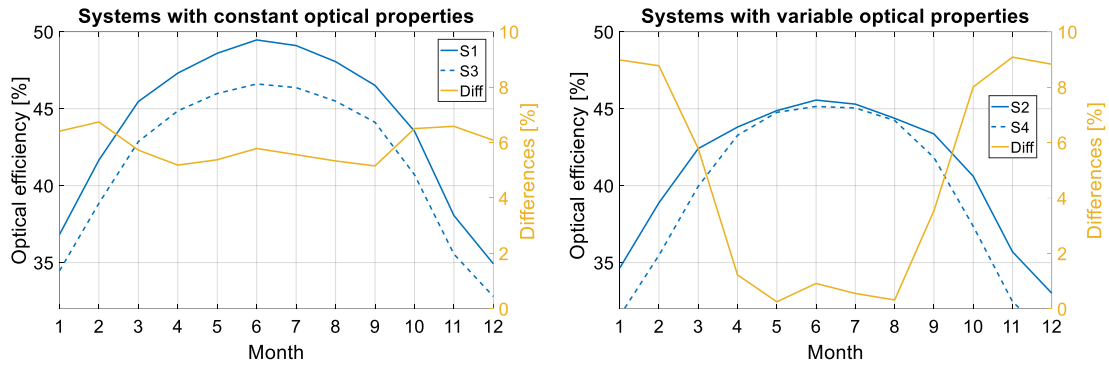
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271 **Fig. 9.** Monthly optical efficiency of the four evaluated cases calculated with the efficiency
 272 matrices and differences found between constant and variable receiver glass envelope
 273 properties. Systems with a secondary reflector are presented on the left and those without it on
 274 the right.

275 When evaluating the monthly efficiency of the system with a secondary reflector (Fig 9. Left),
 276 we can observe that the differences found due to considering the constant or variable optical
 277 properties of the receiver glass envelope are greater in summer months reaching a maximum of
 278 7.9% in June, when the solar elevation angles are higher. It should be noted that days are longer
 279 in the summer months in Seville. Hence, for the annual clear-sky DNI data set, most of the annual
 280 solar radiation is obtained in this period, coinciding with the greater differences in the optical
 281 efficiency. The average optical efficiency depends on the instantaneous optical efficiency as a
 282 weighting factor in the DNI, which in our case is the clear-sky DNI. In summer months, we find
 283 situations where we have a high solar radiation value with a low incidence angle more frequently
 284 than in winter. In the case of not using the secondary reflector (Fig 9. Right), differences are
 285 much lower for all the months, reaching a maximum of 3.4% in August. We also compare S1 to
 286 S3 and S2 to S4 for monthly efficiencies. In Fig 10 we present the monthly optical efficiency and
 287 their percentage differences calculated from equations 8 and 9 (yellow lines).

$$288 \quad Differences_{S1-S3} (\%) = \frac{S1 - S3}{S1} \cdot 100 \quad (8)$$

$$289 \quad Differences_{S2-S4} (\%) = \frac{S2 - S4}{S2} \cdot 100 \quad (9)$$



290

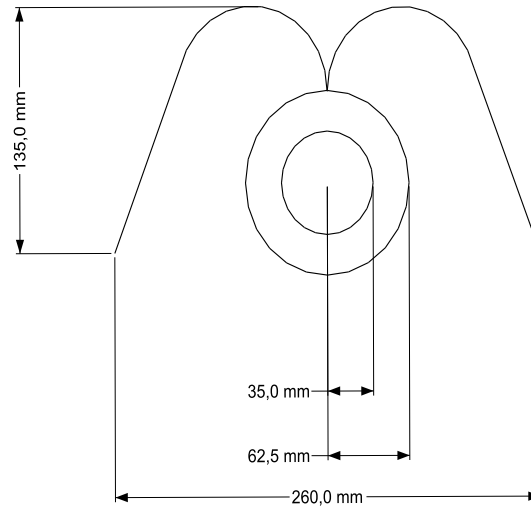
291 **Fig. 10.** Monthly optical efficiency of the four evaluated cases calculated with the efficiency
 292 matrix together with the differences found between them. Systems with constant optical
 293 properties are presented on the left and those with variable properties are on the right.

294 The monthly efficiency values are significantly lower in S3 than in S1 for all the months, but we
 295 find negligible differences between S4 and S2 in summer months, indicating a low contribution
 296 of the modelled secondary reflector in the energy obtained in the receiver when considering the
 297 variable transmittance of the receiver glass envelope.

298 **4 Discussion**

299 The main function of the secondary concentrator is to redirect rays that do not hit the receiver
 300 by increasing the number of rays that strike the receiver and therefore increasing the radiant
 301 energy impinging on it. Most of the rays reflected on the secondary concentrator hit the receiver
 302 with a high incidence angle ($\geq 60^\circ$) leading to low transmittance values, which implies a lower
 303 flux on the receiver. In the case of not using a secondary reflector, all the rays come from the
 304 solar field. In these cases, the incidence angles are generally low ($\leq 60^\circ$) and the receiver glass
 305 envelope transmittance almost reaches its maximum value.

306 Results suggest that the contribution of the installed secondary reflector is small when
 307 evaluating the modelled LFR plant with variable optical properties because the rays reflected on
 308 it impact the receiver glass envelope with large incidence angles, where the transmittance of
 309 the receiver glass envelope drops drastically. A number of authors have proposed alternative
 310 shapes of secondary reflectors in order to enhance the efficiency of LFR collectors [32]. The most
 311 promising secondary reflector design involves joining two sections of identical parabolas at the
 312 optical axis of the concentrator [33]. The dimensions of the two halves of the reflector are
 313 calculated using the radius of the absorber tube and the acceptance angle of the field. In Figure
 314 11, we present the improved design of the secondary reflector for the modelled LFR plant.



315

316 **Fig. 11.** Illustration of the improved secondary reflector together with the receiver.

317 We model the LFR plant including the improved secondary reflector (Fig. 11) instead of the basic
 318 secondary reflector (Fig. 6). We calculate the annual efficiency using the efficiency matrix
 319 method and taking into account constant optical properties of the receiver glass envelope (S5)
 320 or variable optical properties of the receiver glass envelope as a function of the incidence angle
 321 (S6). Results are summarised in Table 7

322 **Table 7.** Annual optical efficiency of the systems with the optimal secondary reflector, calculated
 323 using the efficiency matrix method.

	Annual optical efficiency ($\eta_{opt\ average}$) [%]	
	S5	S6
Efficiency matrix method	45.82	45.31

324

325 There is a decrease of 0.5% from S5 to S6, that is, from constant to variable optical properties.
 326 The impact of the variation of the glass envelope transmittance as a function of the incidence
 327 angle when evaluating the improved secondary reflector design (Fig 11) is much lower than in
 328 the case of the basic design (Fig 6). We have also calculated the distribution of the energy on
 329 the receiver by discretizing into three intervals according to the incidence angle. In Table 8, we
 330 present the distribution of the energy on the receiver for the case of S6. Results are compared
 331 to case S2.

332 **Table 8.** Distribution of energy on the receiver depending on the incidence angle. Comparison
 333 of cases S6 and S2.

	Energy on the receiver (%)		
	$\theta \leq 30^\circ$	$30^\circ < \theta \leq 60^\circ$	$60^\circ < \theta \leq 90^\circ$
S6	33.5	53.1	13.4
S2	31.1	52.1	16.8

334

335 There is a significant drop of energy (-20%) impinging on the receiver for high incidence angles
336 ($60^\circ < \theta \leq 90^\circ$), while for low incidence angles ($\theta \leq 30^\circ$) there is a significant increase of energy
337 (7.7%) impinging on the receiver.

338 **5 Conclusions**

339 To assess the effect of the incidence angle dependence of the receiver glass envelope
340 transmittance on the performance of LFRs, we evaluated the optical performance of a LFR plant
341 installed on the roof of the School of Engineering of the University of Seville using ray-tracing
342 techniques. We have modelled the LFR plant in Tonatiuh and calculated the monthly and annual
343 optical efficiency. Calculations have been performed considering constant and variable optical
344 properties of the absorber tube glass envelope (transmittance and reflectance) as a function of
345 the incidence angle. We have also estimated the optical efficiency of the LFR collector by
346 removing the secondary collector and including an alternative improved shape of the secondary
347 reflector. In light of the results, we can conclude that taking into account constant optical
348 parameters of the absorber tube leads to significant overestimations of the energy produced by
349 a LFR plant. The results of this study suggest that the optical efficiency estimations of LFR plants
350 should be performed taking into account variable properties of the absorber tube glass
351 envelope, mainly for LFR plants with basic secondary reflectors because most of the rays
352 reflected by the secondary reflector impinge on the absorber tube with high incidence angles.
353 When evaluating an improved secondary reflector design, the incidence angle dependence is
354 less significant. In any case, the evaluation of secondary reflector designs should always be
355 performed considering variable optical properties of the absorber tube glass envelope as a
356 function of the incidence angle.

357 We have calculated the average optical efficiency using efficiency matrices and IAM methods,
358 and we have found that the efficiency matrices method is a more accurate method than the IAM
359 method for the optical efficiency calculation of a LFR plant. The IAM method implies an
360 underestimation of the annual optical efficiency, which can be quantified as a reduction of 2.5%
361 (from 42.5% to 40% on average in all the evaluated systems).

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