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UNIVERSIDAD DE SEVILLA
 DEPARTAMENTO DE MATEMÁTICA
 Facultad de Ciencias Exactas
 al folio 237 de 48 del libro
 correspondiente a la asignatura de
 Sevilla

LBS 1004766

Enseña de Licenciado de Física

steua. Laffite

Sobre las componentes irreducibles de la variedad de
 leyes de álgebra de Lie nilpotentes complejas de
 dimensión 8

APÉNDICE

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El doctorando:

G. Valeiras

Fdo: Gerardo Valeiras Reina

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Introducción

Este apéndice consiste en una selección de las salidas impresas \TeX que genera el programa.

Al enseñar estas salidas se pretende:

- Mostrar la naturaleza, magnitud y complejidad de los cálculos que intervienen en los desarrollos realizados en el trabajo.
- Dar una idea de qué es lo que se omite en el capítulo 3 de la Tesis. Lo normal es que entre una afirmación como

‘entonces ... y de aquí ...’

y lo que le sigue, haya varias decenas de páginas como las aquí mostradas, además de otras muchas elaboraciones, unas con ordenador y otras con lápiz y papel.

Evidentemente este apéndice no está orientado a ser leído, excepto lo necesario para ilustrar estos aspectos del trabajo, y qué es lo que se ha omitido en su exposición. Por esto, hemos realizado una selección para que el volumen fuera razonable.

También queremos indicar que hemos evitado la impresión de expresiones excesivamente grandes (no tiene sentido, pues no van a ser interpretadas hasta que no se simplifiquen). Estas aparecen como *‘demasiado grande’* en los listados, y casi siempre son varias páginas para un solo polinomio en muchas variables. Por ejemplo, algunas no tan grandes pueden verse en la etapa 1 de la sucesión característica $(5, 2, 1)$, página 6.

Debemos resaltar que estas salidas impresas fueron una ayuda considerable, sobre todo por hacer posible su posterior interpretación. Sin embargo no son las que mejor muestran el discurso lógico que conduce a la obtención de las componentes irreducibles.

De hecho, deben ser consideradas como *altos en el camino*, en los que se le pide al sistema que escriba un resumen del estado de la computación.

En realidad el trabajo se hace casi todo de forma interactiva con el sistema **Mathematica** utilizando lo que allí se llaman *Notebooks*, que permiten 'dialogar' con el ordenador y pedirle que realice lo que en cada momento parezca más conveniente. Para apreciar la capacidad de estos *Notebooks* no sirven papeles impresos, sino que es necesario verlos en acción.

Sucesión característica (6,1,1)

Etapa 1

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_4] = a_3 X_3$$

$$[X_2, X_5] = a_3 X_4 + a_5 X_3$$

$$[X_2, X_6] = a_3 X_5 + a_5 X_4 + a_7 X_3$$

$$[X_2, X_7] = a_3 X_6 + a_5 X_5 + a_7 X_4 + a_9 X_3$$

$$[X_2, X_8] = a_3 X_7 + a_5 X_6 + a_7 X_5 + a_9 X_4 + a_{11} X_3 + a_{12} X_2$$

$$[X_3, X_8] = b_9 X_3 + b_{10} X_2$$

$$[X_4, X_6] = c_3 X_3$$

$$[X_4, X_7] = c_3 X_4 + c_5 X_3 - b_{10} X_2$$

$$[X_4, X_8] = c_3 X_5 + (b_9 + c_5) X_4$$

$$[X_5, X_6] = c_3 X_4 + d_1 X_3 + b_{10} X_2$$

$$[X_5, X_7] = 2c_3 X_5 + (d_1 + c_5) X_4 + d_3 X_3$$

$$[X_5, X_8] = 3c_3 X_6 + (d_1 + b_9 + 2c_5) X_5 + d_3 X_4 + d_5 X_3 + d_6 X_2$$

$$[X_6, X_7] = 2c_3 X_6 + (d_1 + c_5) X_5 + d_3 X_4 + e_1 X_3 - d_6 X_2$$

$$[X_6, X_8] = 5c_3 X_7 + (2d_1 + b_9 + 3c_5) X_6 + 2d_3 X_5 + (e_1 + d_5) X_4 + e_3 X_3$$

$$[X_7, X_8] = 5c_3 X_8 + (2d_1 + b_9 + 3c_5) X_7 + 2d_3 X_6 + (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & a_3 & a_5 & a_7 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & a_3 & a_5 & a_7 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & a_3 & a_5 & a_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_3 & a_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -b_{10} & 0 & 0 \\ -1 & -a_3 & 0 & 0 & 0 & c_3 & c_5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & c_3 & b_9 + c_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_{10} & 0 & 0 & d_6 \\ 0 & -a_5 & 0 & 0 & 0 & d_1 & d_3 & 0 & d_5 \\ -1 & -a_3 & 0 & 0 & 0 & c_3 & d_1 + c_5 & 0 & d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 2c_3 & d_1 + b_9 + 2c_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3c_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -b_{10} & 0 & -d_6 & 0 \\ 0 & -a_7 & 0 & -c_3 & -d_1 & 0 & e_1 & e_3 \\ 0 & -a_5 & 0 & 0 & -c_3 & 0 & d_3 & e_1 + d_5 \\ -1 & -a_3 & 0 & 0 & 0 & 0 & d_1 + c_5 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 2c_3 & 2d_1 + b_9 + 3c_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5c_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 & f_2 \\ 0 & -a_9 & 0 & -c_5 & -d_3 & -e_1 & 0 & f_1 \\ 0 & -a_7 & 0 & -c_3 & -(d_1 + c_5) & -d_3 & 0 & e_3 \\ 0 & -a_5 & 0 & 0 & -2c_3 & -(d_1 + c_5) & 0 & e_1 + d_5 \\ -1 & -a_3 & 0 & 0 & 0 & -2c_3 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_1 + b_9 + 3c_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 5c_3 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 0 & -d_6 & 0 & -f_2 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & 0 & -(b_9 + c_5) & -d_3 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & -a_7 & 0 & -c_3 & -(d_1 + b_9 + 2c_5) & -2d_3 & -(e_1 + d_5) & 0 \\ 0 & -a_5 & 0 & 0 & -3c_3 & -(2d_1 + b_9 + 3c_5) & -2d_3 & 0 \\ -1 & -a_3 & 0 & 0 & 0 & -5c_3 & -(2d_1 + b_9 + 3c_5) & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -5c_3 & 0 \end{pmatrix}$$

Nilpotencia

$$c_6^6 = -a_3 b_{10}$$

$$c_3^7 = -5c_3(2a_3c_3^2d_6 - 2a_3c_3d_3b_{10} + a_3d_1^2b_{10} + 2a_3d_1c_5b_{10} + a_3c_5^2b_{10} - 2a_5c_3d_1b_{10} - 2a_5c_3c_5b_{10} + 4c_3^2a_7b_{10})$$

$$c_4^7 = -(13a_3c_3^2d_6 - 3a_3c_3d_3b_{10} - a_3d_1^2b_{10} - 2a_3d_1c_5b_{10} - a_3c_5^2b_{10} - 3a_5c_3d_1b_{10} - 3a_5c_3c_5b_{10} + 20c_3^4 + 16c_3^2a_7b_{10})$$

$$c_5^7 = -(2a_3c_3d_6 + a_3d_3b_{10} + a_5d_1b_{10} + a_5c_5b_{10} + 36c_3^3 + c_3a_7b_{10})$$

$$c_6^7 = a_3d_6 - 17c_3^2 + a_7b_{10}$$

$$c_2^8 = (\text{demasiado grande } \dots)$$

$$c_3^8 = (\text{demasiado grande } \dots)$$

$$c_4^8 = (\text{demasiado grande } \dots)$$

$$c_5^8 = -(3a_3d_1f_2 - a_3e_1d_6 - a_3f_1b_{10} + 4a_3b_9f_2 + 6a_3c_5f_2 - a_3d_6d_5 - 5a_5c_3f_2 - 2a_5d_3d_6 - a_5e_3b_{10} - 18c_3^2e_1 - 18c_3^2d_5 + 26c_3d_1d_3 + 51c_3d_3b_9 + 60c_3d_3c_5 + 17c_3d_3a_{12} - c_3a_9d_6 - 4d_1^3 - 24d_1^2b_9 - 28d_1^2c_5 - 8d_1^2a_{12} + 4d_1a_7d_6 - 30d_1b_9^2 - 93d_1b_9c_5 - 20d_1b_9a_{12} - 59d_1c_5^2 - 31d_1c_5a_{12} + 5d_1a_{11}b_{10} + 4a_7b_9d_6 + 7a_7c_5d_6 - a_7d_5b_{10} - 10b_9^3 - 54b_9^2c_5 - 10b_9^2a_{12} - 87b_9c_5^2 - 36b_9c_5a_{12} + 4b_9a_{11}b_{10} - 39c_5^3 - 29c_5^2a_{12} + 9c_5a_{11}b_{10})$$

$$c_6^8 = -(a_3f_2 + 17c_3d_3 - 8d_1^2 - 20d_1b_9 - 31d_1c_5 - 5d_1a_{12} + a_7d_6 - 10b_9^2 - 36b_9c_5 - 5b_9a_{12} - 29c_5^2 - 9c_5a_{12} + a_{11}b_{10})$$

$$c_7^8 = 5d_1 + 5b_9 + 9c_5 + a_{12}$$

Jacobi

$$j_3^{248} = a_3a_{12}$$

$$j_3^{257} = 2a_5c_3$$

$$j_2^{258} = -2a_5b_{10}$$

$$j_3^{258} = 2a_5c_5 + a_5a_{12} + 3c_3a_7$$

$$j_4^{258} = a_3a_{12} + 2a_5c_3$$

$$j_2^{267} = 2a_5b_{10}$$

$$j_3^{267} = 2a_5d_1 + 3c_3a_7$$

$$j_4^{267} = 2a_5c_3$$

$$j_3^{268} = 2a_5d_3 + 6c_3a_9 + 3d_1a_7 + 3a_7c_5 + a_7a_{12}$$

$$j_4^{268} = 2a_5d_1 + 2a_5c_5 + a_5a_{12} + 6c_3a_7$$

$$j_5^{268} = a_3a_{12} + 4a_5c_3$$

$$j_2^{278} = -(2a_5d_6 - 5c_3a_{12} + 2a_9b_{10})$$

$$j_3^{278} = 2a_5e_1 + 5c_3a_{11} + 2d_1a_9 + 3d_3a_7 + 4a_9c_5 + a_9a_{12}$$

$$j_4^{278} = 2a_5d_3 + 6c_3a_9 + 3d_1a_7 + 3a_7c_5 + a_7a_{12}$$

$$j_5^{278} = 2a_5d_1 + 2a_5c_5 + a_5a_{12} + 6c_3a_7$$

$$j_6^{278} = a_3a_{12} + 4a_5c_3$$

$$j_3^{348} = a_3b_{10}$$

$$j_3^{358} = a_5b_{10}$$

$$j_4^{358} = a_3b_{10}$$

$$j_3^{368} = a_7b_{10}$$

$$j_4^{368} = a_5b_{10}$$

$$j_5^{368} = a_3b_{10}$$

$$j_2^{378} = 5c_3b_{10}$$

$$j_3^{378} = 5c_3b_9 + a_9b_{10}$$

$$j_4^{378} = a_7b_{10}$$

$$j_5^{378} = a_5b_{10}$$

$$j_6^{378} = a_3b_{10}$$

$$j_3^{456} = -a_3b_{10}$$

$$j_3^{457} = -a_5b_{10}$$

$$\begin{aligned}
j_4^{457} &= -a_3b_{10} \\
j_3^{458} &= -(a_3d_6 - 3c_3^2) \\
j_3^{467} &= a_3d_6 + 3c_3^2 - a_7b_{10} \\
j_4^{467} &= -a_5b_{10} \\
j_5^{467} &= -a_3b_{10} \\
j_2^{468} &= -5c_3b_{10} \\
j_3^{468} &= c_3(3d_1 + b_9 + 9c_5) \\
j_4^{468} &= 6c_3^2 \\
j_2^{478} &= -b_{10}(2d_1 + 2b_9 + 5c_5 - a_{12}) \\
j_3^{478} &= -(a_3f_2 - 3c_3d_3 - 2d_1c_5 - b_9c_5 - 4c_5^2 - a_{11}b_{10}) \\
j_4^{478} &= 3c_3d_1 + 6c_3b_9 + 9c_3c_5 + a_9b_{10} \\
j_5^{478} &= 6c_3^2 + a_7b_{10} \\
j_6^{478} &= a_5b_{10} \\
j_7^{478} &= a_3b_{10} \\
j_2^{567} &= 5c_3b_{10} \\
j_3^{567} &= a_5d_6 + 5c_3d_1 - a_9b_{10} \\
j_4^{567} &= a_3d_6 + 3c_3^2 - a_7b_{10} \\
j_5^{567} &= -a_5b_{10} \\
j_6^{567} &= -a_3b_{10} \\
j_2^{568} &= b_{10}(2d_1 + 2b_9 + 5c_5 - a_{12}) \\
j_3^{568} &= 6c_3d_3 + 3d_1^2 + d_1b_9 + 5d_1c_5 + a_7d_6 - a_{11}b_{10} \\
j_4^{568} &= a_5d_6 + 8c_3d_1 + c_3b_9 + 9c_3c_5 - a_9b_{10} \\
j_5^{568} &= a_3d_6 + 9c_3^2 - a_7b_{10} \\
j_6^{568} &= -a_5b_{10} \\
j_7^{568} &= -a_3b_{10} \\
j_3^{578} &= -(a_5f_2 - 3c_3e_1 - 3c_3d_5 - 5d_1d_3 - d_3b_9 - 6d_3c_5 - a_9d_6) \\
j_4^{578} &= -(a_3f_2 - 9c_3d_3 - 3d_1^2 - d_1b_9 - 7d_1c_5 - a_7d_6 - b_9c_5 - 4c_5^2) \\
j_5^{578} &= a_5d_6 + 11c_3d_1 + 7c_3b_9 + 18c_3c_5 \\
j_6^{578} &= a_3d_6 + 15c_3^2 \\
j_2^{678} &= -(5d_1d_6 + 3e_1b_{10} + 2b_9d_6 + 7c_5d_6 - d_6a_{12} + 2d_5b_{10}) \\
j_3^{678} &= 2c_3e_3 + 3d_1e_1 - 2d_1d_5 + 2d_3^2 + e_1b_9 + 7e_1c_5 - a_7f_2 + d_6a_{11} \\
j_4^{678} &= -(a_5f_2 - 3c_3e_1 - 3c_3d_5 - 5d_1d_3 - d_3b_9 - 6d_3c_5 - a_9d_6) \\
j_5^{678} &= -(a_3f_2 - 9c_3d_3 - 3d_1^2 - d_1b_9 - 7d_1c_5 - a_7d_6 - b_9c_5 - 4c_5^2) \\
j_6^{678} &= a_5d_6 + 11c_3d_1 + 7c_3b_9 + 18c_3c_5 \\
j_7^{678} &= a_3d_6 + 15c_3^2
\end{aligned}$$

Sucesión característica (6,1,1)

Etapa 2

Sustituciones

$$\begin{aligned} a_3 &= 0 && \text{[por el cambio de base } Y_2 = X_2 - a_3 X_1, Y_i = X_i \forall i \neq 2 \text{]} \\ a_5 b_{10} &= 0 && \text{[de } j_2^{267} \text{ en la etapa 1]} \\ a_5 d_1 &= 0 && \text{[de } j_3^{267} \text{ y } j_4^{468} \text{ en la etapa 1]} \\ a_7 b_{10} &= 0 && \text{[de } j_3^{368} \text{ en la etapa 1]} \\ a_9 b_{10} &= 0 && \text{[de } j_3^{378} \text{ y } j_4^{468} \text{ en la etapa 1]} \\ c_3 &= 0 && \text{[de } j_3^{468} \text{ en la etapa 1]} \end{aligned}$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_5] = a_5 X_3$$

$$[X_2, X_6] = a_5 X_4 + a_7 X_3$$

$$[X_2, X_7] = a_5 X_5 + a_7 X_4 + a_9 X_3$$

$$[X_2, X_8] = a_5 X_6 + a_7 X_5 + a_9 X_4 + a_{11} X_3 + a_{12} X_2$$

$$[X_3, X_8] = b_9 X_3 + b_{10} X_2$$

$$[X_4, X_7] = c_5 X_3 - b_{10} X_2$$

$$[X_4, X_8] = (b_9 + c_5) X_4$$

$$[X_5, X_6] = d_1 X_3 + b_{10} X_2$$

$$[X_5, X_7] = (d_1 + c_5) X_4 + d_3 X_3$$

$$[X_5, X_8] = (d_1 + b_9 + 2c_5) X_5 + d_3 X_4 + d_5 X_3 + d_6 X_2$$

$$[X_6, X_7] = (d_1 + c_5) X_5 + d_3 X_4 + e_1 X_3 - d_6 X_2$$

$$[X_6, X_8] = (2d_1 + b_9 + 3c_5) X_6 + 2d_3 X_5 + (e_1 + d_5) X_4 + e_3 X_3$$

$$[X_7, X_8] = (2d_1 + b_9 + 3c_5) X_7 + 2d_3 X_6 + (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_5 & a_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -b_{10} & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & c_5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_9 + c_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_{10} & 0 & 0 & d_6 \\ 0 & -a_5 & 0 & 0 & 0 & d_1 & d_3 & 0 & d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & d_1 + c_5 & 0 & d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_1 + b_9 + 2c_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -b_{10} & 0 & -d_6 & 0 \\ 0 & -a_7 & 0 & 0 & -d_1 & 0 & e_1 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & d_3 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & d_1 + c_5 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_1 + b_9 + 3c_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 & f_2 \\ 0 & -a_9 & 0 & -c_5 & -d_3 & -e_1 & 0 & f_1 \\ 0 & -a_7 & 0 & 0 & -(d_1 + c_5) & -d_3 & 0 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & -(d_1 + c_5) & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_1 + b_9 + 3c_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 0 & -d_6 & 0 & -f_2 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & 0 & -(b_9 + c_5) & -d_3 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & -a_7 & 0 & 0 & -(d_1 + b_9 + 2c_5) & -2d_3 & -(e_1 + d_5) & 0 \\ 0 & -a_5 & 0 & 0 & 0 & -(2d_1 + b_9 + 3c_5) & -2d_3 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & -(2d_1 + b_9 + 3c_5) \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Nilpotencia

$$c_2^8 = 2a_5d_3b_9^2d_6 + 8a_5d_3b_9^2c_5d_6 + 6a_5d_3b_9c_5^2d_6 + 4d_1^3b_9^2a_{12} + 4d_1^3b_9c_5a_{12} - 4d_1^3b_9a_{11}b_{10} - 4d_1^3c_5a_{11}b_{10} - 4d_1^2a_7b_9^2d_6 - 4d_1^2a_7b_9c_5d_6 + 8d_1^2b_9^2a_{12} + 28d_1^2b_9^2c_5a_{12} - 8d_1^2b_9^2a_{11}b_{10} + 20d_1^2b_9c_5^2a_{12} - 28d_1^2b_9c_5a_{11}b_{10} - 20d_1^2c_5^2a_{11}b_{10} - 4d_1a_7b_9^2d_6 - 16d_1a_7b_9^2c_5d_6 - 12d_1a_7b_9c_5^2d_6 + 5d_1b_9^4a_{12} + 31d_1b_9^3c_5a_{12} - 5d_1b_9^3a_{11}b_{10} + 59d_1b_9^2c_5^2a_{12} - 31d_1b_9^2c_5a_{11}b_{10} + 33d_1b_9c_5^3a_{12} - 59d_1b_9c_5^2a_{11}b_{10} - 33d_1c_5^3a_{11}b_{10} - a_7b_9^3d_6 - 7a_7b_9^3c_5d_6 - 15a_7b_9^2c_5^2d_6 - 9a_7b_9c_5^3d_6 + b_9^5a_{12} + 9b_9^4c_5a_{12} - b_9^4a_{11}b_{10} + 29b_9^3c_5^2a_{12} - 9b_9^3c_5a_{11}b_{10} + 39b_9^2c_5^3a_{12} - 29b_9^2c_5^2a_{11}b_{10} + 18b_9c_5^4a_{12} - 39b_9c_5^3a_{11}b_{10} - 18c_5^4a_{11}b_{10}$$

$$c_3^8 = 6a_5d_3b_9^2d_6 + 16a_5d_3b_9c_5d_6 + 6a_5d_3c_5^2d_6 + 4d_1^3b_9^2 + 4d_1^3b_9c_5 + 8d_1^3b_9a_{12} + 4d_1^3c_5a_{12} - 4d_1^3a_{11}b_{10} - 8d_1^2a_7b_9d_6 - 4d_1^2a_7c_5d_6 + 8d_1^2b_9^3 + 28d_1^2b_9^2c_5 + 24d_1^2b_9^2a_{12} + 20d_1^2b_9c_5^2 + 56d_1^2b_9c_5a_{12} - 16d_1^2b_9a_{11}b_{10} + 20d_1^2c_5^2a_{12} - 28d_1^2c_5a_{11}b_{10} - 12d_1a_7b_9^2d_6 - 32d_1a_7b_9c_5d_6 - 12d_1a_7c_5^2d_6 + 5d_1b_9^4 + 31d_1b_9^3c_5 + 20d_1b_9^3a_{12} + 59d_1b_9^2c_5^2 + 93d_1b_9^2c_5a_{12} - 15d_1b_9^2a_{11}b_{10} + 33d_1b_9c_5^3 + 118d_1b_9c_5^2a_{12} - 62d_1b_9c_5a_{11}b_{10} + 33d_1c_5^3a_{12} - 59d_1c_5^2a_{11}b_{10} - 4a_7b_9^3d_6 - 21a_7b_9^2c_5d_6 - 30a_7b_9c_5^2d_6 - 9a_7c_5^3d_6 + b_9^5 + 9b_9^4c_5 + 5b_9^4a_{12} + 29b_9^3c_5^2 + 36b_9^3c_5a_{12} - 4b_9^3a_{11}b_{10} + 39b_9^2c_5^3 + 87b_9^2c_5^2a_{12} - 27b_9^2c_5a_{11}b_{10} + 18b_9c_5^4 + 78b_9c_5^3a_{12} - 58b_9c_5^2a_{11}b_{10} + 18c_5^4a_{12} - 39c_5^3a_{11}b_{10}$$

$$c_4^8 = 6a_5d_3b_9d_6 + 8a_5d_3c_5d_6 + 8d_1^3b_9 + 4d_1^3c_5 + 4d_1^3a_{12} - 4d_1^2a_7d_6 + 24d_1^2b_9^2 + 56d_1^2b_9c_5 + 24d_1^2b_9a_{12} + 20d_1^2c_5^2 + 28d_1^2c_5a_{12} - 8d_1^2a_{11}b_{10} - 12d_1a_7b_9d_6 - 16d_1a_7c_5d_6 + 20d_1b_9^3 + 93d_1b_9^2c_5 + 30d_1b_9^2a_{12} + 118d_1b_9c_5^2 + 93d_1b_9c_5a_{12} - 15d_1b_9a_{11}b_{10} + 33d_1c_5^3 + 59d_1c_5^2a_{12} - 31d_1c_5a_{11}b_{10} - 6a_7b_9^2d_6 - 21a_7b_9c_5d_6 - 15a_7c_5^2d_6 + 5b_9^4 + 36b_9^3c_5 + 10b_9^3a_{12} + 87b_9^2c_5^2 + 54b_9^2c_5a_{12} - 6b_9^2a_{11}b_{10} + 78b_9c_5^3 + 87b_9c_5^2a_{12} - 27b_9c_5a_{11}b_{10} + 18c_5^4 + 39c_5^3a_{12} - 29c_5^2a_{11}b_{10}$$

$$c_5^8 = 2a_5d_3d_6 + 4d_1^3 + 24d_1^2b_9 + 28d_1^2c_5 + 8d_1^2a_{12} - 4d_1a_7d_6 + 30d_1b_9^2 + 93d_1b_9c_5 + 20d_1b_9a_{12} + 59d_1c_5^2 + 31d_1c_5a_{12} - 5d_1a_{11}b_{10} - 4a_7b_9d_6 - 7a_7c_5d_6 + 10b_9^3 + 54b_9^2c_5 + 10b_9^2a_{12} + 87b_9c_5^2 + 36b_9c_5a_{12} - 4b_9a_{11}b_{10} + 39c_5^3 + 29c_5^2a_{12} - 9c_5a_{11}b_{10}$$

$$c_6^8 = 8d_1^2 + 20d_1b_9 + 31d_1c_5 + 5d_1a_{12} - a_7d_6 + 10b_9^2 + 36b_9c_5 + 5b_9a_{12} + 29c_5^2 + 9c_5a_{12} - a_{11}b_{10}$$

$$c_7^8 = 5d_1 + 5b_9 + 9c_5 + a_{12}$$

Jacobi

$$j_3^{258} = a_5(2c_5 + a_{12})$$

$$j_3^{268} = 2a_5d_3 + 3d_1a_7 + 3a_7c_5 + a_7a_{12}$$

$$j_4^{268} = a_5(2c_5 + a_{12})$$

$$j_2^{278} = -2a_5d_6$$

$$j_3^{278} = 2a_5e_1 + 2d_1a_9 + 3d_3a_7 + 4a_9c_5 + a_9a_{12}$$

$$j_4^{278} = 2a_5d_3 + 3d_1a_7 + 3a_7c_5 + a_7a_{12}$$

$$j_5^{278} = a_5(2c_5 + a_{12})$$

$$j_2^{478} = -b_{10}(2d_1 + 2b_9 + 5c_5 - a_{12})$$

$$j_3^{478} = 2d_1c_5 + b_9c_5 + 4c_5^2 + a_{11}b_{10}$$

$$j_3^{567} = a_5d_6$$

$$j_2^{568} = b_{10}(2d_1 + 2b_9 + 5c_5 - a_{12})$$

$$j_3^{568} = 3d_1^2 + d_1b_9 + 5d_1c_5 + a_7d_6 - a_{11}b_{10}$$

$$j_4^{568} = a_5d_6$$

$$j_3^{578} = -(a_5f_2 - 5d_1d_3 - d_3b_9 - 6d_3c_5 - a_9d_6)$$

$$j_4^{578} = 3d_1^2 + d_1b_9 + 7d_1c_5 + a_7d_6 + b_9c_5 + 4c_5^2$$

$$j_5^{578} = a_5d_6$$

$$j_2^{678} = -(5d_1d_6 + 3e_1b_{10} + 2b_9d_6 + 7c_5d_6 - d_6a_{12} + 2d_5b_{10})$$

$$j_3^{678} = 3d_1e_1 - 2d_1d_5 + 2d_3^2 + e_1b_9 + 7e_1c_5 - a_7f_2 + d_6a_{11}$$

$$j_4^{678} = -(a_5f_2 - 5d_1d_3 - d_3b_9 - 6d_3c_5 - a_9d_6)$$

$$j_5^{678} = 3d_1^2 + d_1b_9 + 7d_1c_5 + a_7d_6 + b_9c_5 + 4c_5^2$$

$$j_6^{678} = a_5d_6$$

Sucesión característica (6,1,1)

Etapa 3

Sustituciones

$$\begin{aligned} a_3 &= 0 && \text{[etapa 2]} \\ a_5 b_{10} &= 0 && \text{[etapa 2]} \\ a_5 d_1 &= 0 && \text{[etapa 2]} \\ a_7 b_{10} &= 0 && \text{[etapa 2]} \\ a_9 b_{10} &= 0 && \text{[etapa 2]} \\ c_3 &= 0 && \text{[etapa 2]} \\ a_5 d_6 &= 0 && \text{[de } j_2^{278} \text{ en la etapa 2]} \\ c_5 &= -b_9 && \text{[de nilpotencia con } [X_4, X_8] \text{ en la etapa 2]} \\ d_1 &= b_9 && \text{[} 2d_1 + b_9 + 3c_5 = 2(d_1 - b_9) \text{ es autovalor de } \text{adj}_{X_4}(2)\text{]} \\ a_{12} &= -b_9 && \text{[de } c_7^8(2) \text{, nilpotencia en } [X_4, X_8](2) \text{ y } d_1 = b_9\text{]} \end{aligned}$$

Ley del Álgebra

$$\begin{aligned} [X_1, X_4] &= X_3 \\ [X_1, X_5] &= X_4 \\ [X_1, X_6] &= X_5 \\ [X_1, X_7] &= X_6 \\ [X_1, X_8] &= X_7 \\ [X_2, X_5] &= a_5 X_3 \\ [X_2, X_6] &= a_5 X_4 + a_7 X_3 \\ [X_2, X_7] &= a_5 X_5 + a_7 X_4 + a_9 X_3 \\ [X_2, X_8] &= a_5 X_6 + a_7 X_5 + a_9 X_4 + a_{11} X_3 - b_9 X_2 \\ [X_3, X_8] &= b_9 X_3 + b_{10} X_2 \\ [X_4, X_7] &= -b_9 X_3 - b_{10} X_2 \\ [X_5, X_6] &= b_9 X_3 + b_{10} X_2 \\ [X_5, X_7] &= d_3 X_3 \\ [X_5, X_8] &= d_3 X_4 + d_5 X_3 + d_6 X_2 \\ [X_6, X_7] &= d_3 X_4 + e_1 X_3 - d_6 X_2 \\ [X_6, X_8] &= 2d_3 X_5 + (e_1 + d_5) X_4 + e_3 X_3 \\ [X_7, X_8] &= 2d_3 X_6 + (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2 \end{aligned}$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -b_9 \\ 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_5 & a_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -b_{10} & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & -b_9 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 \\ 0 & -a_5 & 0 & 0 & 0 & b_9 & d_3 & d_5 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -b_{10} & 0 & -d_6 & 0 \\ 0 & -a_7 & 0 & 0 & -b_9 & 0 & e_1 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & d_3 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 & f_2 \\ 0 & -a_9 & 0 & b_9 & -d_3 & -e_1 & 0 & f_1 \\ 0 & -a_7 & 0 & 0 & 0 & -d_3 & 0 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & b_9 & -b_{10} & 0 & -d_6 & 0 & -f_2 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & 0 & 0 & -d_3 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & -a_7 & 0 & 0 & 0 & -2d_3 & -(e_1 + d_5) & 0 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & -2d_3 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Nilpotencia

$$c_5^8 = -a_7 b_9 d_6$$

$$c_6^8 = -(a_7 d_6 + b_9^2 + a_{11} b_{10})$$

Jacobi

$$j_3^{258} = -3a_5 b_9$$

$$j_3^{267} = 2a_5 b_9$$

$$j_3^{268} = 2a_5 d_3 - a_7 b_9$$

$$j_4^{268} = -a_5 b_9$$

$$j_3^{278} = 2a_5 e_1 + 3d_3 a_7 - 3a_9 b_9$$

$$j_4^{278} = 2a_5 d_3 - a_7 b_9$$

$$j_5^{278} = -a_5 b_9$$

$$j_3^{478} = b_9^2 + a_{11} b_{10}$$

$$j_3^{568} = a_7d_6 - b_9^2 - a_{11}b_{10}$$

$$j_3^{578} = -(a_5f_2 - a_9d_6)$$

$$j_4^{578} = a_7d_6$$

$$j_2^{678} = -(3e_1b_{10} + b_9d_6 + 2d_5b_{10})$$

$$j_3^{678} = 2d_3^2 - 3e_1b_9 - a_7f_2 - 2b_9d_5 + d_6a_{11}$$

$$j_4^{678} = -(a_5f_2 - a_9d_6)$$

$$j_5^{678} = a_7d_6$$

Sucesión característica (6,1,1)

Etapa 4

Sustituciones

$$\begin{aligned} a_3 &= 0 && \text{[etapa 2]} \\ a_5 b_{10} &= 0 && \text{[etapa 2]} \\ a_5 d_1 &= 0 && \text{[etapa 2]} \\ a_7 b_{10} &= 0 && \text{[etapa 2]} \\ a_9 b_{10} &= 0 && \text{[etapa 2]} \\ c_3 &= 0 && \text{[etapa 2]} \\ a_5 d_6 &= 0 && \text{[de } j_2^{278} \text{ en la etapa 2]} \\ b_9 &= 0 && \text{[si } b_{10} = 0 \text{ por NIL en } [X_3, X_8](2) \text{ y si } b_{10} \neq 0 \neq b_9, \text{ con el CB } Y_2 = b_9 X_2 + b_{10} X_3] \\ c_5 &= 0 && \text{[de (3) y } b_9 = 0] \\ d_1 &= 0 && \text{[de (3) y } b_9 = 0] \\ a_{12} &= 0 && \text{[de (3) y } b_9 = 0] \end{aligned}$$

Ley del Álgebra

$$\begin{aligned} [X_1, X_4] &= X_3 \\ [X_1, X_5] &= X_4 \\ [X_1, X_6] &= X_5 \\ [X_1, X_7] &= X_6 \\ [X_1, X_8] &= X_7 \\ [X_2, X_5] &= a_5 X_3 \\ [X_2, X_6] &= a_5 X_4 + a_7 X_3 \\ [X_2, X_7] &= a_5 X_5 + a_7 X_4 + a_9 X_3 \\ [X_2, X_8] &= a_5 X_6 + a_7 X_5 + a_9 X_4 + a_{11} X_3 \\ [X_3, X_8] &= b_{10} X_2 \\ [X_4, X_7] &= -b_{10} X_2 \\ [X_5, X_6] &= b_{10} X_2 \\ [X_5, X_7] &= d_3 X_3 \\ [X_5, X_8] &= d_3 X_4 + d_5 X_3 + d_6 X_2 \\ [X_6, X_7] &= d_3 X_4 + e_1 X_3 - d_6 X_2 \\ [X_6, X_8] &= 2d_3 X_5 + (e_1 + d_5) X_4 + e_3 X_3 \\ [X_7, X_8] &= 2d_3 X_6 + (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2 \end{aligned}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -b_{10} & 0 & -d_6 & 0 \\ 0 & -a_7 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & d_3 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 & f_2 \\ 0 & -a_9 & 0 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & -a_7 & 0 & 0 & 0 & -d_3 & 0 & e_3 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & -d_6 & 0 & -f_2 & 0 & 0 \\ 0 & -a_{11} & 0 & 0 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & -a_9 & 0 & 0 & -d_3 & -(e_1 + d_5) & -e_3 & 0 & 0 \\ 0 & -a_7 & 0 & 0 & 0 & -2d_3 & -(e_1 + d_5) & 0 & 0 \\ 0 & -a_5 & 0 & 0 & 0 & 0 & -2d_3 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Nilpotencia

$$c_6^8 = -(a_7d_6 + a_{11}b_{10})$$

Jacobi

$$j_3^{268} = 2a_5d_3$$

$$j_3^{278} = 2a_5e_1 + 3d_3a_7$$

$$j_4^{278} = 2a_5d_3$$

$$j_3^{478} = a_{11}b_{10}$$

$$j_3^{568} = a_7d_6 - a_{11}b_{10}$$

$$j_3^{578} = -(a_5f_2 - a_9d_6)$$

$$j_4^{578} = a_7d_6$$

$$j_2^{678} = -b_{10}(3e_1 + 2d_5)$$

$$j_3^{678} = 2d_3^2 - a_7f_2 + d_6a_{11}$$

$$j_4^{678} = -(a_5 f_2 - a_9 d_6)$$

$$j_5^{678} = a_7 d_6$$

Sucesión característica (6,1,1)

Etapa 4A

Sustituciones

$$a_3 = 0, a_5 = 0, a_7 = 0, a_9 = 0, a_{11} = 0, a_{12} = 0$$

$$b_9 = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0, d_3 = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_8] = b_{10}X_2$$

$$[X_4, X_7] = -b_{10}X_2$$

$$[X_5, X_6] = b_{10}X_2$$

$$[X_5, X_8] = d_5X_3 + d_6X_2$$

$$[X_6, X_7] = e_1X_3 - d_6X_2$$

$$[X_6, X_8] = (e_1 + d_5)X_4 + e_3X_3$$

$$[X_7, X_8] = (e_1 + d_5)X_5 + e_3X_4 + f_1X_3 + f_2X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -b_{10} & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_{10} & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -b_{10} & 0 & -d_6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & b_{10} & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & -d_6 & 0 & 0 & -f_2 \\ 0 & 0 & 0 & 0 & -d_5 & -e_3 & 0 & -f_1 \\ 0 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$j_2^{678} = -b_{10}(3e_1 + 2d_5)$$

Sucesión característica (6,1,1)

Etapa 4B

Sustituciones

$$a_3 = 0, a_{12} = 0$$

$$b_9 = 0, b_{10} = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0, d_3 = 0, d_6 = 0$$

$$e_1 = 0$$

$$f_2 = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_5] = a_5 X_3$$

$$[X_2, X_6] = a_5 X_4 + a_7 X_3$$

$$[X_2, X_7] = a_5 X_5 + a_7 X_4 + a_9 X_3$$

$$[X_2, X_8] = a_5 X_6 + a_7 X_5 + a_9 X_4 + a_{11} X_3$$

$$[X_5, X_8] = d_5 X_3$$

$$[X_6, X_8] = d_5 X_4 + e_3 X_3$$

$$[X_7, X_8] = d_5 X_5 + e_3 X_4 + f_1 X_3$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & a_5 & a_7 & a_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_5 & a_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (6,1,1)

Etapa 4C

Sustituciones

$$a_3 = 0, a_5 = 0, a_{12} = 0$$

$$b_9 = 0, b_{10} = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0, d_3 = 0, d_6 = 0$$

$$f_2 = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_6] = a_7 X_3$$

$$[X_2, X_7] = a_7 X_4 + a_9 X_3$$

$$[X_2, X_8] = a_7 X_5 + a_9 X_4 + a_{11} X_3$$

$$[X_5, X_8] = d_5 X_3$$

$$[X_6, X_7] = e_1 X_3$$

$$[X_6, X_8] = (e_1 + d_5) X_4 + e_3 X_3$$

$$[X_7, X_8] = (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & a_7 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_7 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_7 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_9 & 0 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & -a_7 & 0 & 0 & 0 & 0 & 0 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{11} & 0 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & 0 & 0 & 0 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & -a_7 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (6,1,1)

Etapa 4D

Sustituciones

$$a_3 = 0, a_5 = 0, a_7 = 0, a_{12} = 0$$

$$b_9 = 0, b_{10} = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0, d_3 = 0, d_6 = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_7] = a_9 X_3$$

$$[X_2, X_8] = a_9 X_4 + a_{11} X_3$$

$$[X_5, X_8] = d_5 X_3$$

$$[X_6, X_7] = e_1 X_3$$

$$[X_6, X_8] = (e_1 + d_5) X_4 + e_3 X_3$$

$$[X_7, X_8] = (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & f_2 \\ 0 & -a_9 & 0 & 0 & 0 & -e_1 & 0 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -f_2 & 0 \\ 0 & -a_{11} & 0 & 0 & -d_5 & -e_3 & 0 & -f_1 & 0 \\ 0 & -a_9 & 0 & 0 & 0 & -(e_1 + d_5) & 0 & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (6,1,1)

Etapas 4E

Sustituciones

$$a_3 = 0, a_5 = 0, a_7 = 0, a_9 = 0, a_{12} = 0$$

$$b_9 = 0, b_{10} = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0$$

$$2d_3^2 + d_6 a_{11} = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_8] = a_{11}X_3$$

$$[X_5, X_7] = d_3X_3$$

$$[X_5, X_8] = d_3X_4 + d_5X_3 + d_6X_2$$

$$[X_6, X_7] = d_3X_4 + e_1X_3 - d_6X_2$$

$$[X_6, X_8] = 2d_3X_5 + (e_1 + d_5)X_4 + e_3X_3$$

$$[X_7, X_8] = 2d_3X_6 + (e_1 + d_5)X_5 + e_3X_4 + f_1X_3 + f_2X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_3 & d_5 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_3 & e_1 + d_5 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_6 & 0 & f_2 & 0 \\ 0 & 0 & 0 & 0 & -d_3 & -e_1 & 0 & f_1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -d_3 & 0 & e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -d_6 & 0 & -f_2 & 0 & 0 \\ 0 & -a_{11} & 0 & 0 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -d_3 & -(e_1 + d_5) & -e_3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -2d_3 & -(e_1 + d_5) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -2d_3 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (6,1,1)

Etapa 4F

Sustituciones

$$a_3 = 0, a_5 = 0, a_7 = 0, a_9 = 0, a_{11} = 0, a_{12} = 0$$

$$b_9 = 0, b_{10} = 0$$

$$c_3 = 0, c_5 = 0$$

$$d_1 = 0, d_3 = 0$$

Ley del Álgebra

$$[X_1, X_4] = X_3$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_5, X_8] = d_5 X_3 + d_6 X_2$$

$$[X_6, X_7] = e_1 X_3 - d_6 X_2$$

$$[X_6, X_8] = (e_1 + d_5) X_4 + e_3 X_3$$

$$[X_7, X_8] = (e_1 + d_5) X_5 + e_3 X_4 + f_1 X_3 + f_2 X_2$$

Adjuntas

$$adj_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 + d_5 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$adj_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -d_6 & 0 & 0 & -f_2 \\ 0 & 0 & 0 & 0 & -d_5 & -e_3 & 0 & -f_1 \\ 0 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(e_1 + d_5) & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (5, 2, 1)

Etapa 1

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_6] = a_7 X_4$$

$$[X_2, X_7] = a_{10} X_2 + a_9 X_4 + a_7 X_5$$

$$[X_2, X_8] = a_{12} X_2 + a_{10} X_3 + a_{11} X_4 + a_9 X_5 + a_7 X_6$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = -2a_{10} X_2 + b_5 X_4 + (a_7 + b_3) X_5$$

$$[X_3, X_7] = b_8 X_2 - a_{10} X_3 + b_7 X_4 + (a_9 + b_5) X_5 + (2a_7 + b_3) X_6$$

$$[X_3, X_8] = b_{10} X_2 + (a_{12} + b_8) X_3 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + (3a_7 + b_3) X_7$$

$$[X_4, X_8] = -2d_4 X_2 + c_7 X_4$$

$$[X_5, X_7] = d_4 X_2 + d_3 X_4$$

$$[X_5, X_8] = d_6 X_2 - d_4 X_3 + d_5 X_4 + (c_7 + d_3) X_5$$

$$[X_6, X_7] = -(d_6 X_2) + d_4 X_3 + e_1 X_4 + d_3 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5 + (c_7 + 2d_3) X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6 + (c_7 + 2d_3) X_7$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_{10} & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{10} \\ 0 & 0 & a_1 & 0 & 0 & a_7 & a_9 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & 0 & a_7 & a_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & -2a_{10} & b_8 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & -a_{10} & a_{12} + b_8 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 \\ 0 & 0 & 0 & 0 & 0 & a_7 + b_3 & a_9 + b_5 & a_{11} + b_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 2a_7 + b_3 & 2a_9 + b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3a_7 + b_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -2d_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -d_4 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2a_{10} & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & 0 \\ 0 & -a_7 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -(a_7 + b_3) & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{10} & -b_8 & 0 & -d_4 & d_6 & 0 & f_2 \\ 0 & 0 & a_{10} & 0 & 0 & -d_4 & 0 & e_4 \\ 0 & -a_9 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & -a_7 & -(a_9 + b_5) & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & -2a_7 - b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 2d_4 & -d_6 & -e_4 & -f_2 & 0 & 0 \\ 0 & -a_{10} & -(a_{12} + b_8) & 0 & d_4 & 0 & -e_4 & 0 & 0 \\ 0 & -a_{11} & -b_9 & -c_7 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & -(c_7 + d_3) & -(d_5 + e_1) & -e_3 & 0 & 0 \\ 0 & -a_7 & -2a_9 - b_5 & 0 & 0 & -c_7 - 2d_3 & -(d_5 + e_1) & 0 & 0 \\ -1 & 0 & -3a_7 - b_3 & 0 & 0 & 0 & -c_7 - 2d_3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : 2a_7^2 = 0$$

$$J_2 : 2a_7a_{10} = 0$$

$$J_3 : a_7a_{10} - a_{10}b_3 = 0$$

$$J_4 : a_7a_{10} + a_{10}b_3 = 0$$

$$J_5 : 3a_7a_{10} + a_{10}b_3 = 0$$

$$J_6 : 2a_9a_{10} + 2a_7a_{12} + a_{12}b_3 + a_{10}b_5 + a_7b_8 + b_3b_8 = 0$$

$$J_7 : 5a_7a_9 + 2a_1a_{12} + a_1b_8 - a_1c_7 = 0$$

$$J_8 : 2a_9a_{10} + a_7a_{12} + a_{12}b_3 + a_7b_8 + b_3b_8 - 2a_7d_3 = 0$$

$$J_9 : a_7a_{12} + a_{10}b_5 + 2a_7d_3 = 0$$

$$J_{10} : 2a_1d_4 = 0$$

$$J_{11} : -2a_7d_4 = 0$$

$$J_{12} : -2a_9d_4 = 0$$

$$J_{13} : -2a_{10}d_4 = 0$$

$$J_{14} : 2a_{10}d_4 = 0$$

$$J_{15} : -(a_{10}b_3) - a_1d_4 = 0$$

$$J_{16} : a_{10}b_3 - a_1d_4 = 0$$

$$J_{17} : a_7a_{10} + a_1d_4 = 0$$

$$J_{18} : 5a_7a_{10} + a_{10}b_3 + 2a_1d_4 = 0$$

$$J_{19} : 2a_{10}^2 - 2a_7d_4 = 0$$

$$J_{20} : -2a_{10}^2 + 2a_7d_4 = 0$$

$$J_{21} : -3a_7d_4 - b_3d_4 = 0$$

$$J_{22} : -(a_7d_4) - b_3d_4 = 0$$

$$J_{23} : 4a_{10}^2 - a_7d_4 - b_3d_4 = 0$$

$$J_{24} : a_7d_4 - b_3d_4 = 0$$

$$J_{25} : -3a_7d_4 + b_3d_4 = 0$$

$$J_{26} : -(a_{10}b_8) - a_{10}c_7 - 2a_{10}d_3 + 3a_9d_4 + 2b_5d_4 = 0$$

$$J_{27} : a_{12}b_3 + b_3b_8 - 3a_7d_3 - a_1d_6 = 0$$

$$J_{28} : 2a_9a_{10} - a_{10}b_5 + a_7b_8 - a_7d_3 + a_1d_6 = 0$$

$$J_{29} : a_{10}b_8 + a_{10}c_7 + 2a_{10}d_3 + 3a_9d_4 - 2a_7d_6 = 0$$

$$J_{30} : -(b_5d_4) + a_7d_6 = 0$$

$$J_{31} : -2a_9d_4 - b_5d_4 + a_7d_6 = 0$$

$$J_{32} : -2a_{10}b_8 - 2a_{10}c_7 - 4a_{10}d_3 + 2b_5d_4 + 2a_7d_6 = 0$$

$$J_{33} : -(a_{12}d_4) - b_8d_4 + 2c_7d_4 + 5d_3d_4 + a_{10}d_6 = 0$$

$$J_{34} : a_{10}a_{11} + a_9a_{12} + a_{12}b_5 + a_{10}b_7 + b_5b_8 + a_7b_{10} + 3a_9d_3 + 2b_5d_3 - a_7d_5 - a_7e_1 = 0$$

$$J_{35} : 2a_{10}a_{11} + a_{12}b_5 + b_5b_8 + a_7b_{10} + 2b_5d_3 - a_7d_5 - 3a_7e_1 - a_1e_4 = 0$$

$$J_{36} : -(a_{10}a_{11}) + a_9a_{12} + a_{10}b_7 + 3a_9d_3 + 2a_7e_1 + a_1e_4 = 0$$

$$J_{37} : -(b_{10}d_4) + d_4d_5 + a_{12}d_6 - 2c_7d_6 - 5d_3d_6 + 3d_4e_1 + 3a_{10}e_4 = 0$$

$$J_{38} : c_7d_3 + 3d_3^2 - a_{11}d_4 - b_7d_4 + a_9d_6 - b_3e_4 = 0$$

$$J_{39} : b_8^2 + 2a_{10}b_{10} + b_8c_7 + 2b_8d_3 + a_{11}d_4 + 3b_7d_4 - 2a_{10}d_5 - 3a_9d_6 - 2b_5d_6 - 2a_{10}e_1 - 2a_7e_4 - b_3e_4 = 0$$

$$J_{40} : a_{12}b_7 - a_{11}b_8 + b_7b_8 + a_{10}b_9 + a_9b_{10} + a_{11}d_3 + 3b_7d_3 - a_9d_5 + 2a_9e_1 + 2b_5e_1 - 2a_7e_3 - a_1f_2 = 0$$

$$J_{41} : -(b_9d_4) + a_{11}d_6 + c_7e_1 + 5d_3e_1 + a_9e_4 - b_5e_4 - a_7f_2 = 0$$

Nilpotencia

$$N_1 : 2a_{12} + b_8 + 4c_7 + 5d_3 = 0$$

$$N_2 : -a_{10}^2 - 3a_7d_4 - b_3d_4 = 0$$

$$N_3 : -(a_7a_{10}d_4) - a_{10}b_3d_4 = 0$$

$$N_4 : 2a_7^2d_4^2 + a_7b_3d_4^2 = 0$$

$$N_5 : a_{12}^2 + a_{12}b_8 - a_{10}b_{10} + 8a_{12}c_7 + 4b_8c_7 + 6c_7^2 + 10a_{12}d_3 + 5b_8d_3 + 15c_7d_3 + 8d_3^2 + 3a_{11}d_4 + b_7d_4 - a_9d_6 - 4a_7e_4 - b_3e_4 = 0$$

$$N_6 : 4a_{12}^2c_7 + 4a_{12}b_8c_7 - 4a_{10}b_{10}c_7 + 12a_{12}c_7^2 + 6b_8c_7^2 + 4c_7^3 + 5a_{12}^2d_3 + 5a_{12}b_8d_3 - 5a_{10}b_{10}d_3 + 30a_{12}c_7d_3 + 15b_8c_7d_3 + 15c_7^2d_3 + 16a_{12}d_3^2 + 8b_8d_3^2 + 16c_7d_3^2 + 4d_3^3 + 3a_{11}a_{12}d_4 + a_{12}b_7d_4 + 2a_{11}b_8d_4 - 2a_{10}b_9d_4 - a_9b_{10}d_4 + 9a_{11}c_7d_4 + 3b_7c_7d_4 + 14a_{11}d_3d_4 + 4b_7d_3d_4 - 4a_9d_4d_5 - b_5d_4d_5 + a_{10}a_{11}d_6 - a_9a_{12}d_6 + a_{10}b_7d_6 - a_9b_8d_6 - 3a_9c_7d_6 - 4a_9d_3d_6 + a_7d_5d_6 - 2a_9d_4e_1 - b_5d_4e_1 + a_7d_6e_1 - 5a_7d_4e_3 - b_3d_4e_3 + 2a_9a_{10}e_4 - 4a_7a_{12}e_4 - a_{12}b_3e_4 + a_{10}b_5e_4 - a_7b_8e_4 - 12a_7c_7e_4 - 3b_3c_7e_4 - 12a_7d_3e_4 - 3b_3d_3e_4 + 3a_7a_{10}f_2 + a_{10}b_3f_2 = 0$$

$$N_7 : 6a_{12}^2c_7^2 + 6a_{12}b_8c_7^2 - 6a_{10}b_{10}c_7^2 + 8a_{12}c_7^3 + 4b_8c_7^3 + c_7^4 + 15a_{12}^2c_7d_3 + 15a_{12}b_8c_7d_3 - 15a_{10}b_{10}c_7d_3 + 30a_{12}c_7^2d_3 + 15b_8c_7^2d_3 + 5c_7^3d_3 + 8a_{12}^2d_3^2 + 8a_{12}b_8d_3^2 - 8a_{10}b_{10}d_3^2 + 32a_{12}c_7d_3^2 + 16b_8c_7d_3^2 + 8c_7^2d_3^2 + 8a_{12}d_3^3 + 4b_8d_3^3 + 4c_7d_3^3 + 9a_{11}a_{12}c_7d_4 + 3a_{12}b_7c_7d_4 + 6a_{11}b_8c_7d_4 - 6a_{10}b_9c_7d_4 - 3a_9b_{10}c_7d_4 + 9a_{11}c_7^2d_4 + 3b_7c_7^2d_4 + 14a_{11}a_{12}d_3d_4 + 4a_{12}b_7d_3d_4 + 10a_{11}b_8d_3d_4 - 10a_{10}b_9d_3d_4 - 4a_9b_{10}d_3d_4 + 28a_{11}c_7d_3d_4 + 8b_7c_7d_3d_4 + 20a_{11}d_3^2d_4 + 4b_7d_3^2d_4 + 2a_{11}^2d_4^2 + 2a_{11}b_7d_4^2 - 2a_9b_9d_4^2 + 2a_{10}a_{11}d_4d_5 - 4a_9a_{12}d_4d_5 - a_{12}b_5d_4d_5 + 2a_{10}b_7d_4d_5 - 2a_9b_8d_4d_5 + a_7b_{10}d_4d_5 - 8a_9c_7d_4d_5 - 2b_5c_7d_4d_5 - 12a_9d_3d_4d_5 - 2b_5d_3d_4d_5 + 5a_7d_4d_5^2 + b_3d_4d_5^2 + 3a_{10}a_{11}c_7d_6 - 3a_9a_{12}c_7d_6 + 3a_{10}b_7c_7d_6 - 3a_9b_8c_7d_6 - 3a_9c_7^2d_6 + 4a_{10}a_{11}d_3d_6 - 4a_9a_{12}d_3d_6 + 4a_{10}b_7d_3d_6 - 4a_9b_8d_3d_6 - 8a_9c_7d_3d_6 - 4a_9d_3^2d_6 - 2a_9a_{10}d_5d_6 + a_7a_{12}d_5d_6 - a_{10}b_5d_5d_6 + a_7b_8d_5d_6 + 2a_7c_7d_5d_6 + 2a_7d_3d_5d_6 - 2a_9a_{12}d_4e_1 - a_{12}b_5d_4e_1 + a_7b_{10}d_4e_1 - 4a_9c_7d_4e_1 - 2b_5c_7d_4e_1 - 4a_9d_3d_4e_1 - 2b_5d_3d_4e_1 + 8a_7d_4d_5e_1 + 2b_3d_4d_5e_1 - 2a_9a_{10}d_6e_1 + a_7a_{12}d_6e_1 - a_{10}b_5d_6e_1 + a_7b_8d_6e_1 + 2a_7c_7d_6e_1 + 2a_7d_3d_6e_1 + 3a_7d_4e_1^2 + b_3d_4e_1^2 + 4a_9a_{10}d_4e_3 - 5a_7a_{12}d_4e_3 - a_{12}b_3d_4e_3 + 2a_{10}b_5d_4e_3 - 2a_7b_8d_4e_3 - 10a_7c_7d_4e_3 - 2b_3c_7d_4e_3 - 12a_7d_3d_4e_3 - 2b_3d_3d_4e_3 - 3a_7a_{10}d_6e_3 - a_{10}b_3d_6e_3 + 6a_9a_{10}c_7e_4 - 12a_7a_{12}c_7e_4 - 3a_{12}b_3c_7e_4 + 3a_{10}b_5c_7e_4 - 3a_7b_8c_7e_4 - 12a_7c_7^2e_4 - 3b_3c_7^2e_4 + 6a_9a_{10}d_3e_4 - 12a_7a_{12}d_3e_4 - 3a_{12}b_3d_3e_4 + 3a_{10}b_5d_3e_4 - 3a_7b_8d_3e_4 - 24a_7c_7d_3e_4 - 6b_3c_7d_3e_4 - 8a_7d_3^2e_4 - 2b_3d_3^2e_4 + 2a_9^2d_4e_4 - 7a_7a_{11}d_4e_4 - 2a_{11}b_3d_4e_4 + a_9b_5d_4e_4 - a_7b_7d_4e_4 - 3a_7a_{10}d_5e_4 - a_{10}b_3d_5e_4 + 3a_7a_9d_6e_4 + a_9b_3d_6e_4 - 3a_7a_{10}e_1e_4 - a_{10}b_3e_1e_4 + 3a_7^2e_4^2 + a_7b_3e_4^2 + 6a_7a_{10}d_4f_1 + 2a_{10}b_3d_4f_1 + 9a_7a_{10}c_7f_2 + 3a_{10}b_3c_7f_2 + 9a_7a_{10}d_3f_2 + 3a_{10}b_3d_3f_2 + 3a_7a_9d_4f_2 + a_9b_3d_4f_2 = 0$$

$$N_8 : 4a_{12}^2c_7^3 + 4a_{12}b_8c_7^3 - 4a_{10}b_{10}c_7^3 + 2a_{12}c_7^4 + b_8c_7^4 + 15a_{12}^2c_7^2d_3 + 15a_{12}b_8c_7^2d_3 - 15a_{10}b_{10}c_7^2d_3 + 10a_{12}c_7^3d_3 + 5b_8c_7^3d_3 + 16a_{12}^2c_7d_3^2 + 16a_{12}b_8c_7d_3^2 - 16a_{10}b_{10}c_7d_3^2 + 16a_{12}c_7^2d_3^2 + 8b_8c_7^2d_3^2 + 4a_{12}^2d_3^3 + 4a_{12}b_8d_3^3 - 4a_{10}b_{10}d_3^3 + 8a_{12}c_7d_3^3 + 4b_8c_7d_3^3 + 9a_{11}a_{12}c_7^2d_4 + 3a_{12}b_7c_7^2d_4 + 6a_{11}b_8c_7^2d_4 - 6a_{10}b_9c_7^2d_4 - 3a_9b_{10}c_7^2d_4 + 3a_{11}c_7^3d_4 + b_7c_7^3d_4 + 28a_{11}a_{12}c_7d_3d_4 + 8a_{12}b_7c_7d_3d_4 + 20a_{11}b_8c_7d_3d_4 - 20a_{10}b_9c_7d_3d_4 - 8a_9b_{10}c_7d_3d_4 + 14a_{11}c_7^2d_3d_4 + 4b_7c_7^2d_3d_4 + 20a_{11}a_{12}d_3^2d_4 + 4a_{12}b_7d_3^2d_4 + 16a_{11}b_8d_3^2d_4 - 16a_{10}b_9d_3^2d_4 - 4a_9b_{10}d_3^2d_4 + 20a_{11}c_7d_3^2d_4 + 4b_7c_7d_3^2d_4 + 8a_{11}d_3^3d_4 + 4a_{11}^2c_7d_4^2 + 4a_{11}b_7c_7d_4^2 - 4a_9b_9c_7d_4^2 + 8a_{11}^2d_3d_4^2 + 8a_{11}b_7d_3d_4^2 - 8a_9b_9d_3d_4^2 + 4a_{10}a_{11}c_7d_4d_5 - 8a_9a_{12}c_7d_4d_5 - 2a_{12}b_5c_7d_4d_5 + 4a_{10}b_7c_7d_4d_5 - 4a_9b_8c_7d_4d_5 + 2a_7b_{10}c_7d_4d_5 - 4a_9c_7^2d_4d_5 - b_5c_7^2d_4d_5 + 8a_{10}a_{11}d_3d_4d_5 - 12a_9a_{12}d_3d_4d_5 - 2a_{12}b_5d_3d_4d_5 + 8a_{10}b_7d_3d_4d_5 - 8a_9b_8d_3d_4d_5 + 2a_7b_{10}d_3d_4d_5 - 12a_9c_7d_3d_4d_5 - 2b_5c_7d_3d_4d_5 - 8a_9d_3^2d_4d_5 - 4a_9a_{11}d_4^2d_5 - 2a_{11}b_5d_4^2d_5 + 2a_7b_9d_4^2d_5 - 4a_9a_{10}d_4d_5^2 + 5a_7a_{12}d_4d_5^2 + a_{12}b_3d_4d_5^2 - 2a_{10}b_5d_4d_5^2 + 2a_7b_8d_4d_5^2 + 5a_7c_7d_4d_5^2 + b_3c_7d_4d_5^2 + 4a_7d_3d_4d_5^2 + 3a_{10}a_{11}c_7^2d_6 - 3a_9a_{12}c_7^2d_6 + 3a_{10}b_7c_7^2d_6 - 3a_9b_8c_7^2d_6 - a_9c_7^3d_6 + 8a_{10}a_{11}c_7d_3d_6 - 8a_9a_{12}c_7d_3d_6 + 8a_{10}b_7c_7d_3d_6 - 8a_9b_8c_7d_3d_6 - 4a_9c_7^2d_3d_6 + 4a_{10}a_{11}d_3^2d_6 - 4a_9a_{12}d_3^2d_6 + 4a_{10}b_7d_3^2d_6 - 4a_9b_8d_3^2d_6 - 4a_9c_7d_3^2d_6 - 4a_9a_{10}c_7d_5d_6 + 2a_7a_{12}c_7d_5d_6 - 2a_{10}b_5c_7d_5d_6 + 2a_7b_8c_7d_5d_6 + 2a_7c_7d_3d_5d_6 + 3a_7a_{10}d_5^2d_6 + a_{10}b_3d_5^2d_6 - 4a_9a_{12}c_7d_4e_1 - 2a_{12}b_5c_7d_4e_1 + 2a_7b_{10}c_7d_4e_1 - 2a_9c_7^2d_4e_1 - b_5c_7^2d_4e_1 - 4a_9a_{12}d_3d_4e_1 - 2a_{12}b_5d_3d_4e_1 + 2a_7b_{10}d_3d_4e_1 - 4a_9c_7d_3d_4e_1 - 2b_5c_7d_3d_4e_1 - 4a_9a_{11}d_4^2e_1 - 2a_{11}b_5d_4^2e_1 + 2a_7b_9d_4^2e_1 - 4a_9a_{10}d_4d_5e_1 + 8a_7a_{12}d_4d_5e_1 + 2a_{12}b_3d_4d_5e_1 - 2a_{10}b_5d_4d_5e_1 + 2a_7b_8d_4d_5e_1 + 8a_7c_7d_4d_5e_1 + 2b_3c_7d_4d_5e_1 + 4a_7d_3d_4d_5e_1 - 4a_9a_{10}c_7d_6e_1 + 2a_7a_{12}c_7d_6e_1 - 2a_{10}b_5c_7d_6e_1 + 2a_7b_8c_7d_6e_1 + a_7c_7^2d_6e_1 - 4a_9a_{10}d_3d_6e_1 + 2a_7a_{12}d_3d_6e_1 - 2a_{10}b_5d_3d_6e_1 + 2a_7b_8d_3d_6e_1 + 2a_7c_7d_3d_6e_1 + 6a_7a_{10}d_5d_6e_1 +$$

$$\begin{aligned}
 & 2a_{10}b_3d_5d_6e_1 + 3a_7a_{12}d_4e_1^2 + a_{12}b_3d_4e_1^2 + 3a_7c_7d_4e_1^2 + b_3c_7d_4e_1^2 + 3a_7a_{10}d_6e_1^2 + a_{10}b_3d_6e_1^2 + \\
 & 8a_9a_{10}c_7d_4e_3 - 10a_7a_{12}c_7d_4e_3 - 2a_{12}b_3c_7d_4e_3 + 4a_{10}b_5c_7d_4e_3 - 4a_7b_8c_7d_4e_3 - 5a_7c_7^2d_4e_3 - b_3c_7^2d_4e_3 + \\
 & 12a_9a_{10}d_3d_4e_3 - 12a_7a_{12}d_3d_4e_3 - 2a_{12}b_3d_3d_4e_3 + 6a_{10}b_5d_3d_4e_3 - 6a_7b_8d_3d_4e_3 - 12a_7c_7d_3d_4e_3 - \\
 & 2b_3c_7d_3d_4e_3 - 4a_7d_3^2d_4e_3 + 4a_9^2d_4^2e_3 - 8a_7a_{11}d_4^2e_3 - 2a_{11}b_3d_4^2e_3 + 2a_9b_5d_4^2e_3 - 2a_7b_7d_4^2e_3 - \\
 & 12a_7a_{10}d_4d_5e_3 - 4a_{10}b_3d_4d_5e_3 - 6a_7a_{10}c_7d_6e_3 - 2a_{10}b_3c_7d_6e_3 - 6a_7a_{10}d_3d_6e_3 - 2a_{10}b_3d_3d_6e_3 - 6a_7a_{10}d_4e_1e_3 - \\
 & 2a_{10}b_3d_4e_1e_3 + 6a_9a_{10}c_7^2e_4 - 12a_7a_{12}c_7^2e_4 - 3a_{12}b_3c_7^2e_4 + 3a_{10}b_5c_7^2e_4 - 3a_7b_8c_7^2e_4 - 4a_7c_7^3e_4 - \\
 & b_3c_7^3e_4 + 12a_9a_{10}c_7d_3e_4 - 24a_7a_{12}c_7d_3e_4 - 6a_{12}b_3c_7d_3e_4 + 6a_{10}b_5c_7d_3e_4 - 6a_7b_8c_7d_3e_4 - 12a_7c_7^2d_3e_4 - \\
 & 3b_3c_7^2d_3e_4 + 4a_9a_{10}d_3^2e_4 - 8a_7a_{12}d_3^2e_4 - 2a_{12}b_3d_3^2e_4 + 2a_{10}b_5d_3^2e_4 - 2a_7b_8d_3^2e_4 - 8a_7c_7d_3^2e_4 - \\
 & 2b_3c_7d_3^2e_4 + 4a_9^2c_7d_4e_4 - 14a_7a_{11}c_7d_4e_4 - 4a_{11}b_3c_7d_4e_4 + 2a_9b_5c_7d_4e_4 - 2a_7b_7c_7d_4e_4 + 4a_9^2d_3d_4e_4 - \\
 & 20a_7a_{11}d_3d_4e_4 - 6a_{11}b_3d_3d_4e_4 + 2a_9b_5d_3d_4e_4 - 2a_7b_7d_3d_4e_4 - 6a_7a_{10}c_7d_5e_4 - 2a_{10}b_3c_7d_5e_4 - 3a_7a_{10}d_3d_5e_4 - \\
 & a_{10}b_3d_3d_5e_4 + 3a_7a_9d_4d_5e_4 + a_9b_3d_4d_5e_4 + 6a_7a_9c_7d_6e_4 + 2a_9b_3c_7d_6e_4 + 6a_7a_9d_3d_6e_4 + 2a_9b_3d_3d_6e_4 - \\
 & 3a_7^2d_5d_6e_4 - a_7b_3d_5d_6e_4 - 6a_7a_{10}c_7e_1e_4 - 2a_{10}b_3c_7e_1e_4 - 3a_7a_{10}d_3e_1e_4 - a_{10}b_3d_3e_1e_4 - 3a_7a_9d_4e_1e_4 - \\
 & a_9b_3d_4e_1e_4 - 3a_7^2d_6e_1e_4 - a_7b_3d_6e_1e_4 + 9a_7^2d_4e_3e_4 + 3a_7b_3d_4e_3e_4 + 6a_7^2c_7e_4^2 + 2a_7b_3c_7e_4^2 + 3a_7^2d_3e_4^2 + \\
 & a_7b_3d_3e_4^2 + 12a_7a_{10}c_7d_4f_1 + 4a_{10}b_3c_7d_4f_1 + 18a_7a_{10}d_3d_4f_1 + 6a_{10}b_3d_3d_4f_1 + 6a_7a_9d_4^2f_1 + 2a_9b_3d_4^2f_1 + \\
 & 9a_7a_{10}c_7^2f_2 + 3a_{10}b_3c_7^2f_2 + 18a_7a_{10}c_7d_3f_2 + 6a_{10}b_3c_7d_3f_2 + 6a_7a_{10}d_3^2f_2 + 2a_{10}b_3d_3^2f_2 + 6a_7a_9c_7d_4f_2 + \\
 & 2a_9b_3c_7d_4f_2 + 6a_7a_9d_3d_4f_2 + 2a_9b_3d_3d_4f_2 - 3a_7^2d_4d_5f_2 - a_7b_3d_4d_5f_2 - 3a_7^2d_4e_1f_2 - a_7b_3d_4e_1f_2 = 0
 \end{aligned}$$

$$\begin{aligned}
 N_9 : & a_{12}^2c_7^4 + a_{12}b_8c_7^4 - a_{10}b_{10}c_7^4 + 5a_{12}^2c_7^3d_3 + 5a_{12}b_8c_7^3d_3 - 5a_{10}b_{10}c_7^3d_3 + 8a_{12}^2c_7^2d_3^2 + 8a_{12}b_8c_7^2d_3^2 - \\
 & 8a_{10}b_{10}c_7^2d_3^2 + 4a_{12}^2c_7d_3^3 + 4a_{12}b_8c_7d_3^3 - 4a_{10}b_{10}c_7d_3^3 + 3a_{11}a_{12}c_7^3d_4 + a_{12}b_7c_7^3d_4 + 2a_{11}b_8c_7^3d_4 - \\
 & 2a_{10}b_9c_7^3d_4 - a_9b_{10}c_7^3d_4 + 14a_{11}a_{12}c_7^2d_3d_4 + 4a_{12}b_7c_7^2d_3d_4 + 10a_{11}b_8c_7^2d_3d_4 - 10a_{10}b_9c_7^2d_3d_4 - \\
 & 4a_9b_{10}c_7^2d_3d_4 + 20a_{11}a_{12}c_7d_3^2d_4 + 4a_{12}b_7c_7d_3^2d_4 + 16a_{11}b_8c_7d_3^2d_4 - 16a_{10}b_9c_7d_3^2d_4 - 4a_9b_{10}c_7d_3^2d_4 + \\
 & 8a_{11}a_{12}d_3^3d_4 + 8a_{11}b_8d_3^3d_4 - 8a_{10}b_9d_3^3d_4 + 2a_{11}^2c_7^2d_4^2 + 2a_{11}b_7c_7^2d_4^2 - 2a_9b_9c_7^2d_4^2 + 8a_{11}^2c_7d_3d_4^2 + \\
 & 8a_{11}b_7c_7d_3d_4^2 - 8a_9b_9c_7d_3d_4^2 + 8a_{11}^2d_3^2d_4^2 + 8a_{11}b_7d_3^2d_4^2 - 8a_9b_9d_3^2d_4^2 + 2a_{10}a_{11}c_7^2d_4d_5 - 4a_9a_{12}c_7^2d_4d_5 - \\
 & a_{12}b_5c_7^2d_4d_5 + 2a_{10}b_7c_7^2d_4d_5 - 2a_9b_8c_7^2d_4d_5 + a_7b_{10}c_7^2d_4d_5 + 8a_{10}a_{11}c_7d_3d_4d_5 - 12a_9a_{12}c_7d_3d_4d_5 - \\
 & 2a_{12}b_5c_7d_3d_4d_5 + 8a_{10}b_7c_7d_3d_4d_5 - 8a_9b_8c_7d_3d_4d_5 + 2a_7b_{10}c_7d_3d_4d_5 + 8a_{10}a_{11}d_3^2d_4d_5 - 8a_9a_{12}d_3^2d_4d_5 + \\
 & 8a_{10}b_7d_3^2d_4d_5 - 8a_9b_8d_3^2d_4d_5 - 4a_9a_{11}c_7d_4^2d_5 - 2a_{11}b_5c_7d_4^2d_5 + 2a_7b_9c_7d_4^2d_5 - 8a_9a_{11}d_3d_4^2d_5 - \\
 & 4a_{11}b_5d_3d_4^2d_5 + 4a_7b_9d_3d_4^2d_5 - 4a_9a_{10}c_7d_4d_5^2 + 5a_7a_{12}c_7d_4d_5^2 + a_{12}b_3c_7d_4d_5^2 - 2a_{10}b_5c_7d_4d_5^2 + \\
 & 2a_7b_8c_7d_4d_5^2 - 8a_9a_{10}d_3d_4d_5^2 + 4a_7a_{12}d_3d_4d_5^2 - 4a_{10}b_5d_3d_4d_5^2 + 4a_7b_8d_3d_4d_5^2 + 6a_7a_{11}d_4^2d_5^2 + \\
 & 2a_{11}b_3d_4^2d_5^2 + 6a_7a_{10}d_4d_5^3 + 2a_{10}b_3d_4d_5^3 + a_{10}a_{11}c_7^3d_6 - a_9a_{12}c_7^3d_6 + a_{10}b_7c_7^3d_6 - a_9b_8c_7^3d_6 + \\
 & 4a_{10}a_{11}c_7^2d_3d_6 - 4a_9a_{12}c_7^2d_3d_6 + 4a_{10}b_7c_7^2d_3d_6 - 4a_9b_8c_7^2d_3d_6 + 4a_{10}a_{11}c_7d_3^2d_6 - 4a_9a_{12}c_7d_3^2d_6 + \\
 & 4a_{10}b_7c_7d_3^2d_6 - 4a_9b_8c_7d_3^2d_6 - 2a_9a_{10}c_7^2d_5d_6 + a_7a_{12}c_7^2d_5d_6 - a_{10}b_5c_7^2d_5d_6 + a_7b_8c_7^2d_5d_6 - 4a_9a_{10}c_7d_3d_5d_6 + \\
 & 2a_7a_{12}c_7d_3d_5d_6 - 2a_{10}b_5c_7d_3d_5d_6 + 2a_7b_8c_7d_3d_5d_6 + 3a_7a_{10}c_7d_5^2d_6 + a_{10}b_3c_7d_5^2d_6 - 2a_9a_{12}c_7^2d_4e_1 - \\
 & a_{12}b_5c_7^2d_4e_1 + a_7b_{10}c_7^2d_4e_1 - 4a_9a_{12}c_7d_3d_4e_1 - 2a_{12}b_5c_7d_3d_4e_1 + 2a_7b_{10}c_7d_3d_4e_1 - 4a_9a_{11}c_7d_4^2e_1 - \\
 & 2a_{11}b_5c_7d_4^2e_1 + 2a_7b_9c_7d_4^2e_1 - 8a_9a_{11}d_3d_4^2e_1 - 4a_{11}b_5d_3d_4^2e_1 + 4a_7b_9d_3d_4^2e_1 - 4a_9a_{10}c_7d_4d_5e_1 + \\
 & 8a_7a_{12}c_7d_4d_5e_1 + 2a_{12}b_3c_7d_4d_5e_1 - 2a_{10}b_5c_7d_4d_5e_1 + 2a_7b_8c_7d_4d_5e_1 - 8a_9a_{10}d_3d_4d_5e_1 + 4a_7a_{12}d_3d_4d_5e_1 - \\
 & 4a_{10}b_5d_3d_4d_5e_1 + 4a_7b_8d_3d_4d_5e_1 + 12a_7a_{11}d_4^2d_5e_1 + 4a_{11}b_3d_4^2d_5e_1 + 12a_7a_{10}d_4d_5^2e_1 + 4a_{10}b_3d_4d_5^2e_1 - \\
 & 2a_9a_{10}c_7^2d_6e_1 + a_7a_{12}c_7^2d_6e_1 - a_{10}b_5c_7^2d_6e_1 + a_7b_8c_7^2d_6e_1 - 4a_9a_{10}c_7d_3d_6e_1 + 2a_7a_{12}c_7d_3d_6e_1 - \\
 & 2a_{10}b_5c_7d_3d_6e_1 + 2a_7b_8c_7d_3d_6e_1 + 6a_7a_{10}c_7d_5d_6e_1 + 2a_{10}b_3c_7d_5d_6e_1 + 3a_7a_{12}c_7d_4e_1^2 + a_{12}b_3c_7d_4e_1^2 + \\
 & 6a_7a_{11}d_4^2e_1^2 + 2a_{11}b_3d_4^2e_1^2 + 6a_7a_{10}d_4d_5e_1^2 + 2a_{10}b_3d_4d_5e_1^2 + 3a_7a_{10}c_7d_6e_1^2 + a_{10}b_3c_7d_6e_1^2 + \\
 & 4a_9a_{10}c_7^2d_4e_3 - 5a_7a_{12}c_7^2d_4e_3 - a_{12}b_3c_7^2d_4e_3 + 2a_{10}b_5c_7^2d_4e_3 - 2a_7b_8c_7^2d_4e_3 + 12a_9a_{10}c_7d_3d_4e_3 - \\
 & 12a_7a_{12}c_7d_3d_4e_3 - 2a_{12}b_3c_7d_3d_4e_3 + 6a_{10}b_5c_7d_3d_4e_3 - 6a_7b_8c_7d_3d_4e_3 + 8a_9a_{10}d_3^2d_4e_3 - 4a_7a_{12}d_3^2d_4e_3 + \\
 & 4a_{10}b_5d_3^2d_4e_3 - 4a_7b_8d_3^2d_4e_3 + 4a_9^2c_7d_4^2e_3 - 8a_7a_{11}c_7d_4^2e_3 - 2a_{11}b_3c_7d_4^2e_3 + 2a_9b_5c_7d_4^2e_3 - \\
 & 2a_7b_7c_7d_4^2e_3 + 8a_9^2d_3d_4^2e_3 - 16a_7a_{11}d_3d_4^2e_3 - 4a_{11}b_3d_3d_4^2e_3 + 4a_9b_5d_3d_4^2e_3 - 4a_7b_7d_3d_4^2e_3 - \\
 & 12a_7a_{10}c_7d_4d_5e_3 - 4a_{10}b_3c_7d_4d_5e_3 - 18a_7a_{10}d_3d_4d_5e_3 - 6a_{10}b_3d_3d_4d_5e_3 - 6a_7a_9d_4^2d_5e_3 - 2a_9b_3d_4^2d_5e_3 - \\
 & 3a_7a_{10}c_7^2d_6e_3 - a_{10}b_3c_7^2d_6e_3 - 6a_7a_{10}c_7d_3d_6e_3 - 2a_{10}b_3c_7d_3d_6e_3 - 6a_7a_{10}c_7d_4e_1e_3 - 2a_{10}b_3c_7d_4e_1e_3 - \\
 & 6a_7a_{10}d_3d_4e_1e_3 - 2a_{10}b_3d_3d_4e_1e_3 - 6a_7a_9d_4^2e_1e_3 - 2a_9b_3d_4^2e_1e_3 + 6a_7^2d_4^2e_3^2 + 2a_7b_3d_4^2e_3^2 + 2a_9a_{10}c_7^3e_4 - \\
 & 4a_7a_{12}c_7^3e_4 - a_{12}b_3c_7^3e_4 + a_{10}b_5c_7^3e_4 - a_7b_8c_7^3e_4 + 6a_9a_{10}c_7^2d_3e_4 - 12a_7a_{12}c_7^2d_3e_4 - 3a_{12}b_3c_7^2d_3e_4 + \\
 & 3a_{10}b_5c_7^2d_3e_4 - 3a_7b_8c_7^2d_3e_4 + 4a_9a_{10}c_7d_3^2e_4 - 8a_7a_{12}c_7d_3^2e_4 - 2a_{12}b_3c_7d_3^2e_4 + 2a_{10}b_5c_7d_3^2e_4 - \\
 & 2a_7b_8c_7d_3^2e_4 + 2a_9^2c_7^2d_4e_4 - 7a_7a_{11}c_7^2d_4e_4 - 2a_{11}b_3c_7^2d_4e_4 + a_9b_5c_7^2d_4e_4 - a_7b_7c_7^2d_4e_4 + 4a_9^2c_7d_3d_4e_4 - \\
 & 20a_7a_{11}c_7d_3d_4e_4 - 6a_{11}b_3c_7d_3d_4e_4 + 2a_9b_5c_7d_3d_4e_4 - 2a_7b_7c_7d_3d_4e_4 - 12a_7a_{11}d_3^2d_4e_4 - 4a_{11}b_3d_3^2d_4e_4 - \\
 & 3a_7a_{10}c_7^2d_5e_4 - a_{10}b_3c_7^2d_5e_4 - 3a_7a_{10}c_7d_3d_5e_4 - a_{10}b_3c_7d_3d_5e_4 + 3a_7a_9c_7d_4d_5e_4 + a_9b_3c_7d_4d_5e_4 + \\
 & 12a_7a_9d_3d_4d_5e_4 + 4a_9b_3d_3d_4d_5e_4 - 6a_7^2d_4d_5^2e_4 - 2a_7b_3d_4d_5^2e_4 + 3a_7a_9c_7^2d_6e_4 + a_9b_3c_7^2d_6e_4 + \\
 & 6a_7a_9c_7d_3d_6e_4 + 2a_9b_3c_7d_3d_6e_4 - 3a_7^2c_7d_5d_6e_4 - a_7b_3c_7d_5d_6e_4 - 3a_7a_{10}c_7^2e_1e_4 - a_{10}b_3c_7^2e_1e_4 - \\
 & 3a_7a_{10}c_7d_3e_1e_4 - a_{10}b_3c_7d_3e_1e_4 - 3a_7a_9c_7d_4e_1e_4 - a_9b_3c_7d_4e_1e_4 - 6a_7^2d_4d_5e_1e_4 - 2a_7b_3d_4d_5e_1e_4 -
 \end{aligned}$$

$$\begin{aligned}
& 3a_7^2 c_7 d_6 e_1 e_4 - a_7 b_3 c_7 d_6 e_1 e_4 + 9a_7^2 c_7 d_4 e_3 e_4 + 3a_7 b_3 c_7 d_4 e_3 e_4 + 6a_7^2 d_3 d_4 e_3 e_4 + 2a_7 b_3 d_3 d_4 e_3 e_4 + \\
& 3a_7^2 c_7^2 e_4^2 + a_7 b_3 c_7^2 e_4^2 + 3a_7^2 c_7 d_3 e_4^2 + a_7 b_3 c_7 d_3 e_4^2 + 6a_7 a_{10} c_7^2 d_4 f_1 + 2a_{10} b_3 c_7^2 d_4 f_1 + 18a_7 a_{10} c_7 d_3 d_4 f_1 + \\
& 6a_{10} b_3 c_7 d_3 d_4 f_1 + 12a_7 a_{10} d_3^2 d_4 f_1 + 4a_{10} b_3 d_3^2 d_4 f_1 + 6a_7 a_9 c_7 d_4^2 f_1 + 2a_9 b_3 c_7 d_4^2 f_1 + 12a_7 a_9 d_3 d_4^2 f_1 + \\
& 4a_9 b_3 d_3 d_4^2 f_1 - 6a_7^2 d_4^2 d_5 f_1 - 2a_7 b_3 d_4^2 d_5 f_1 - 6a_7^2 d_4^2 e_1 f_1 - 2a_7 b_3 d_4^2 e_1 f_1 + 3a_7 a_{10} c_7^3 f_2 + a_{10} b_3 c_7^3 f_2 + \\
& 9a_7 a_{10} c_7^2 d_3 f_2 + 3a_{10} b_3 c_7^2 d_3 f_2 + 6a_7 a_{10} c_7 d_3^2 f_2 + 2a_{10} b_3 c_7 d_3^2 f_2 + 3a_7 a_9 c_7^2 d_4 f_2 + a_9 b_3 c_7^2 d_4 f_2 + \\
& 6a_7 a_9 c_7 d_3 d_4 f_2 + 2a_9 b_3 c_7 d_3 d_4 f_2 - 3a_7^2 c_7 d_4 d_5 f_2 - a_7 b_3 c_7 d_4 d_5 f_2 - 3a_7^2 c_7 d_4 e_1 f_2 - a_7 b_3 c_7 d_4 e_1 f_2 = 0
\end{aligned}$$

Sucesión característica (5, 2, 1)

Etapa 2

Relaciones

$$R_1: a_7 = 0 \text{ por } J_1(1)$$

$$R_2: a_{10} = 0 \text{ por } a_7 = 0 \text{ en } J_{19}(1)$$

$$R_3: a_1 d_4 = 0 \text{ por } J_{10}(1)$$

$$R_4: a_1 d_4 = 0 \text{ por } a_7 = 0 \text{ en } J_{12}(1)$$

$$R_5: b_3 d_4 = 0 \text{ por } a_7 = 0 \text{ en } J_{21}(1)$$

$$R_6: a_1 d_6 = 0 \text{ por } a_7 = a_{10} = 0 \text{ en } J_{28}(1)$$

$$R_7: b_5 d_4 = 0 \text{ por } a_7 = 0 \text{ en } J_{30}(1)$$

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = b_8 X_2 + b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + (a_{12} + b_8) X_3 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_4, X_8] = -2d_4X_2 + c_7X_4$$

$$[X_5, X_7] = d_4X_2 + d_3X_4$$

$$[X_5, X_8] = d_6X_2 - d_4X_3 + d_5X_4 + (c_7 + d_3) X_5$$

$$[X_6, X_7] = -(d_6X_2) + d_4X_3 + e_1X_4 + d_3X_5$$

$$[X_6, X_8] = e_4X_2 + e_3X_4 + (d_5 + e_1) X_5 + (c_7 + 2d_3) X_6$$

$$[X_7, X_8] = f_2X_2 + e_4X_3 + f_1X_4 + e_3X_5 + (d_5 + e_1) X_6 + (c_7 + 2d_3) X_7$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & b_8 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} + b_8 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & 0 & b_9 \\ 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -2d_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -d_4 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_8 & 0 & -d_4 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -d_4 & 0 & e_4 \\ 0 & -a_9 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 2d_4 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & -(a_{12} + b_8) & 0 & d_4 & 0 & -e_4 & 0 \\ 0 & -a_{11} & -b_9 & -c_7 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & -(c_7 + d_3) & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & -c_7 - 2d_3 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & -c_7 - 2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : a_{12}b_3 + b_3b_8 = 0$$

$$J_2 : 2a_1a_{12} + a_1b_8 - a_1c_7 = 0$$

$$J_3 : a_9a_{12} + a_{12}b_5 + b_5b_8 + 3a_9d_3 + 2b_5d_3 = 0$$

$$J_4 : -(a_{12}d_4) - b_8d_4 + 2c_7d_4 + 5d_3d_4 = 0$$

$$J_5 : -(b_{10}d_4) + d_4d_5 + a_{12}d_6 - 2c_7d_6 - 5d_3d_6 + 3d_4e_1 = 0$$

$$J_6 : a_{12}b_5 + b_5b_8 + 2b_5d_3 - a_1e_4 = 0$$

$$J_7 : a_9a_{12} + 3a_9d_3 + a_1e_4 = 0$$

$$J_8 : c_7d_3 + 3d_3^2 - a_{11}d_4 - b_7d_4 + a_9d_6 - b_3e_4 = 0$$

$$J_9 : b_8^2 + b_8c_7 + 2b_8d_3 + a_{11}d_4 + 3b_7d_4 - 3a_9d_6 - 2b_5d_6 - b_3e_4 = 0$$

$$J_{10} : -(b_9d_4) + a_{11}d_6 + c_7e_1 + 5d_3e_1 + a_9e_4 - b_5e_4 = 0$$

$$J_{11} : a_{12}b_7 - a_{11}b_8 + b_7b_8 + a_9b_{10} + a_{11}d_3 + 3b_7d_3 - a_9d_5 + 2a_9e_1 + 2b_5e_1 - a_1f_2 = 0$$

Nilpotencia

$$N_1 : 2a_{12} + b_8 + 4c_7 + 5d_3 = 0$$

$$N_2 : a_{12}^2 + a_{12}b_8 + 8a_{12}c_7 + 4b_8c_7 + 6c_7^2 + 10a_{12}d_3 + 5b_8d_3 + 15c_7d_3 + 8d_3^2 + 3a_{11}d_4 + b_7d_4 - a_9d_6 - b_3e_4 = 0$$

$$N_3 : (\text{demasiado grande } \dots)$$

$$N_4 : (\text{demasiado grande } \dots)$$

$$N_5 : (\text{demasiado grande } \dots)$$

$$N_6 : (\text{demasiado grande } \dots)$$

Sucesión característica (5, 2, 1)

Etapa 3

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = (-2a_{12} - 4c_7 - 5d_3) X_2 + b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + (-a_{12} - 4c_7 - 5d_3) X_3 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_4, X_8] = -2d_4 X_2 + c_7 X_4$$

$$[X_5, X_7] = d_4 X_2 + d_3 X_4$$

$$[X_5, X_8] = d_6 X_2 - d_4 X_3 + d_5 X_4 + (c_7 + d_3) X_5$$

$$[X_6, X_7] = -(d_6 X_2) + d_4 X_3 + e_1 X_4 + d_3 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5 + (c_7 + 2d_3) X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6 + (c_7 + 2d_3) X_7$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & -2a_{12} - 4c_7 - 5d_3 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -a_{12} - 4c_7 - 5d_3 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_9 + b_5 & a_{11} + b_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -2d_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & d_6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -d_4 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2a_{12} + 4c_7 + 5d_3 & 0 & -d_4 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -d_4 & 0 & e_4 \\ 0 & -a_9 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_7 + 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 2d_4 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & a_{12} + 4c_7 + 5d_3 & 0 & d_4 & 0 & -e_4 & 0 \\ 0 & -a_{11} & -b_9 & -c_7 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & -(c_7 + d_3) & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & -c_7 - 2d_3 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & -c_7 - 2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : -5a_1c_7 - 5a_1d_3 = 0$$

$$J_2 : -(a_{12}b_3) - 4b_3c_7 - 5b_3d_3 = 0$$

$$J_3 : a_9a_{12} - a_{12}b_5 - 4b_5c_7 + 3a_9d_3 - 3b_5d_3 = 0$$

$$J_4 : a_{12}d_4 + 6c_7d_4 + 10d_3d_4 = 0$$

$$J_5 : -(b_{10}d_4) + d_4d_5 + a_{12}d_6 - 2c_7d_6 - 5d_3d_6 + 3d_4e_1 = 0$$

$$J_6 : -(a_{12}b_5) - 4b_5c_7 - 3b_5d_3 - a_1e_4 = 0$$

$$J_7 : a_9a_{12} + 3a_9d_3 + a_1e_4 = 0$$

$$J_8 : c_7d_3 + 3d_3^2 - a_{11}d_4 - b_7d_4 + a_9d_6 - b_3e_4 = 0$$

$$J_9 : 4a_{12}^2 + 14a_{12}c_7 + 12c_7^2 + 16a_{12}d_3 + 27c_7d_3 + 15d_3^2 + a_{11}d_4 + 3b_7d_4 - 3a_9d_6 - 2b_5d_6 - b_3e_4 = 0$$

$$J_{10} : -(b_9d_4) + a_{11}d_6 + c_7e_1 + 5d_3e_1 + a_9e_4 - b_5e_4 = 0$$

$$J_{11} : 2a_{11}a_{12} - a_{12}b_7 + a_9b_{10} + 4a_{11}c_7 - 4b_7c_7 + 6a_{11}d_3 - 2b_7d_3 - a_9d_5 + 2a_9e_1 + 2b_5e_1 - a_1f_2 = 0$$

Nilpotencia

$$N_1 : -a_{12}^2 - 4a_{12}c_7 - 10c_7^2 - 5a_{12}d_3 - 25c_7d_3 - 17d_3^2 + 3a_{11}d_4 + b_7d_4 - a_9d_6 - b_3e_4 = 0$$

$$N_2 : -4a_{12}^2c_7 - 16a_{12}c_7^2 - 20c_7^3 - 5a_{12}^2d_3 - 40a_{12}c_7d_3 - 75c_7^2d_3 - 25a_{12}d_3^2 - 91c_7d_3^2 - 36d_3^3 - a_{11}a_{12}d_4 + a_{12}b_7d_4 + a_{11}c_7d_4 + 3b_7c_7d_4 + 4a_{11}d_3d_4 + 4b_7d_3d_4 + a_9a_{12}d_6 + a_9c_7d_6 + a_9d_3d_6 - a_{12}b_3e_4 - 3b_3c_7e_4 - 3b_3d_3e_4 = 0$$

N_3 : (demasiado grande ...)

N_4 : (demasiado grande ...)

N_5 : (demasiado grande ...)

Sucesión característica (5, 2, 1)

Etapa 4A

Relaciones

$R_1: d_4 \neq 0$

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Part(*rel, i*)

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_7] = \frac{5d_3X_2}{3} + b_7X_4$$

$$[X_3, X_8] = b_{10}X_2 + \frac{5d_3X_3}{3} + b_9X_4 + b_7X_5$$

$$[X_4, X_8] = -2d_4X_2 - \frac{5d_3X_4}{3}$$

$$[X_5, X_7] = d_4X_2 + d_3X_4$$

$$[X_5, X_8] = d_6X_2 - d_4X_3 + d_5X_4 - \frac{2d_3X_5}{3}$$

$$[X_6, X_7] = -(d_6X_2) + d_4X_3 + e_1X_4 + d_3X_5$$

$$[X_6, X_8] = e_4X_2 + e_3X_4 + (d_5 + e_1)X_5 + \frac{d_3X_6}{3}$$

$$[X_7, X_8] = f_2X_2 + e_4X_3 + f_1X_4 + e_3X_5 + (d_5 + e_1)X_6 + \frac{d_3X_7}{3}$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & \frac{5d_3}{3} & b_{10} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5d_3}{3} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_7 & b_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -2d_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{-5d_3}{3} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -d_4 \\ -1 & 0 & 0 & 0 & 0 & 0 & d_3 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{-2d_3}{3} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{d_3}{3} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{-5d_3}{3} & 0 & -d_4 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -d_4 & 0 & e_4 \\ 0 & 0 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{d_3}{3} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 2d_4 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & \frac{-5d_3}{3} & 0 & d_4 & 0 & -e_4 & 0 \\ 0 & 0 & -b_9 & \frac{5d_3}{3} & -d_5 & -e_3 & -f_1 & 0 \\ 0 & 0 & -b_7 & 0 & \frac{2d_3}{3} & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{-d_3}{3} & -(d_5 + e_1) & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & \frac{-d_3}{3} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : \frac{14b_7d_3}{3} = 0$$

$$J_2 : \frac{4d_3^2}{3} - b_7d_4 = 0$$

$$J_3 : \frac{10d_3^2}{3} + 3b_7d_4 = 0$$

$$J_4 : -(b_9d_4) + \frac{10d_3e_1}{3} = 0$$

$$J_5 : -(b_{10}d_4) + d_4d_5 - \frac{5d_3d_6}{3} + 3d_4e_1 = 0$$

Nilpotencia

$$N_1 : \frac{-28d_3^2}{9} + b_7d_4 = 0$$

$$N_2 : \frac{-2d_3^3}{27} - b_7d_3d_4 = 0$$

$$N_3 : \frac{25d_3^4}{27} - b_7d_3^2d_4 = 0$$

$$N_4 : \frac{50d_3^5}{243} - \frac{5b_7d_3^3d_4}{27} = 0$$

Sucesión característica (5, 2, 1)

Etapa 4A2

Relaciones

$R_1: d_4 \neq 0$

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_8] = (d_5 + 3e_1) X_2$$

$$[X_4, X_8] = -2d_4 X_2$$

$$[X_5, X_7] = d_4 X_2$$

$$[X_5, X_8] = d_6 X_2 - d_4 X_3 + d_5 X_4$$

$$[X_6, X_7] = -(d_6 X_2) + d_4 X_3 + e_1 X_4$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & d_4 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -d_4 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & -d_4 & 0 & e_4 \\ 0 & 0 & 0 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -d_5 - 3e_1 & 2d_4 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & d_4 & 0 & -e_4 & 0 \\ 0 & 0 & 0 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(d_5 + e_1) & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión Característica de $\text{adj}_{X_1+mX_8}$

$$S_1^8: -3m^3d_4 + 9m^2d_4d_5 - 9md_4d_5^2 + 3d_4d_5^3 + 9m^2d_4e_1 - 18md_4d_5e_1 + 9d_4d_5^2e_1 - 9md_4e_1^2 + 9d_4d_5e_1^2 + 3d_4e_1^3 = 0$$

$$S_2^8: 3m^4d_4 - 9m^3d_4d_5 + 9m^2d_4d_5^2 - 3md_4d_5^3 - 9m^3d_4e_1 + 18m^2d_4d_5e_1 - 9md_4d_5^2e_1 + 9m^2d_4e_1^2 - 9md_4d_5e_1^2 - 3md_4e_1^3 = 0$$

$$S_3^8: 3m^5d_4^2 - 15m^4d_4^2d_5 + 30m^3d_4^2d_5^2 - 30m^2d_4^2d_5^3 + 15md_4^2d_5^4 - 3d_4^2d_5^5 - 15m^4d_4^2e_1 + 60m^3d_4^2d_5e_1 - 90m^2d_4^2d_5^2e_1 + 60md_4^2d_5^3e_1 - 15d_4^2d_5^4e_1 + 30m^3d_4^2e_1^2 - 90m^2d_4^2d_5e_1^2 + 90md_4^2d_5^2e_1^2 - 30d_4^2d_5^3e_1^2 - 30m^2d_4^2e_1^3 + 60md_4^2d_5e_1^3 - 30d_4^2d_5^2e_1^3 + 15md_4^2e_1^4 - 15d_4^2d_5e_1^4 - 3d_4^2e_1^5 = 0$$

$$S_4^8: 3m^6d_4^2 - 15m^5d_4^2d_5 + 30m^4d_4^2d_5^2 - 30m^3d_4^2d_5^3 + 15m^2d_4^2d_5^4 - 3md_4^2d_5^5 - 15m^5d_4^2e_1 + 60m^4d_4^2d_5e_1 - 90m^3d_4^2d_5^2e_1 + 60m^2d_4^2d_5^3e_1 - 15md_4^2d_5^4e_1 + 30m^4d_4^2e_1^2 - 90m^3d_4^2d_5e_1^2 + 90m^2d_4^2d_5^2e_1^2 - 30md_4^2d_5^3e_1^2 - 30m^3d_4^2e_1^3 + 60m^2d_4^2d_5e_1^3 - 30md_4^2d_5^2e_1^3 + 15m^2d_4^2e_1^4 - 15md_4^2d_5e_1^4 - 3md_4^2e_1^5 = 0$$

$$S_5^8: (\text{demasiado grande } \dots)$$

$$S_6^8: (\text{demasiado grande } \dots)$$

$$S_7^8: (\text{demasiado grande } \dots)$$

S_8^8 : (demasiado grande ...)

S_9^8 : (demasiado grande ...)

S_{10}^8 : (demasiado grande ...)

$$S_{11}^8 : -3m^4d_4^2e_3+12m^3d_4^2d_5e_3-18m^2d_4^2d_5^2e_3+12md_4^2d_5^3e_3-3d_4^2d_5^4e_3+12m^3d_4^2e_1e_3-36m^2d_4^2d_5e_1e_3+36md_4^2d_5^2e_1e_3-12d_4^2d_5^3e_1e_3-18m^2d_4^2e_1^2e_3+36md_4^2d_5e_1^2e_3-18d_4^2d_5^2e_1^2e_3+12md_4^2e_1^3e_3-12d_4^2d_5e_1^3e_3-3d_4^2e_1^4e_3=0$$

$$S_{12}^8 : -3m^5d_4^2e_3+12m^4d_4^2d_5e_3-18m^3d_4^2d_5^2e_3+12m^2d_4^2d_5^3e_3-3md_4^2d_5^4e_3+12m^4d_4^2e_1e_3-36m^3d_4^2d_5e_1e_3+36m^2d_4^2d_5^2e_1e_3-12md_4^2d_5^3e_1e_3-18m^3d_4^2e_1^2e_3+36m^2d_4^2d_5e_1^2e_3-18md_4^2d_5^2e_1^2e_3+12m^2d_4^2e_1^3e_3-12md_4^2d_5e_1^3e_3-3md_4^2e_1^4e_3=0$$

$$S_{13}^8 : 3m^5d_4^2e_3-15m^4d_4^2d_5e_3+30m^3d_4^2d_5^2e_3-30m^2d_4^2d_5^3e_3+15md_4^2d_5^4e_3-3d_4^2d_5^5e_3-15m^4d_4^2e_1e_3+60m^3d_4^2d_5e_1e_3-90m^2d_4^2d_5^2e_1e_3+60md_4^2d_5^3e_1e_3-15d_4^2d_5^4e_1e_3+30m^3d_4^2e_1^2e_3-90m^2d_4^2d_5e_1^2e_3+90md_4^2d_5^2e_1^2e_3-30d_4^2d_5^3e_1^2e_3-30m^2d_4^2e_1^3e_3+60md_4^2d_5e_1^3e_3-30d_4^2d_5^2e_1^3e_3+15md_4^2e_1^4e_3-15d_4^2d_5e_1^4e_3-3d_4^2e_1^5e_3=0$$

$$S_{14}^8 : -3m^6d_4^2e_3+15m^5d_4^2d_5e_3-30m^4d_4^2d_5^2e_3+30m^3d_4^2d_5^3e_3-15m^2d_4^2d_5^4e_3+3md_4^2d_5^5e_3+15m^5d_4^2e_1e_3-60m^4d_4^2d_5e_1e_3+90m^3d_4^2d_5^2e_1e_3-60m^2d_4^2d_5^3e_1e_3+15md_4^2d_5^4e_1e_3-30m^4d_4^2e_1^2e_3+90m^3d_4^2d_5e_1^2e_3-90m^2d_4^2d_5^2e_1^2e_3+30md_4^2d_5^3e_1^2e_3+30m^3d_4^2e_1^3e_3-60m^2d_4^2d_5e_1^3e_3+30md_4^2d_5^2e_1^3e_3-15m^2d_4^2e_1^4e_3+15md_4^2d_5e_1^4e_3+3md_4^2e_1^5e_3=0$$

S_{15}^8 : (demasiado grande ...)

S_{16}^8 : (demasiado grande ...)

Sucesión característica (5, 2, 1)

Etapas 4B

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = (-2a_{12} - 5d_3) X_2 + b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + (-a_{12} - 5d_3) X_3 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_5, X_7] = d_3 X_4$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_4 + d_3 X_5$$

$$[X_6, X_7] = -(d_6 X_2) + e_1 X_4 + d_3 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5 + 2d_3 X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6 + 2d_3 X_7$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & -2a_{12} - 5d_3 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -a_{12} - 5d_3 & b_9 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 & a_{11} + b_7 \\ 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 & 2a_9 + b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 & b_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2a_{12} + 5d_3 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & -a_9 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 0 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & a_{12} + 5d_3 & 0 & 0 & 0 & -e_4 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & -d_3 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & -2d_3 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & -2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : -(a_{12}b_3) - 5b_3d_3 = 0$$

$$J_2 : a_9a_{12} - a_{12}b_5 + 3a_9d_3 - 3b_5d_3 = 0$$

$$J_3 : a_{12}d_6 - 5d_3d_6 = 0$$

$$J_4 : -(a_{12}b_5) - 3b_5d_3 - a_1e_4 = 0$$

$$J_5 : a_9a_{12} + 3a_9d_3 + a_1e_4 = 0$$

$$J_6 : 3d_3^2 + a_9d_6 - b_3e_4 = 0$$

$$J_7 : 4a_{12}^2 + 16a_{12}d_3 + 15d_3^2 - 3a_9d_6 - 2b_5d_6 - b_3e_4 = 0$$

$$J_8 : a_{11}d_6 + 5d_3e_1 + a_9e_4 - b_5e_4 = 0$$

$$J_9 : 2a_{11}a_{12} - a_{12}b_7 + a_9b_{10} + 6a_{11}d_3 - 2b_7d_3 - a_9d_5 + 2a_9e_1 + 2b_5e_1 - a_1f_2 = 0$$

Nilpotencia

$$N_1 : -a_{12}^2 - 5a_{12}d_3 - 17d_3^2 - a_9d_6 - b_3e_4 = 0$$

$$N_2 : -5a_{12}^2d_3 - 25a_{12}d_3^2 - 36d_3^3 + a_9a_{12}d_6 + a_9d_3d_6 - a_{12}b_3e_4 - 3b_3d_3e_4 = 0$$

$$N_3 : -8a_{12}^2d_3^2 - 40a_{12}d_3^3 - 20d_3^4 + 4a_9a_{12}d_3d_6 + 16a_9d_3^2d_6 - 3a_{12}b_3d_3e_4 - 2b_3d_3^2e_4 + a_9b_3d_6e_4 = 0$$

$$N_4 : -4a_{12}^2d_3^3 - 20a_{12}d_3^4 + 4a_9a_{12}d_3^2d_6 + 20a_9d_3^3d_6 - 2a_{12}b_3d_3^2e_4 + 2a_9b_3d_3d_6e_4 = 0$$

Sucesión característica (5, 2, 1)

Etapa 4BA

Ley del Álgebra

$$[X_1, X_3] = X_2 + M X_8$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_5, X_8] = d_5 X_4$$

$$[X_6, X_7] = e_1 X_4$$

$$[X_6, X_8] = e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & M & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 \\ 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 \\ -M & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_9 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & 0 & 0 & 0 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & 0 & -(d_5 + e_1) & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1: -(Ma_9) = 0$$

$$J_2: -(Ma_{11}) = 0$$

$$J_3: Md_5 = 0$$

$$J_4: Md_5 + Me_1 = 0$$

$$J_5: Me_3 = 0$$

$$J_6: Mf_1 = 0$$

$$J_7: Mf_2 = 0$$

$$J_8: a_9 b_{10} - a_9 d_5 + 2a_9 e_1 + 2b_5 e_1 - a_1 f_2 = 0$$

Sucesión característica (5, 2, 1)

Etapa 4BB

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = (-2a_{12} - 5d_3) X_2 + b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + (-a_{12} - 5d_3) X_3 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_5, X_7] = d_3 X_4$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_4 + d_3 X_5$$

$$[X_6, X_7] = -(d_6 X_2) + e_1 X_4 + d_3 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5 + 2d_3 X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6 + 2d_3 X_7$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & -2a_{12} - 5d_3 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -a_{12} - 5d_3 & 0 \\ 0 & 0 & 0 & 0 & b_3 & b_5 & b_7 & b_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & d_3 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2a_{12} + 5d_3 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & -a_9 & -b_7 & 0 & -d_3 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & -d_3 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 2d_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & 0 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & a_{12} + 5d_3 & 0 & 0 & 0 & -e_4 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & -d_3 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & -2d_3 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & -2d_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : a_9 a_{12} + 3a_9 d_3 = 0$$

$$J_2 : -(a_{12} b_3) - 5b_3 d_3 = 0$$

$$J_3 : -(a_{12} b_5) - 3b_5 d_3 = 0$$

$$J_4 : a_9 a_{12} - a_{12} b_5 + 3a_9 d_3 - 3b_5 d_3 = 0$$

$$J_5 : a_{12} d_6 - 5d_3 d_6 = 0$$

$$J_6 : 2a_{11} a_{12} - a_{12} b_7 + a_9 b_{10} + 6a_{11} d_3 - 2b_7 d_3 - a_9 d_5 + 2a_9 e_1 + 2b_5 e_1 = 0$$

$$J_7 : 3d_3^2 + a_9 d_6 - b_3 e_4 = 0$$

$$J_8 : 4a_{12}^2 + 16a_{12} d_3 + 15d_3^2 - 3a_9 d_6 - 2b_5 d_6 - b_3 e_4 = 0$$

$$J_9 : a_{11} d_6 + 5d_3 e_1 + a_9 e_4 - b_5 e_4 = 0$$

Nilpotencia

$$N_1 : -a_{12}^2 - 5a_{12}d_3 - 17d_3^2 - a_9d_6 - b_3e_4 = 0$$

$$N_2 : -5a_{12}^2d_3 - 25a_{12}d_3^2 - 36d_3^3 + a_9a_{12}d_6 + a_9d_3d_6 - a_{12}b_3e_4 - 3b_3d_3e_4 = 0$$

$$N_3 : -8a_{12}^2d_3^2 - 40a_{12}d_3^3 - 20d_3^4 + 4a_9a_{12}d_3d_6 + 16a_9d_3^2d_6 - 3a_{12}b_3d_3e_4 - 2b_3d_3^2e_4 + a_9b_3d_6e_4 = 0$$

$$N_4 : -4a_{12}^2d_3^3 - 20a_{12}d_3^4 + 4a_9a_{12}d_3^2d_6 + 20a_9d_3^3d_6 - 2a_{12}b_3d_3^2e_4 + 2a_9b_3d_3d_6e_4 = 0$$

Sucesión característica (5, 2, 1)

Etapas 4BB1

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_3 X_5$$

$$[X_3, X_7] = b_7 X_4 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + b_7 X_5 + b_3 X_7$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_4$$

$$[X_6, X_7] = -(d_6 X_2) + e_1 X_4$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & 0 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & -d_6 & -e_4 & -f_2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -e_4 & 0 & 0 \\ 0 & 0 & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(d_5 + e_1) & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : -(b_3 e_4) = 0$$

Nilpotencia

$$N_1 : -(b_3 e_4) = 0$$

Sucesión Característica de $\text{adj}_{X_1+mX_8}$

$$S_1^8 : m^4 b_3^2 e_4^2 = 0$$

$$S_2^8 : -(m^5 b_3^2 e_4^2) = 0$$

$$S_3^8 : -(m^5 b_3^3 e_4^2) = 0$$

$$S_4^8 : -(m^5 b_3^2 e_3 e_4^2) = 0$$

$$S_5^8 : -(m^5 b_3^2 e_4^3) = 0$$

$$S_6^8 : m^7 b_3^3 e_3 e_4^3 = 0$$

$$\begin{aligned}
S_7^8 &: m^8 b_3^3 e_3 e_4^3 = 0 \\
S_8^8 &: m^8 b_3^4 e_3 e_4^3 = 0 \\
S_9^8 &: m^7 b_3^3 e_4^4 = 0 \\
S_{10}^8 &: m^8 b_3^3 e_4^4 = 0 \\
S_{11}^8 &: m^8 b_3^4 e_4^4 = 0 \\
S_{12}^8 &: m^2 b_3 e_4 - 2m^3 b_3 d_5 e_4 + m^4 b_3 d_5^2 e_4 - 2m^3 b_3 e_1 e_4 + 2m^4 b_3 d_5 e_1 e_4 + m^4 b_3 e_1^2 e_4 + m^4 b_3 b_7 e_4^2 = 0 \\
S_{13}^8 &: -(m^3 b_3 e_4) + 2m^4 b_3 d_5 e_4 - m^5 b_3 d_5^2 e_4 + 2m^4 b_3 e_1 e_4 - 2m^5 b_3 d_5 e_1 e_4 - m^5 b_3 e_1^2 e_4 - m^5 b_3 b_7 e_4^2 = 0 \\
S_{14}^8 &: -(m^3 b_3^2 e_4) + 2m^4 b_3^2 d_5 e_4 - m^5 b_3^2 d_5^2 e_4 + 2m^4 b_3^2 e_1 e_4 - 2m^5 b_3^2 d_5 e_1 e_4 - m^5 b_3^2 e_1^2 e_4 - m^5 b_3^2 b_7 e_4^2 = 0 \\
S_{15}^8 &: -2m^3 b_3 e_3 e_4 + 2m^4 b_3 d_5 e_3 e_4 + m^4 b_3 e_1 e_3 e_4 + m^4 b_3 b_9 e_4^2 = 0 \\
S_{16}^8 &: 2m^4 b_3 e_3 e_4 - 2m^5 b_3 d_5 e_3 e_4 - m^5 b_3 e_1 e_3 e_4 - m^5 b_3 b_9 e_4^2 = 0 \\
S_{17}^8 &: 2m^4 b_3^2 e_3 e_4 - 2m^5 b_3^2 d_5 e_3 e_4 - m^5 b_3^2 e_1 e_3 e_4 - m^5 b_3^2 b_9 e_4^2 = 0 \\
S_{18}^8 &: m^4 b_3 d_6 e_3 e_4 - 2m^3 b_3 e_4^2 + m^4 b_3 b_{10} e_4^2 + m^4 b_3 d_5 e_4^2 + m^4 b_3 e_1 e_4^2 = 0 \\
S_{19}^8 &: -(m^5 b_3 d_6 e_3 e_4) + 2m^4 b_3 e_4^2 - m^5 b_3 b_{10} e_4^2 - m^5 b_3 d_5 e_4^2 - m^5 b_3 e_1 e_4^2 = 0 \\
S_{20}^8 &: m^4 b_3^2 e_4^2 - m^5 b_3^2 d_5 e_4^2 - m^5 b_3^2 e_1 e_4^2 = 0 \\
S_{21}^8 &: -(m^5 b_3^2 d_6 e_3 e_4) + 2m^4 b_3^2 e_4^2 - m^5 b_3^2 b_{10} e_4^2 - m^5 b_3^2 d_5 e_4^2 - m^5 b_3^2 e_1 e_4^2 = 0 \\
S_{22}^8 &: -(m^6 b_3^3 e_4^3) + m^7 b_3^3 d_5 e_4^3 + m^7 b_3^3 e_1 e_4^3 = 0 \\
S_{23}^8 &: -(m^7 b_3^3 e_4^3) + m^8 b_3^3 d_5 e_4^3 + m^8 b_3^3 e_1 e_4^3 = 0 \\
S_{24}^8 &: -(m^7 b_3^4 e_4^3) + m^8 b_3^4 d_5 e_4^3 + m^8 b_3^4 e_1 e_4^3 = 0 \\
S_{25}^8 &: m^4 b_3^2 e_4^2 - 3m^5 b_3^2 d_5 e_4^2 + 3m^6 b_3^2 d_5^2 e_4^2 - m^7 b_3^2 d_5^3 e_4^2 - 3m^5 b_3^2 e_1 e_4^2 + 6m^6 b_3^2 d_5 e_1 e_4^2 - 3m^7 b_3^2 d_5^2 e_1 e_4^2 + \\
& 3m^6 b_3^2 e_1^2 e_4^2 - 3m^7 b_3^2 d_5 e_1^2 e_4^2 - m^7 b_3^2 e_1^3 e_4^2 + m^6 b_3^2 b_7 e_4^3 - m^7 b_3^2 b_7 d_5 e_4^3 - m^7 b_3^2 b_7 e_1 e_4^3 = 0 \\
S_{26}^8 &: m^5 b_3^2 e_4^2 - 3m^6 b_3^2 d_5 e_4^2 + 3m^7 b_3^2 d_5^2 e_4^2 - m^8 b_3^2 d_5^3 e_4^2 - 3m^6 b_3^2 e_1 e_4^2 + 6m^7 b_3^2 d_5 e_1 e_4^2 - 3m^8 b_3^2 d_5^2 e_1 e_4^2 + \\
& 3m^7 b_3^2 e_1^2 e_4^2 - 3m^8 b_3^2 d_5 e_1^2 e_4^2 - m^8 b_3^2 e_1^3 e_4^2 + m^7 b_3^2 b_7 e_4^3 - m^8 b_3^2 b_7 d_5 e_4^3 - m^8 b_3^2 b_7 e_1 e_4^3 = 0 \\
S_{27}^8 &: m^5 b_3^3 e_4^2 - 3m^6 b_3^3 d_5 e_4^2 + 3m^7 b_3^3 d_5^2 e_4^2 - m^8 b_3^3 d_5^3 e_4^2 - 3m^6 b_3^3 e_1 e_4^2 + 6m^7 b_3^3 d_5 e_1 e_4^2 - 3m^8 b_3^3 d_5^2 e_1 e_4^2 + \\
& 3m^7 b_3^3 e_1^2 e_4^2 - 3m^8 b_3^3 d_5 e_1^2 e_4^2 - m^8 b_3^3 e_1^3 e_4^2 + m^7 b_3^3 b_7 e_4^3 - m^8 b_3^3 b_7 d_5 e_4^3 - m^8 b_3^3 b_7 e_1 e_4^3 = 0 \\
S_{28}^8 &: -2m^5 b_3^2 e_3 e_4^2 + 4m^6 b_3^2 d_5 e_3 e_4^2 - 2m^7 b_3^2 d_5^2 e_3 e_4^2 + 3m^6 b_3^2 e_1 e_3 e_4^2 - 3m^7 b_3^2 d_5 e_1 e_3 e_4^2 - m^7 b_3^2 e_1^2 e_3 e_4^2 + \\
& m^6 b_3^2 b_9 e_4^3 - m^7 b_3^2 b_9 d_5 e_4^3 - m^7 b_3^2 b_9 e_1 e_4^3 = 0 \\
S_{29}^8 &: -2m^6 b_3^2 e_3 e_4^2 + 4m^7 b_3^2 d_5 e_3 e_4^2 - 2m^8 b_3^2 d_5^2 e_3 e_4^2 + 3m^7 b_3^2 e_1 e_3 e_4^2 - 3m^8 b_3^2 d_5 e_1 e_3 e_4^2 - m^8 b_3^2 e_1^2 e_3 e_4^2 + \\
& m^7 b_3^2 b_9 e_4^3 - m^8 b_3^2 b_9 d_5 e_4^3 - m^8 b_3^2 b_9 e_1 e_4^3 = 0 \\
S_{30}^8 &: -2m^6 b_3^3 e_3 e_4^2 + 4m^7 b_3^3 d_5 e_3 e_4^2 - 2m^8 b_3^3 d_5^2 e_3 e_4^2 + 3m^7 b_3^3 e_1 e_3 e_4^2 - 3m^8 b_3^3 d_5 e_1 e_3 e_4^2 - m^8 b_3^3 e_1^2 e_3 e_4^2 + \\
& m^7 b_3^3 b_9 e_4^3 - m^8 b_3^3 b_9 d_5 e_4^3 - m^8 b_3^3 b_9 e_1 e_4^3 = 0 \\
S_{31}^8 &: m^6 b_3^2 d_6 e_3 e_4^2 - m^7 b_3^2 d_5 d_6 e_3 e_4^2 - m^7 b_3^2 d_6 e_1 e_3 e_4^2 - 2m^5 b_3^2 e_4^3 + m^6 b_3^2 b_{10} e_4^3 + 3m^6 b_3^2 d_5 e_4^3 - \\
& m^7 b_3^2 b_{10} d_5 e_4^3 - m^7 b_3^2 d_5^2 e_4^3 + 3m^6 b_3^2 e_1 e_4^3 - m^7 b_3^2 b_{10} e_1 e_4^3 - 2m^7 b_3^2 d_5 e_1 e_4^3 - m^7 b_3^2 e_1^2 e_4^3 = 0 \\
S_{32}^8 &: m^7 b_3^2 d_6 e_3 e_4^2 - m^8 b_3^2 d_5 d_6 e_3 e_4^2 - m^8 b_3^2 d_6 e_1 e_3 e_4^2 - 2m^6 b_3^2 e_4^3 + m^7 b_3^2 b_{10} e_4^3 + 3m^7 b_3^2 d_5 e_4^3 - \\
& m^8 b_3^2 b_{10} d_5 e_4^3 - m^8 b_3^2 d_5^2 e_4^3 + 3m^7 b_3^2 e_1 e_4^3 - m^8 b_3^2 b_{10} e_1 e_4^3 - 2m^8 b_3^2 d_5 e_1 e_4^3 - m^8 b_3^2 e_1^2 e_4^3 = 0 \\
S_{33}^8 &: m^7 b_3^3 d_6 e_3 e_4^2 - m^8 b_3^3 d_5 d_6 e_3 e_4^2 - m^8 b_3^3 d_6 e_1 e_3 e_4^2 - 2m^6 b_3^3 e_4^3 + m^7 b_3^3 b_{10} e_4^3 + 3m^7 b_3^3 d_5 e_4^3 - \\
& m^8 b_3^3 b_{10} d_5 e_4^3 - m^8 b_3^3 d_5^2 e_4^3 + 3m^7 b_3^3 e_1 e_4^3 - m^8 b_3^3 b_{10} e_1 e_4^3 - 2m^8 b_3^3 d_5 e_1 e_4^3 - m^8 b_3^3 e_1^2 e_4^3 = 0
\end{aligned}$$

$$S_{34}^8 : m^5 b_3^2 e_4^3 - 2m^6 b_3^2 d_5 e_4^3 + m^7 b_3^2 d_5^2 e_4^3 - 2m^6 b_3^2 e_1 e_4^3 + 2m^7 b_3^2 d_5 e_1 e_4^3 + m^7 b_3^2 e_1^2 e_4^3 + m^7 b_3^2 b_7 e_4^4 = 0$$

$$S_{35}^8 : m^6 b_3^2 e_4^3 - 2m^7 b_3^2 d_5 e_4^3 + m^8 b_3^2 d_5^2 e_4^3 - 2m^7 b_3^2 e_1 e_4^3 + 2m^8 b_3^2 d_5 e_1 e_4^3 + m^8 b_3^2 e_1^2 e_4^3 + m^8 b_3^2 b_7 e_4^4 = 0$$

$$S_{36}^8 : m^6 b_3^3 e_4^3 - 2m^7 b_3^3 d_5 e_4^3 + m^8 b_3^3 d_5^2 e_4^3 - 2m^7 b_3^3 e_1 e_4^3 + 2m^8 b_3^3 d_5 e_1 e_4^3 + m^8 b_3^3 e_1^2 e_4^3 + m^8 b_3^3 b_7 e_4^4 = 0$$

$$S_{37}^8 : -2m^6 b_3^2 e_3 e_4^3 + 2m^7 b_3^2 d_5 e_3 e_4^3 + m^7 b_3^2 e_1 e_3 e_4^3 + m^7 b_3^2 b_9 e_4^4 = 0$$

$$S_{38}^8 : -2m^7 b_3^2 e_3 e_4^3 + 2m^8 b_3^2 d_5 e_3 e_4^3 + m^8 b_3^2 e_1 e_3 e_4^3 + m^8 b_3^2 b_9 e_4^4 = 0$$

$$S_{39}^8 : -2m^7 b_3^3 e_3 e_4^3 + 2m^8 b_3^3 d_5 e_3 e_4^3 + m^8 b_3^3 e_1 e_3 e_4^3 + m^8 b_3^3 b_9 e_4^4 = 0$$

$$S_{40}^8 : -(m^7 b_3^2 d_6 e_3 e_4^3) + 2m^6 b_3^2 e_4^4 - m^7 b_3^2 b_{10} e_4^4 - m^7 b_3^2 d_5 e_4^4 - m^7 b_3^2 e_1 e_4^4 = 0$$

$$S_{41}^8 : -(m^8 b_3^2 d_6 e_3 e_4^3) + 2m^7 b_3^2 e_4^4 - m^8 b_3^2 b_{10} e_4^4 - m^8 b_3^2 d_5 e_4^4 - m^8 b_3^2 e_1 e_4^4 = 0$$

$$S_{42}^8 : -(m^8 b_3^3 d_6 e_3 e_4^3) + 2m^7 b_3^3 e_4^4 - m^8 b_3^3 b_{10} e_4^4 - m^8 b_3^3 d_5 e_4^4 - m^8 b_3^3 e_1 e_4^4 = 0$$

$$S_{43}^8 : m^2 b_3 e_4 - 3m^3 b_3 d_5 e_4 + 3m^4 b_3 d_5^2 e_4 - m^5 b_3 d_5^3 e_4 - 2m^3 b_3 e_1 e_4 + 4m^4 b_3 d_5 e_1 e_4 - 2m^5 b_3 d_5^2 e_1 e_4 + m^4 b_3 e_1^2 e_4 - m^5 b_3 d_5 e_1^2 e_4 + m^4 b_3 b_7 e_4^2 - m^5 b_3 b_7 d_5 e_4^2 - m^5 b_3^2 e_4^2 f_1 = 0$$

$$S_{44}^8 : -(m^4 b_3^2 e_4^2) + 3m^5 b_3^2 d_5 e_4^2 - 3m^6 b_3^2 d_5^2 e_4^2 + m^7 b_3^2 d_5^3 e_4^2 + 2m^5 b_3^2 e_1 e_4^2 - 4m^6 b_3^2 d_5 e_1 e_4^2 + 2m^7 b_3^2 d_5^2 e_1 e_4^2 - m^6 b_3^2 e_1^2 e_4^2 + m^7 b_3^2 d_5 e_1^2 e_4^2 - m^6 b_3^2 b_7 e_4^3 + m^7 b_3^2 b_7 d_5 e_4^3 + m^7 b_3^3 e_4^3 f_1 = 0$$

$$S_{45}^8 : -(m^5 b_3^2 e_4^2) + 3m^6 b_3^2 d_5 e_4^2 - 3m^7 b_3^2 d_5^2 e_4^2 + m^8 b_3^2 d_5^3 e_4^2 + 2m^6 b_3^2 e_1 e_4^2 - 4m^7 b_3^2 d_5 e_1 e_4^2 + 2m^8 b_3^2 d_5^2 e_1 e_4^2 - m^7 b_3^2 e_1^2 e_4^2 + m^8 b_3^2 d_5 e_1^2 e_4^2 - m^7 b_3^2 b_7 e_4^3 + m^8 b_3^2 b_7 d_5 e_4^3 + m^8 b_3^3 e_4^3 f_1 = 0$$

$$S_{46}^8 : -(m^5 b_3^3 e_4^2) + 3m^6 b_3^3 d_5 e_4^2 - 3m^7 b_3^3 d_5^2 e_4^2 + m^8 b_3^3 d_5^3 e_4^2 + 2m^6 b_3^3 e_1 e_4^2 - 4m^7 b_3^3 d_5 e_1 e_4^2 + 2m^8 b_3^3 d_5^2 e_1 e_4^2 - m^7 b_3^3 e_1^2 e_4^2 + m^8 b_3^3 d_5 e_1^2 e_4^2 - m^7 b_3^3 b_7 e_4^3 + m^8 b_3^3 b_7 d_5 e_4^3 + m^8 b_3^4 e_4^3 f_1 = 0$$

S_{47}^8 : (demasiado grande ...)

S_{48}^8 : (demasiado grande ...)

S_{49}^8 : (demasiado grande ...)

$$S_{50}^8 : -(m^3 b_3 d_6 e_4) + 2m^4 b_3 d_5 d_6 e_4 - m^5 b_3 d_5^2 d_6 e_4 + 2m^4 b_3 d_6 e_1 e_4 - 2m^5 b_3 d_5 d_6 e_1 e_4 - m^5 b_3 d_6 e_1^2 e_4 - m^5 b_3 b_7 d_6 e_4^2 - m^5 b_3^2 e_4^2 f_2 = 0$$

$$S_{51}^8 : m^5 b_3^2 d_6 e_4^2 - 2m^6 b_3^2 d_5 d_6 e_4^2 + m^7 b_3^2 d_5^2 d_6 e_4^2 - 2m^6 b_3^2 d_6 e_1 e_4^2 + 2m^7 b_3^2 d_5 d_6 e_1 e_4^2 + m^7 b_3^2 d_6 e_1^2 e_4^2 + m^7 b_3^2 b_7 d_6 e_4^3 + m^7 b_3^3 e_4^3 f_2 = 0$$

$$S_{52}^8 : m^6 b_3^2 d_6 e_4^2 - 2m^7 b_3^2 d_5 d_6 e_4^2 + m^8 b_3^2 d_5^2 d_6 e_4^2 - 2m^7 b_3^2 d_6 e_1 e_4^2 + 2m^8 b_3^2 d_5 d_6 e_1 e_4^2 + m^8 b_3^2 d_6 e_1^2 e_4^2 + m^8 b_3^2 b_7 d_6 e_4^3 + m^8 b_3^3 e_4^3 f_2 = 0$$

$$S_{53}^8 : m^6 b_3^3 d_6 e_4^2 - 2m^7 b_3^3 d_5 d_6 e_4^2 + m^8 b_3^3 d_5^2 d_6 e_4^2 - 2m^7 b_3^3 d_6 e_1 e_4^2 + 2m^8 b_3^3 d_5 d_6 e_1 e_4^2 + m^8 b_3^3 d_6 e_1^2 e_4^2 + m^8 b_3^3 b_7 d_6 e_4^3 + m^8 b_3^4 e_4^3 f_2 = 0$$

S_{54}^8 : (demasiado grande ...)

S_{55}^8 : (demasiado grande ...)

S_{56}^8 : (demasiado grande ...)

S_{57}^8 : (demasiado grande ...)

S_{58}^8 : (demasiado grande ...)

S_{59}^8 : (demasiado grande ...)

Sucesión característica (5, 2, 1)

Etapas 4BB1B

Relaciones

$$R_1: b_3 \neq 0$$

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_3 X_5$$

$$[X_3, X_7] = b_7 X_4 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + b_7 X_5 + b_3 X_7$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_4$$

$$[X_6, X_7] = -(d_6 X_2) + e_1 X_4$$

$$[X_6, X_8] = e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & -d_6 & 0 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (5, 2, 1)

Etapas 4BB1C

Relaciones

$$R_1: e_4 \neq 0$$

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_3, X_7] = b_7 X_4$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + b_7 X_5$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_4$$

$$[X_6, X_7] = -(d_6 X_2) + e_1 X_4$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_6 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_6 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & 0 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -e_4 & 0 \\ 0 & 0 & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -(d_5 + e_1) & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Sucesión característica (5, 2, 1)

Etapa 4BB2

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_7] = b_5 X_4$$

$$[X_2, X_8] = a_{11} X_4 + b_5 X_5$$

$$[X_3, X_6] = b_5 X_4$$

$$[X_3, X_7] = b_7 X_4 + 2b_5 X_5$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + (a_{11} + b_7) X_5 + 3b_5 X_6$$

$$[X_5, X_8] = d_5 X_4$$

$$[X_6, X_7] = e_1 X_4$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_5 & a_{11} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_5 & b_7 & b_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 2b_5 & a_{11} + b_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 3b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & e_4 \\ 0 & -b_5 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & -2b_5 & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & 0 & -e_4 & -f_2 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -e_4 & 0 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 & 0 \\ 0 & -b_5 & -(a_{11} + b_7) & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 & 0 \\ 0 & 0 & -3b_5 & 0 & 0 & 0 & -(d_5 + e_1) & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : b_5 b_{10} - b_5 d_5 + 4b_5 e_1 = 0$$

Sucesión Característica de $\text{adj}_{X_1+mX_8}$

$$S_1^8 : 3m^4 b_5^2 e_4^2 = 0$$

$$S_2^8 : -3m^5 b_5^2 e_4^2 = 0$$

$$S_3^8 : -9m^7 b_5^3 e_4^4 = 0$$

$$S_4^8 : 9m^7 b_5^3 e_4^4 = 0$$

$$S_5^8 : -9m^8 b_5^3 e_4^4 = 0$$

$$S_6^8 : 9m^8 b_5^3 e_4^4 = 0$$

$$S_7^8 : -27m^8 b_5^4 e_4^4 = 0$$

$$S_8^8 : 27m^9 b_5^4 e_4^4 = 0$$

$$S_9^8 : 5m^2b_5e_4 - m^3b_5b_{10}e_4 - 9m^3b_5d_5e_4 + m^4b_5b_{10}d_5e_4 + 4m^4b_5d_5^2e_4 - 4m^3b_5e_1e_4 + 4m^4b_5d_5e_1e_4 + 3m^4a_{11}b_5e_4^2 = 0$$

$$S_{10}^8 : -5m^3b_5e_4 + m^4b_5b_{10}e_4 + 9m^4b_5d_5e_4 - m^5b_5b_{10}d_5e_4 - 4m^5b_5d_5^2e_4 + 4m^4b_5e_1e_4 - 4m^5b_5d_5e_1e_4 - 3m^5a_{11}b_5e_4^2 = 0$$

$$S_{11}^8 : 3m^4b_5^2e_4^2 - 3m^5b_5^2d_5e_4^2 = 0$$

$$S_{12}^8 : 3m^5b_5^2e_4^2 - 3m^6b_5^2d_5e_4^2 = 0$$

$$S_{13}^8 : -15m^5b_5^3e_4^2 + 3m^6b_5^3b_{10}e_4^2 + 27m^6b_5^3d_5e_4^2 - 3m^7b_5^3b_{10}d_5e_4^2 - 12m^7b_5^3d_5^2e_4^2 + 12m^6b_5^3e_1e_4^2 - 12m^7b_5^3d_5e_1e_4^2 = 0$$

$$S_{14}^8 : 3m^5b_5^3e_4^2 - 6m^6b_5^3d_5e_4^2 + 3m^7b_5^3d_5^2e_4^2 - 3m^6b_5^3e_1e_4^2 + 3m^7b_5^3d_5e_1e_4^2 = 0$$

$$S_{15}^8 : 12m^5b_5^3e_4^2 - 3m^6b_5^3b_{10}e_4^2 - 21m^6b_5^3d_5e_4^2 + 3m^7b_5^3b_{10}d_5e_4^2 + 9m^7b_5^3d_5^2e_4^2 - 9m^6b_5^3e_1e_4^2 + 9m^7b_5^3d_5e_1e_4^2 = 0$$

$$S_{16}^8 : -15m^6b_5^3e_4^2 + 3m^7b_5^3b_{10}e_4^2 + 27m^7b_5^3d_5e_4^2 - 3m^8b_5^3b_{10}d_5e_4^2 - 12m^8b_5^3d_5^2e_4^2 + 12m^7b_5^3e_1e_4^2 - 12m^8b_5^3d_5e_1e_4^2 = 0$$

$$S_{17}^8 : 3m^6b_5^3e_4^2 - 6m^7b_5^3d_5e_4^2 + 3m^8b_5^3d_5^2e_4^2 - 3m^7b_5^3e_1e_4^2 + 3m^8b_5^3d_5e_1e_4^2 = 0$$

$$S_{18}^8 : 12m^6b_5^3e_4^2 - 3m^7b_5^3b_{10}e_4^2 - 21m^7b_5^3d_5e_4^2 + 3m^8b_5^3b_{10}d_5e_4^2 + 9m^8b_5^3d_5^2e_4^2 - 9m^7b_5^3e_1e_4^2 + 9m^8b_5^3d_5e_1e_4^2 = 0$$

$$S_{19}^8 : -3m^6b_5^3e_4^3 + 3m^7b_5^3d_5e_4^3 = 0$$

$$S_{20}^8 : -9m^6b_5^3e_4^3 + 9m^7b_5^3d_5e_4^3 = 0$$

$$S_{21}^8 : -3m^7b_5^3e_4^3 + 3m^8b_5^3d_5e_4^3 = 0$$

$$S_{22}^8 : -9m^7b_5^3e_4^3 + 9m^8b_5^3d_5e_4^3 = 0$$

$$S_{23}^8 : 9m^7b_5^4e_4^3 - 9m^8b_5^4d_5e_4^3 = 0$$

$$S_{24}^8 : -9m^7b_5^4e_4^3 + 9m^8b_5^4d_5e_4^3 = 0$$

$$S_{25}^8 : -9m^8b_5^4e_4^3 + 9m^9b_5^4d_5e_4^3 = 0$$

$$S_{26}^8 : -2m^5b_5^2e_4^3 + m^6b_5^2b_{10}e_4^3 + 3m^6b_5^2d_5e_4^3 - m^7b_5^2b_{10}d_5e_4^3 - m^7b_5^2d_5^2e_4^3 + m^6b_5^2e_1e_4^3 - m^7b_5^2d_5e_1e_4^3 = 0$$

$$S_{27}^8 : -2m^6b_5^2e_4^3 + m^7b_5^2b_{10}e_4^3 + 3m^7b_5^2d_5e_4^3 - m^8b_5^2b_{10}d_5e_4^3 - m^8b_5^2d_5^2e_4^3 + m^7b_5^2e_1e_4^3 - m^8b_5^2d_5e_1e_4^3 = 0$$

$$S_{28}^8 : -6m^6b_5^3e_4^3 + 3m^7b_5^3b_{10}e_4^3 + 9m^7b_5^3d_5e_4^3 - 3m^8b_5^3b_{10}d_5e_4^3 - 3m^8b_5^3d_5^2e_4^3 + 3m^7b_5^3e_1e_4^3 - 3m^8b_5^3d_5e_1e_4^3 = 0$$

$$S_{29}^8 : 15m^6b_5^3e_4^3 - 3m^7b_5^3b_{10}e_4^3 - 27m^7b_5^3d_5e_4^3 + 3m^8b_5^3b_{10}d_5e_4^3 + 12m^8b_5^3d_5^2e_4^3 - 12m^7b_5^3e_1e_4^3 + 12m^8b_5^3d_5e_1e_4^3 = 0$$

$$S_{30}^8 : -15m^7b_5^3e_4^3 + 3m^8b_5^3b_{10}e_4^3 + 27m^8b_5^3d_5e_4^3 - 3m^9b_5^3b_{10}d_5e_4^3 - 12m^9b_5^3d_5^2e_4^3 + 12m^8b_5^3e_1e_4^3 - 12m^9b_5^3d_5e_1e_4^3 = 0$$

$$S_{31}^8 : 6m^7b_5^3e_4^3 - 3m^8b_5^3b_{10}e_4^3 - 9m^8b_5^3d_5e_4^3 + 3m^9b_5^3b_{10}d_5e_4^3 + 3m^9b_5^3d_5^2e_4^3 - 3m^8b_5^3e_1e_4^3 + 3m^9b_5^3d_5e_1e_4^3 = 0$$

$$S_{32}^8 : 12m^4b_5^2e_4^2 - 3m^5b_5^2b_{10}e_4^2 - 33m^5b_5^2d_5e_4^2 + 6m^6b_5^2b_{10}d_5e_4^2 + 30m^6b_5^2d_5^2e_4^2 - 3m^7b_5^2b_{10}d_5^2e_4^2 - 9m^7b_5^2d_5^3e_4^2 - 21m^5b_5^2e_1e_4^2 + 3m^6b_5^2b_{10}e_1e_4^2 + 39m^6b_5^2d_5e_1e_4^2 - 3m^7b_5^2b_{10}d_5e_1e_4^2 - 18m^7b_5^2d_5^2e_1e_4^2 + 9m^6b_5^2e_1^2e_4^2 - 9m^7b_5^2d_5e_1^2e_4^2 + 6m^6a_{11}b_5^2e_4^3 - 3m^6b_5^2b_7e_4^3 - 6m^7a_{11}b_5^2d_5e_4^3 + 3m^7b_5^2b_7d_5e_4^3 - 9m^7a_{11}b_5^2e_1e_4^3 + 9m^7b_5^3e_3e_4^3 = 0$$

$$S_{33}^8 : 12m^5b_5^2e_4^2 - 3m^6b_5^2b_{10}e_4^2 - 33m^6b_5^2d_5e_4^2 + 6m^7b_5^2b_{10}d_5e_4^2 + 30m^7b_5^2d_5^2e_4^2 - 3m^8b_5^2b_{10}d_5^2e_4^2 - 9m^8b_5^2d_5^3e_4^2 - 21m^6b_5^2e_1e_4^2 + 3m^7b_5^2b_{10}e_1e_4^2 + 39m^7b_5^2d_5e_1e_4^2 - 3m^8b_5^2b_{10}d_5e_1e_4^2 - 18m^8b_5^2d_5^2e_1e_4^2 + 9m^7b_5^2e_1^2e_4^2 - 9m^8b_5^2d_5e_1^2e_4^2 + 6m^7a_{11}b_5^2e_4^3 - 3m^7b_5^2b_7e_4^3 - 6m^8a_{11}b_5^2d_5e_4^3 + 3m^8b_5^2b_7d_5e_4^3 - 9m^8a_{11}b_5^2e_1e_4^3 + 9m^8b_5^3e_3e_4^3 = 0$$

$$S_{34}^8 : -9m^5b_5^2e_4^3 + 18m^6b_5^2d_5e_4^3 - 9m^7b_5^2d_5^2e_4^3 + 9m^6b_5^2e_1e_4^3 - 9m^7b_5^2d_5e_1e_4^3 - 9m^7a_{11}b_5^2e_4^4 = 0$$

$$S_{35}^8 : 15m^5b_5^2e_4^3 - 3m^6b_5^2b_{10}e_4^3 - 27m^6b_5^2d_5e_4^3 + 3m^7b_5^2b_{10}d_5e_4^3 + 12m^7b_5^2d_5^2e_4^3 - 12m^6b_5^2e_1e_4^3 + 12m^7b_5^2d_5e_1e_4^3 + 9m^7a_{11}b_5^2e_4^4 = 0$$

$$S_{36}^8 : -9m^6b_5^2e_4^3 + 18m^7b_5^2d_5e_4^3 - 9m^8b_5^2d_5^2e_4^3 + 9m^7b_5^2e_1e_4^3 - 9m^8b_5^2d_5e_1e_4^3 - 9m^8a_{11}b_5^2e_4^4 = 0$$

$$S_{37}^8 : 15m^6b_5^2e_4^3 - 3m^7b_5^2b_{10}e_4^3 - 27m^7b_5^2d_5e_4^3 + 3m^8b_5^2b_{10}d_5e_4^3 + 12m^8b_5^2d_5^2e_4^3 - 12m^7b_5^2e_1e_4^3 + 12m^8b_5^2d_5e_1e_4^3 + 9m^8a_{11}b_5^2e_4^4 = 0$$

$$S_{38}^8 : -36m^6b_5^3e_4^3 + 9m^7b_5^3b_{10}e_4^3 + 63m^7b_5^3d_5e_4^3 - 9m^8b_5^3b_{10}d_5e_4^3 - 27m^8b_5^3d_5^2e_4^3 + 27m^7b_5^3e_1e_4^3 - 27m^8b_5^3d_5e_1e_4^3 - 27m^8a_{11}b_5^3e_4^4 = 0$$

$$S_{39}^8 : 36m^7b_5^3e_4^3 - 9m^8b_5^3b_{10}e_4^3 - 63m^8b_5^3d_5e_4^3 + 9m^9b_5^3b_{10}d_5e_4^3 + 27m^9b_5^3d_5^2e_4^3 - 27m^8b_5^3e_1e_4^3 + 27m^9b_5^3d_5e_1e_4^3 + 27m^9a_{11}b_5^3e_4^4 = 0$$

$$S_{40}^8 : 9m^7b_5^3e_4^4 - 9m^8b_5^3d_5e_4^4 = 0$$

$$S_{41}^8 : -9m^8b_5^3e_4^4 + 9m^9b_5^3d_5e_4^4 = 0$$

$$S_{42}^8 : -9m^8b_5^4e_4^4 + 9m^9b_5^4d_5e_4^4 = 0$$

$$S_{43}^8 : (\text{demasiado grande ...})$$

$$S_{44}^8 : (\text{demasiado grande ...})$$

$$S_{45}^8 : 2m^4b_5^2e_4^2 - m^5b_5^2b_{10}e_4^2 - 5m^5b_5^2d_5e_4^2 + 2m^6b_5^2b_{10}d_5e_4^2 + 4m^6b_5^2d_5^2e_4^2 - m^7b_5^2b_{10}d_5^2e_4^2 - m^7b_5^2d_5^3e_4^2 - 3m^5b_5^2e_1e_4^2 + m^6b_5^2b_{10}e_1e_4^2 + 5m^6b_5^2d_5e_1e_4^2 - m^7b_5^2b_{10}d_5e_1e_4^2 - 2m^7b_5^2d_5^2e_1e_4^2 + m^6b_5^2e_1^2e_4^2 - m^7b_5^2d_5e_1^2e_4^2 - 3m^6b_5^3e_4^2f_2 + 3m^7b_5^3d_5e_4^2f_2 = 0$$

$$S_{46}^8 : 5m^4b_5^2e_4^2 - 6m^5b_5^2b_{10}e_4^2 + m^6b_5^2b_{10}^2e_4^2 - 9m^5b_5^2d_5e_4^2 + 10m^6b_5^2b_{10}d_5e_4^2 - m^7b_5^2b_{10}^2d_5e_4^2 + 4m^6b_5^2d_5^2e_4^2 - 4m^7b_5^2b_{10}d_5^2e_4^2 - 4m^5b_5^2e_1e_4^2 + 4m^6b_5^2b_{10}e_1e_4^2 + 4m^6b_5^2d_5e_1e_4^2 - 4m^7b_5^2b_{10}d_5e_1e_4^2 - 3m^6a_{11}b_5^2e_4^3 - 3m^6b_5^2b_7e_4^3 + 3m^7a_{11}b_5^2d_5e_4^3 + 3m^7b_5^2b_7d_5e_4^3 - 3m^6b_5^3e_4^2f_2 + 3m^7b_5^3d_5e_4^2f_2 = 0$$

$$S_{47}^8 : 22m^4b_5^2e_4^2 - 10m^5b_5^2b_{10}e_4^2 + m^6b_5^2b_{10}^2e_4^2 - 56m^5b_5^2d_5e_4^2 + 18m^6b_5^2b_{10}d_5e_4^2 - m^7b_5^2b_{10}^2d_5e_4^2 + 47m^6b_5^2d_5^2e_4^2 - 8m^7b_5^2b_{10}d_5^2e_4^2 - 13m^7b_5^2d_5^3e_4^2 - 34m^5b_5^2e_1e_4^2 + 8m^6b_5^2b_{10}e_1e_4^2 + 60m^6b_5^2d_5e_1e_4^2 - 8m^7b_5^2b_{10}d_5e_1e_4^2 - 26m^7b_5^2d_5^2e_1e_4^2 + 13m^6b_5^2e_1^2e_4^2 - 13m^7b_5^2d_5e_1^2e_4^2 + 6m^6a_{11}b_5^2e_4^3 - 3m^6b_5^2b_7e_4^3 - 6m^7a_{11}b_5^2d_5e_4^3 + 3m^7b_5^2b_7d_5e_4^3 - 9m^7a_{11}b_5^2e_1e_4^3 + 9m^7b_5^3e_3e_4^3 - 3m^6b_5^3e_4^2f_2 + 3m^7b_5^3d_5e_4^2f_2 = 0$$

$$S_{48}^8 : 2m^5b_5^2e_4^2 - m^6b_5^2b_{10}e_4^2 - 5m^6b_5^2d_5e_4^2 + 2m^7b_5^2b_{10}d_5e_4^2 + 4m^7b_5^2d_5^2e_4^2 - m^8b_5^2b_{10}d_5^2e_4^2 - m^8b_5^2d_5^3e_4^2 - 3m^6b_5^2e_1e_4^2 + m^7b_5^2b_{10}e_1e_4^2 + 5m^7b_5^2d_5e_1e_4^2 - m^8b_5^2b_{10}d_5e_1e_4^2 - 2m^8b_5^2d_5^2e_1e_4^2 + m^7b_5^2e_1^2e_4^2 - m^8b_5^2d_5e_1^2e_4^2 - 3m^7b_5^3e_4^2f_2 + 3m^8b_5^3d_5e_4^2f_2 = 0$$

$$S_{49}^8 : 5m^5b_5^2e_4^2 - 6m^6b_5^2b_{10}e_4^2 + m^7b_5^2b_{10}^2e_4^2 - 9m^6b_5^2d_5e_4^2 + 10m^7b_5^2b_{10}d_5e_4^2 - m^8b_5^2b_{10}^2d_5e_4^2 + 4m^7b_5^2d_5^2e_4^2 - 4m^8b_5^2b_{10}d_5^2e_4^2 - 4m^6b_5^2e_1e_4^2 + 4m^7b_5^2b_{10}e_1e_4^2 + 4m^7b_5^2d_5e_1e_4^2 - 4m^8b_5^2b_{10}d_5e_1e_4^2 - 3m^7a_{11}b_5^2e_4^3 - 3m^7b_5^2b_7e_4^3 + 3m^8a_{11}b_5^2d_5e_4^3 + 3m^8b_5^2b_7d_5e_4^3 - 3m^7b_5^3e_4^2f_2 + 3m^8b_5^3d_5e_4^2f_2 = 0$$

$$S_{50}^8 : 22m^5b_5^2e_4^2 - 10m^6b_5^2b_{10}e_4^2 + m^7b_5^2b_{10}^2e_4^2 - 56m^6b_5^2d_5e_4^2 + 18m^7b_5^2b_{10}d_5e_4^2 - m^8b_5^2b_{10}^2d_5e_4^2 + 47m^7b_5^2d_5^2e_4^2 - 8m^8b_5^2b_{10}d_5^2e_4^2 - 13m^8b_5^2d_5^3e_4^2 - 34m^6b_5^2e_1e_4^2 + 8m^7b_5^2b_{10}e_1e_4^2 + 60m^7b_5^2d_5e_1e_4^2 - 8m^8b_5^2b_{10}d_5e_1e_4^2 - 26m^8b_5^2d_5^2e_1e_4^2 + 13m^7b_5^2e_1^2e_4^2 - 13m^8b_5^2d_5e_1^2e_4^2 + 6m^7a_{11}b_5^2e_4^3 - 3m^7b_5^2b_7e_4^3 - 6m^8a_{11}b_5^2d_5e_4^3 + 3m^8b_5^2b_7d_5e_4^3 - 9m^8a_{11}b_5^2e_1e_4^3 + 9m^8b_5^3e_3e_4^3 - 3m^7b_5^3e_4^2f_2 + 3m^8b_5^3d_5e_4^2f_2 = 0$$

$$S_{51}^8 : -51m^5b_5^3e_4^2 + 27m^6b_5^3b_{10}e_4^2 - 3m^7b_5^3b_{10}^2e_4^2 + 126m^6b_5^3d_5e_4^2 - 48m^7b_5^3b_{10}d_5e_4^2 + 3m^8b_5^3b_{10}^2d_5e_4^2 - 102m^7b_5^3d_5^2e_4^2 + 21m^8b_5^3b_{10}d_5^2e_4^2 + 27m^8b_5^3d_5^3e_4^2 + 75m^6b_5^3e_1e_4^2 - 21m^7b_5^3b_{10}e_1e_4^2 - 129m^7b_5^3d_5e_1e_4^2 + 21m^8b_5^3b_{10}d_5e_1e_4^2 + 54m^8b_5^3d_5^2e_1e_4^2 - 27m^7b_5^3e_1^2e_4^2 + 27m^8b_5^3d_5e_1^2e_4^2 - 18m^7a_{11}b_5^3e_4^3 + 9m^7b_5^3b_7e_4^3 + 18m^8a_{11}b_5^3d_5e_4^3 - 9m^8b_5^3b_7d_5e_4^3 + 27m^8a_{11}b_5^3e_1e_4^3 - 27m^8b_5^4e_3e_4^3 + 9m^7b_5^4e_4^2f_2 - 9m^8b_5^4d_5e_4^2f_2 = 0$$

$$S_{52}^8 : 51m^6b_5^3e_4^2 - 27m^7b_5^3b_{10}e_4^2 + 3m^8b_5^3b_{10}^2e_4^2 - 126m^7b_5^3d_5e_4^2 + 48m^8b_5^3b_{10}d_5e_4^2 - 3m^9b_5^3b_{10}^2d_5e_4^2 + 102m^8b_5^3d_5^2e_4^2 - 21m^9b_5^3b_{10}d_5^2e_4^2 - 27m^9b_5^3d_5^3e_4^2 - 75m^7b_5^3e_1e_4^2 + 21m^8b_5^3b_{10}e_1e_4^2 + 129m^8b_5^3d_5e_1e_4^2 - 21m^9b_5^3b_{10}d_5e_1e_4^2 - 54m^9b_5^3d_5^2e_1e_4^2 + 27m^8b_5^3e_1^2e_4^2 - 27m^9b_5^3d_5e_1^2e_4^2 + 18m^8a_{11}b_5^3e_4^3 - 9m^8b_5^3b_7e_4^3 - 18m^9a_{11}b_5^3d_5e_4^3 + 9m^9b_5^3b_7d_5e_4^3 - 27m^9a_{11}b_5^3e_1e_4^3 + 27m^9b_5^4e_3e_4^3 - 9m^8b_5^4e_4^2f_2 + 9m^9b_5^4d_5e_4^2f_2 = 0$$

S_{53}^8 : (demasiado grande ...)

S_{54}^8 : (demasiado grande ...)

S_{55}^8 : (demasiado grande ...)

S_{56}^8 : (demasiado grande ...)

S_{57}^8 : (demasiado grande ...)

S_{58}^8 : (demasiado grande ...)

$$S_{59}^8 : -7m^5b_5^2e_4^3 + 7m^6b_5^2b_{10}e_4^3 - m^7b_5^2b_{10}^2e_4^3 + 14m^6b_5^2d_5e_4^3 - 12m^7b_5^2b_{10}d_5e_4^3 + m^8b_5^2b_{10}^2d_5e_4^3 - 8m^7b_5^2d_5^2e_4^3 + 5m^8b_5^2b_{10}d_5^2e_4^3 + m^8b_5^2d_5^3e_4^3 + 7m^6b_5^2e_1e_4^3 - 5m^7b_5^2b_{10}e_1e_4^3 - 9m^7b_5^2d_5e_1e_4^3 + 5m^8b_5^2b_{10}d_5e_1e_4^3 + 2m^8b_5^2d_5^2e_1e_4^3 - m^7b_5^2e_1^2e_4^3 + m^8b_5^2d_5e_1^2e_4^3 + 3m^7a_{11}b_5^2e_4^4 + 3m^7b_5^2b_7e_4^4 - 3m^8a_{11}b_5^2d_5e_4^4 - 3m^8b_5^2b_7d_5e_4^4 + 3m^7b_5^3e_4^3f_2 - 3m^8b_5^3d_5e_4^3f_2 = 0$$

$$S_{60}^8 : 7m^6b_5^2e_4^3 - 7m^7b_5^2b_{10}e_4^3 + m^8b_5^2b_{10}^2e_4^3 - 14m^7b_5^2d_5e_4^3 + 12m^8b_5^2b_{10}d_5e_4^3 - m^9b_5^2b_{10}^2d_5e_4^3 + 8m^8b_5^2d_5^2e_4^3 - 5m^9b_5^2b_{10}d_5^2e_4^3 - m^9b_5^2d_5^3e_4^3 - 7m^7b_5^2e_1e_4^3 + 5m^8b_5^2b_{10}e_1e_4^3 + 9m^8b_5^2d_5e_1e_4^3 - 5m^9b_5^2b_{10}d_5e_1e_4^3 - 2m^9b_5^2d_5^2e_1e_4^3 + m^8b_5^2e_1^2e_4^3 - m^9b_5^2d_5e_1^2e_4^3 - 3m^8a_{11}b_5^2e_4^4 - 3m^8b_5^2b_7e_4^4 + 3m^9a_{11}b_5^2d_5e_4^4 + 3m^9b_5^2b_7d_5e_4^4 - 3m^8b_5^3e_4^3f_2 + 3m^9b_5^3d_5e_4^3f_2 = 0$$

Sucesión característica (5, 2, 1)

Etapa 4BB3

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_5, X_8] = d_5 X_4$$

$$[X_6, X_7] = e_1 X_4$$

$$[X_6, X_8] = e_3 X_4 + (d_5 + e_1) X_5$$

$$[X_7, X_8] = f_2 X_2 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_9 & -b_7 & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} & 0 & 0 & 0 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & 0 & -(d_5 + e_1) & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & 0 & -(d_5 + e_1) & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : a_9 b_{10} - a_9 d_5 + 2a_9 e_1 + 2b_5 e_1 - a_1 f_2 = 0$$

Sucesión característica (5, 2, 1)

Etapa 4BBX

Ley del Álgebra

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_{11} X_4 + a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = \left(b_{10} - \frac{a_1 f_2}{b_5} \right) X_2 + b_9 X_4 + (a_{11} + b_7) X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_5, X_8] = d_5 X_4$$

$$[X_6, X_7] = \left(e_1 + \frac{a_1 f_2}{2b_5} \right) X_4$$

$$[X_6, X_8] = e_3 X_4 + \left(d_5 + e_1 + \frac{a_1 f_2}{2b_5} \right) X_5$$

$$[X_7, X_8] = f_2 X_2 + f_1 X_4 + e_3 X_5 + \left(d_5 + e_1 + \frac{a_1 f_2}{2b_5} \right) X_6$$

Adjuntas

$$\text{adj}_{X_1} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_2} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_9 & a_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_3} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{10} - \frac{a_1 f_2}{b_5} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_1 & 0 & 0 & b_3 & b_5 & b_7 & b_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & b_3 & a_9 + b_5 & a_{11} + b_7 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 2a_9 + b_5 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_4} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_5} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_6} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_5 & 0 & 0 & 0 & e_1 + \frac{a_1 f_2}{2b_5} & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 + \frac{a_1 f_2}{2b_5} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_7} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & f_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_9 & -b_7 & 0 & 0 & -e_1 - \frac{a_1 f_2}{2b_5} & 0 & f_1 \\ 0 & 0 & -(a_9 + b_5) & 0 & 0 & 0 & 0 & e_3 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & d_5 + e_1 + \frac{a_1 f_2}{2b_5} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}_{X_8} = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_{10} + \frac{a_1 f_2}{b_5} & 0 & 0 & 0 & 0 & -f_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{11} & -b_9 & 0 & -d_5 & -e_3 & 0 & -f_1 & 0 \\ 0 & -a_9 & -(a_{11} + b_7) & 0 & 0 & -d_5 - e_1 - \frac{a_1 f_2}{2b_5} & 0 & -e_3 & 0 \\ 0 & 0 & -2a_9 - b_5 & 0 & 0 & 0 & 0 & -d_5 - e_1 - \frac{a_1 f_2}{2b_5} & 0 \\ -1 & 0 & -b_3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

Jacobi

$$J_1 : a_9 b_{10} - a_9 d_5 + 2a_9 e_1 + 2b_5 e_1 = 0$$

SUCESIÓN CARACTERÍSTICA (5, 2, 1)
ETAPA 4PR ()

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_5] = X_4$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_4$$

$$[X_2, X_7] = a_9 X_4$$

$$[X_2, X_8] = a_9 X_5$$

$$[X_3, X_5] = b_3 X_4$$

$$[X_3, X_6] = b_5 X_4 + b_3 X_5$$

$$[X_3, X_7] = \frac{5d_3 X_2}{3} + b_7 X_4 + (a_9 + b_5) X_5 + b_3 X_6$$

$$[X_3, X_8] = b_{10} X_2 + \frac{5d_3 X_3}{3} + b_9 X_4 + b_7 X_5 + (2a_9 + b_5) X_6 + b_3 X_7$$

$$[X_4, X_8] = -2d_4 X_2 - \frac{5d_3 X_4}{3}$$

$$[X_5, X_7] = d_4 X_2 + d_3 X_4$$

$$[X_5, X_8] = d_6 X_2 - d_4 X_3 + d_5 X_4 - \frac{2d_3 X_5}{3}$$

$$[X_6, X_7] = -(d_6 X_2) + d_4 X_3 + e_1 X_4 + d_3 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_3 X_4 + (d_5 + e_1) X_5 + \frac{d_3 X_6}{3}$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + f_1 X_4 + e_3 X_5 + (d_5 + e_1) X_6 + \frac{d_3 X_7}{3}$$

RELACIONES

$R_1: d_4 \neq 0$

$a_1 d_4 \rightarrow 0$

$a_9 d_4 \rightarrow 0$

$b_3 d_4 \rightarrow 0$

$a_1 d_6 \rightarrow 0$

$b_5 d_4 \rightarrow 0$

$\frac{5b_3 d_3}{3} \rightarrow 0$

$\frac{-2a_1 d_3}{3} \rightarrow 0$

$0 \rightarrow 0$

JACOBI

$J_1: \frac{10a_1 d_3}{3} = 0$

$J_2: 3a_9 d_3 + \frac{11b_3 d_3}{3} = 0$

$J_3: -(b_{10} d_4) + d_4 d_5 - \frac{5d_3 d_6}{3} + 3d_4 e_1 = 0$

$J_4: \frac{11b_3 d_3}{3} - a_1 e_4 = 0$

$J_5: 3a_9 d_3 + a_1 e_4 = 0$

$J_6: \frac{4d_3^2}{3} - b_7 d_4 + a_9 d_6 - b_3 e_4 = 0$

$J_7: \frac{10d_3^2}{3} + 3b_7 d_4 - 3a_9 d_6 - 2b_5 d_6 - b_3 e_4 = 0$

$J_8: -(b_9 d_4) + \frac{10d_3 e_1}{3} + a_9 e_4 - b_5 e_4 = 0$

$J_9: a_9 b_{10} + \frac{14b_7 d_3}{3} - a_9 d_5 + 2a_9 e_1 + 2b_5 e_1 - a_1 f_2 = 0$

NILPOTENCIA

$N_1: \frac{-28d_3^2}{9} + b_7 d_4 - a_9 d_6 - b_3 e_4 = 0$

$N_2: \frac{-2d_3^3}{27} - b_7 d_3 d_4 - \frac{2a_9 d_3 d_6}{3} + 2b_3 d_3 e_4 = 0$

$N_3: \frac{25d_3^4}{27} - b_7 d_3^2 d_4 - 2a_9 b_9 d_4^2 + \frac{8a_9 d_3^2 d_6}{3} - \frac{b_3 d_3^2 e_4}{3} + 2a_9^2 d_4 e_4 + a_9 b_3 d_6 e_4 = 0$

$N_4: \frac{50d_3^5}{243} - \frac{5b_7 d_3^3 d_4}{27} - \frac{4a_9 b_9 d_3 d_4^2}{3} + \frac{50a_9 d_3^3 d_6}{27} + 4a_9^2 d_4^2 e_3 + 2a_9 b_5 d_4^2 e_3 - \frac{10b_3 d_3^3 e_4}{27} - \frac{8a_9^2 d_3 d_4 e_4}{3} - \frac{4a_9 b_3 d_3 d_6 e_4}{3} + 2a_9 b_3 d_4^2 f_1 = 0$

$N_5: \frac{-2a_9 b_9 d_3^2 d_4^2}{9} + \frac{25a_9 d_3^4 d_6}{81} + \frac{4a_9^2 d_3 d_4^2 e_3}{3} + \frac{2a_9 b_5 d_3 d_4^2 e_3}{3} - 2a_9 b_3 d_4^2 d_5 e_3 - 2a_9 b_3 d_4^2 e_1 e_3 - \frac{10a_9^2 d_3^2 d_4 e_4}{9} - \frac{5a_9 b_3 d_3^2 d_6 e_4}{9} + \frac{2a_9 b_3 d_3 d_4^2 f_1}{3} = 0$

SUCESISN CHARACTERMSTICA (5, 1, 1, 1)
ETAPA 1

LEY DEL ÁLGEBRA

$$[x_1, x_5] = x_4$$

$$[x_1, x_6] = x_5$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_3] = a_1 x_4$$

$$[x_2, x_7] = a_{13} x_4$$

$$[x_2, x_8] = a_{18} x_2 + a_{17} x_3 + a_{16} x_4 + a_{13} x_5$$

$$[x_3, x_6] = b_7 x_4$$

$$[x_3, x_7] = b_{10} x_4 + b_7 x_5$$

$$[x_3, x_8] = b_{15} x_2 + b_{14} x_3 + b_{13} x_4 + b_{10} x_5 + b_7 x_6$$

$$[x_5, x_8] = d_9 x_2 + d_8 x_3$$

$$[x_6, x_7] = -(d_9 x_2) - d_8 x_3 + e_1 x_4$$

$$[x_6, x_8] = e_4 x_4 + e_1 x_5$$

$$[x_7, x_8] = f_3 x_2 + f_2 x_3 + f_1 x_4 + e_4 x_5 + e_1 x_6$$

ADJUNTAS

$$\text{adj}(x_1) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_2) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{18} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{17} \\ 0 & 0 & a_1 & 0 & 0 & 0 & a_{13} & a_{16} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{13} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_3) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{15} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_{14} \\ 0 & -a_1 & 0 & 0 & 0 & b_7 & b_{10} & b_{13} \\ 0 & 0 & 0 & 0 & 0 & 0 & b_7 & b_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & b_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_4) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_5) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_8 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_6) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_9 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -d_8 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & 0 & e_1 & e_4 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_7) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & d_9 & 0 & f_3 \\ 0 & 0 & 0 & 0 & 0 & d_8 & 0 & f_2 \\ 0 & -a_{13} & -b_{10} & 0 & 0 & -e_1 & 0 & f_1 \\ 0 & 0 & -b_7 & 0 & 0 & 0 & 0 & e_4 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_8) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{18} & -b_{15} & 0 & -d_9 & 0 & -f_3 & 0 \\ 0 & -a_{17} & -b_{14} & 0 & -d_8 & 0 & -f_2 & 0 \\ 0 & -a_{16} & -b_{13} & 0 & 0 & -e_4 & -f_1 & 0 \\ 0 & -a_{13} & -b_{10} & 0 & 0 & -e_1 & -e_4 & 0 \\ 0 & 0 & -b_7 & 0 & 0 & 0 & -e_1 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

BASE DE GROEBNER DE LAS RELACIONES OBTENIDAS (J,N,S1)

$$G_1 : b_{15} d_8 - b_{14} d_9 = 0$$

$$G_2 : b_7 d_9 = 0$$

$$G_3 : b_7 d_8 = 0$$

$$G_4 : b_7 b_{14} = 0$$

$$G_5 : b_7^2 f_2 = 0$$

$$G_6 : a_{18} + b_{14} = 0$$

$$G_7 : b_{14} d_8 + a_{17} d_9 = 0$$

$$G_8 : -b_{14}^2 - a_{17} b_{15} = 0$$

$$G_9 : a_{17} b_7 = 0$$

$$G_{10} : b_{13} d_8 + a_{16} d_9 - b_7 f_2 = 0$$

$$G_{11} : -(b_{13} b_{14} d_8) - a_{16} b_{15} d_8 = 0$$

$$G_{12} : -(a_{17} b_{13} d_8) + a_{16} b_{14} d_8 = 0$$

$$G_{13} : -(b_{10} d_8) - a_{13} d_9 = 0$$

$$G_{14} : -(b_{10} b_{14} d_8) - a_{13} b_{15} d_8 = 0$$

$$G_{15} : b_{10} b_{14} f_2 + a_{13} b_{15} f_2 + 2 b_7 e_1 f_2 + a_{17} b_{10} f_3 - a_{13} b_{14} f_3 = 0$$

$$G_{16} : a_{17} b_{10} d_8 - a_{13} b_{14} d_8 = 0$$

$$G_{17} : -(a_{16} b_{10} d_8^2) + a_{13} b_{13} d_8^2 = 0$$

$$G_{18} : -((a_{16} b_{10} - a_{13} b_{13}) d_8) - a_{13} b_7 f_2 = 0$$

$$G_{19} : a_{16} a_{17} b_{10} d_8 - a_{13} a_{17} b_{13} d_8 = 0$$

$$G_{20} : b_{10} b_{14} + a_{13} b_{15} + 2 b_7 e_1 - a_1 f_3 = 0$$

$$G_{21} : a_{17} b_{10} - a_{13} b_{14} + a_1 f_2 = 0$$

$$G_{22} : a_1 d_9 = 0$$

$$G_{23} : -(a_1 d_8) = 0$$

SUCESIÓN CARACTERÍSTICA (5, 1, 1, 1)

ETAPA 1A

28/1/1992

LEY DEL ÁLGEBRA

$$[x_1, x_5] = x_4$$

$$[x_1, x_6] = x_5$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_3] = a_1 x_4$$

$$[x_2, x_7] = a_{13} x_4$$

$$[x_2, x_8] = a_{16} x_4 + a_{13} x_5$$

$$[x_3, x_6] = b_7 x_4$$

$$[x_3, x_7] = b_{10} x_4 + b_7 x_5$$

$$[x_3, x_8] = b_{15} x_2 + b_{13} x_4 + b_{10} x_5 + b_7 x_6$$

$$[x_6, x_7] = e_1 x_4$$

$$[x_6, x_8] = e_4 x_4 + e_1 x_5$$

$$[x_7, x_8] = f_3 x_2 + f_1 x_4 + e_4 x_5 + e_1 x_6$$

sucesión característica (5, 1, 1, 1)

Etapas 1A -- Pagina 2

RELACIONES

$$R_1: b_7 \neq 0 \Leftrightarrow E1A$$

RELACIONES OBTENIDAS (TODAS: J, N, SC)

$$G_1: a_{13} b_{15} + 2 b_7 e_1 - a_1 f_3 = 0$$

SOLUCIÓN 1

$$a_1 \rightarrow \frac{a_{13} b_{15} + 2 b_7 e_1}{f_3}$$

SOLUCIÓN 2

$$a_{13} \rightarrow \frac{-2 b_7 e_1}{b_{15}}$$

$$f_3 \rightarrow 0$$

SOLUCIÓN 3

$$b_7 \rightarrow 0$$

$$b_{15} \rightarrow 0$$

$$f_3 \rightarrow 0$$

SOLUCIÓN 4

$$b_{15} \rightarrow 0$$

$$e_1 \rightarrow 0$$

$$f_3 \rightarrow 0$$

SUCESIÓN CARACTERÍSTICA (5, 1, 1, 1)

ETAPA 1B

29/1/1992

LEY DEL ÁLGEBRA

$$[x_1, x_5] = x_4$$

$$[x_1, x_6] = x_5$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_3] = a_1 x_4$$

$$[x_2, x_7] = a_{13} x_4$$

$$[x_2, x_8] = a_{18} x_2 + a_{17} x_3 + a_{16} x_4 + a_{13} x_5$$

$$[x_3, x_7] = b_{10} x_4$$

$$[x_3, x_8] = b_{15} x_2 + b_{14} x_3 + b_{13} x_4 + b_{10} x_5$$

$$[x_6, x_7] = e_1 x_4$$

$$[x_6, x_8] = e_4 x_4 + e_1 x_5$$

$$[x_7, x_8] = f_3 x_2 + f_2 x_3 + f_1 x_4 + e_4 x_5 + e_1 x_6$$

RELACIONES

$$R_1: b_7 = 0 \Leftarrow E1B$$

$$R_2: a_1 \neq 0 \Leftarrow E1B$$

BASE DE GROEBNER DE LAS RELACIONES (TODAS: J, N, SC)

$$G_1: a_{18} + b_{14} = 0$$

$$G_2: -b_{14}^2 - a_{17} b_{15} = 0$$

$$G_3: b_{10} b_{14} f_2 + a_{13} b_{15} f_2 + a_{17} b_{10} f_3 - a_{13} b_{14} f_3 = 0$$

$$G_4: b_{10} b_{14} + a_{13} b_{15} - a_1 f_3 = 0$$

$$G_5: a_{17} b_{10} - a_{13} b_{14} + a_1 f_2 = 0$$

SOLUCIÓN 1

$$f_3 \rightarrow \frac{b_{14} \left(b_{10} - \frac{a_{13} b_{14}}{a_{17}} \right)}{a_1}$$

$$f_2 \rightarrow \frac{-(a_{17} b_{10}) + a_{13} b_{14}}{a_1}$$

$$b_{15} \rightarrow -\frac{b_{14}^2}{a_{17}}$$

$$a_{18} \rightarrow -b_{14}$$

SOLUCIÓN 2

$$f_3 \rightarrow \frac{a_{13} b_{15}}{a_1}$$

$$f_2 \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

sucesión característica (5, 1, 1, 1)

Etapas 1B - - Pagina 3

SOLUCIÓN 3

$$f_3 \rightarrow \frac{a_{13} b_{15}}{a_1}$$

$$f_2 \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

SUCESIÓN CARACTERÍSTICA (5, 1, 1, 1)

ETAPA 1C

29/1/1992

LEY DEL ÁLGEBRA

$$[x_1, x_5] = x_4$$

$$[x_1, x_6] = x_5$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_7] = a_{13} x_4$$

$$[x_2, x_8] = a_{18} x_2 + a_{17} x_3 + a_{16} x_4 + a_{13} x_5$$

$$[x_3, x_7] = b_{10} x_4$$

$$[x_3, x_8] = b_{15} x_2 + b_{14} x_3 + b_{13} x_4 + b_{10} x_5$$

$$[x_5, x_8] = d_9 x_2 + d_8 x_3$$

$$[x_6, x_7] = -(d_9 x_2) - d_8 x_3 + e_1 x_4$$

$$[x_6, x_8] = e_4 x_4 + e_1 x_5$$

$$[x_7, x_8] = f_3 x_2 + f_2 x_3 + f_1 x_4 + e_4 x_5 + e_1 x_6$$

RELACIONES

$$R_1: b_7 = a_1 = 0 \Leftarrow E1C$$

BASE DE GROEBNER (J, N, SC1)

$$G_1: b_{15} d_8 - b_{14} d_9 = 0$$

$$G_2: a_{18} + b_{14} = 0$$

$$G_3: b_{14} d_8 + a_{17} d_9 = 0$$

$$G_4: -b_{14}^2 - a_{17} b_{15} = 0$$

$$G_5: b_{13} d_8 + a_{16} d_9 = 0$$

$$G_6: -(b_{13} b_{14} d_8) - a_{16} b_{15} d_8 = 0$$

$$G_7: -(a_{17} b_{13} d_8) + a_{16} b_{14} d_8 = 0$$

$$G_8: -(b_{10} d_8) - a_{13} d_9 = 0$$

$$G_9: b_{10} b_{14} + a_{13} b_{15} = 0$$

$$G_{10}: a_{17} b_{10} - a_{13} b_{14} = 0$$

$$G_{11}: -(a_{16} b_{10} d_8) + a_{13} b_{13} d_8 = 0$$

SOLUCIÓN 1

$$d_9 \rightarrow 0$$

$$d_8 \rightarrow 0$$

$$b_{15} \rightarrow -\frac{a_{18}^2}{a_{17}}$$

$$b_{14} \rightarrow -a_{18}$$

$$b_{10} \rightarrow -\frac{a_{13} a_{18}}{a_{17}}$$

SOLUCIÓN 2

$$d_9 \rightarrow \frac{a_{18} d_8}{a_{17}}$$

$$b_{15} \rightarrow -\frac{a_{18}^2}{a_{17}}$$

$$b_{14} \rightarrow -a_{18}$$

$$b_{13} \rightarrow -\frac{a_{16} a_{18}}{a_{17}}$$

$$b_{10} \rightarrow -\frac{a_{13} a_{18}}{a_{17}}$$

SOLUCIÓN 3

$$d_9 \rightarrow \frac{a_{18} d_8}{a_{17}}$$

$$b_{15} \rightarrow -\frac{a_{18}^2}{a_{17}}$$

$$b_{14} \rightarrow -a_{18}$$

$$b_{13} \rightarrow 0$$

$$b_{10} \rightarrow -\frac{a_{13} a_{18}}{a_{17}}$$

$$a_{16} \rightarrow 0$$

SOLUCIÓN 4

$$d_9 \rightarrow \frac{a_{18} d_8}{a_{17}}$$

$$b_{15} \rightarrow -\frac{a_{18}^2}{a_{17}}$$

$$b_{14} \rightarrow -a_{18}$$

$$b_{13} \rightarrow -\frac{a_{16} a_{18}}{a_{17}}$$

$$b_{10} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 5

$$d_9 \rightarrow \frac{a_{18} d_8}{a_{17}}$$

$$b_{15} \rightarrow -\frac{a_{18}^2}{a_{17}}$$

$$b_{14} \rightarrow -a_{18}$$

$$b_{13} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{16} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 6

$$d_9 \rightarrow 0$$

$$d_8 \rightarrow 0$$

$$b_{15} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

SOLUCIÓN 7

$$d_9 \rightarrow -\frac{b_{10} d_8}{a_{13}}$$

$$b_{15} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{13} \rightarrow \frac{a_{16} b_{10}}{a_{13}}$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

SOLUCIÓN 8

$$d_9 \rightarrow 0$$

$$d_8 \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 9

$$d_8 \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{16} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 10

$$d_9 \rightarrow 0$$

$$d_8 \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 11

$$d_8 \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{16} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 12

$$d_9 \rightarrow -\frac{b_{13} d_8}{a_{16}}$$

$$b_{15} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 13

$$d_8 \rightarrow 0$$

$$b_{15} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{16} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SOLUCIÓN 14

$$b_{15} \rightarrow 0$$

$$b_{14} \rightarrow 0$$

$$b_{13} \rightarrow 0$$

$$b_{10} \rightarrow 0$$

$$a_{18} \rightarrow 0$$

$$a_{17} \rightarrow 0$$

$$a_{16} \rightarrow 0$$

$$a_{13} \rightarrow 0$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1

9/3/1992

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_4] = X_3$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_5$$

$$[X_2, X_4] = a_4 X_2 + a_3 X_5 + a_1 X_6$$

$$[X_2, X_7] = -(a_4 X_5)$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_5 - a_4 X_6$$

$$[X_3, X_4] = b_2 X_2 + a_4 X_3 + b_1 X_5 + a_3 X_6 + a_1 X_7$$

$$[X_3, X_6] = a_4 X_5$$

$$[X_3, X_7] = b_8 X_2 + b_7 X_5$$

$$[X_3, X_8] = b_{10} X_2 + (a_{12} + b_8) X_3 + b_9 X_5 + (a_{11} + b_7) X_6 - a_4 X_7$$

$$[X_4, X_6] = c_4 X_2 + c_3 X_5 + a_4 X_6$$

$$[X_4, X_7] = c_6 X_2 + (b_8 + c_4) X_3 + c_5 X_5 + (b_7 + c_3) X_6 + a_4 X_7$$

$$[X_4, X_8] = c_8 X_2 + (b_{10} + c_6) X_3 + (a_{12} + 2b_8 + c_4) X_4 + c_7 X_5 + (b_9 + c_5) X_6 + (a_{11} + 2b_7 + c_3) X_7$$

$$[X_5, X_8] = d_6 X_2 + d_5 X_5$$

$$[X_6, X_7] = e_2 X_2 + e_1 X_5$$

$$[X_6, X_8] = e_4 X_2 + (d_6 + e_2) X_3 + e_3 X_5 + (d_5 + e_1) X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + (d_6 + e_2) X_4 + f_1 X_5 + e_3 X_6 + (d_5 + e_1) X_7$$

ADJUNTAS

$$\text{adj}(x_1) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_2) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & a_4 & 0 & 0 & 0 & a_{12} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & a_1 & a_3 & 0 & 0 & -a_4 & a_{11} \\ 0 & 0 & 0 & a_1 & 0 & 0 & 0 & -a_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_3) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & b_2 & 0 & 0 & b_8 & b_{10} \\ 0 & 0 & 0 & a_4 & 0 & 0 & 0 & a_{12} + b_8 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_1 & 0 & b_1 & 0 & a_4 & b_7 & b_9 \\ 0 & 0 & 0 & a_3 & 0 & 0 & 0 & a_{11} + b_7 \\ 0 & 0 & 0 & a_1 & 0 & 0 & 0 & -a_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_4) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_4 & -b_2 & 0 & 0 & c_4 & c_6 & c_8 \\ -1 & 0 & -a_4 & 0 & 0 & 0 & b_8 + c_4 & b_{10} + c_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & a_{12} + 2b_8 + c_4 \\ 0 & -a_3 & -b_1 & 0 & 0 & c_3 & c_5 & c_7 \\ 0 & -a_1 & -a_3 & 0 & 0 & a_4 & b_7 + c_3 & b_9 + c_5 \\ 0 & 0 & -a_1 & 0 & 0 & 0 & a_4 & a_{11} + 2b_7 + c_3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_5) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_6) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -c_4 & 0 & 0 & e_2 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 + e_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & -a_4 & -c_3 & 0 & 0 & e_1 & e_3 \\ 0 & 0 & 0 & -a_4 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_7) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -b_8 & -c_6 & 0 & -e_2 & 0 & f_2 \\ 0 & 0 & 0 & -b_8 - c_4 & 0 & 0 & 0 & e_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_6 + e_2 \\ 0 & a_4 & -b_7 & -c_5 & 0 & -e_1 & 0 & f_1 \\ -1 & 0 & 0 & -b_7 - c_3 & 0 & 0 & 0 & e_3 \\ 0 & 0 & 0 & -a_4 & 0 & 0 & 0 & d_5 + e_1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_8) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -a_{12} & -b_{10} & -c_8 & -d_6 & -e_4 & -f_2 & 0 \\ 0 & 0 & -a_{12} - b_8 & -b_{10} - c_6 & 0 & -d_6 - e_2 & -e_4 & 0 \\ 0 & 0 & 0 & -a_{12} - 2b_8 - c_4 & 0 & 0 & -d_6 - e_2 & 0 \\ 0 & -a_{11} & -b_9 & -c_7 & -d_5 & -e_3 & -f_1 & 0 \\ 0 & a_4 & -a_{11} - b_7 & -b_9 - c_5 & 0 & -d_5 - e_1 & -e_3 & 0 \\ -1 & 0 & a_4 & -a_{11} - 2b_7 - c_3 & 0 & 0 & -d_5 - e_1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1A

9/3/1992

LEY DEL ÁLGEBRA

$$\mu(X_1, X_3) = X_2$$

$$\mu(X_1, X_4) = X_3$$

$$\mu(X_1, X_6) = X_5$$

$$\mu(X_1, X_7) = X_6$$

$$\mu(X_1, X_8) = X_7$$

$$\mu(X_3, X_4) = b_2 X_2 + b_1 X_5$$

$$\mu(X_3, X_7) = b_8 X_2 + b_7 X_5$$

$$\mu(X_3, X_8) = b_{10} X_2 + b_8 X_3 + b_9 X_5 + b_7 X_6$$

$$\mu(X_4, X_6) = c_4 X_2 + c_3 X_5$$

$$\mu(X_4, X_7) = c_6 X_2 + (b_8 + c_4) X_3 + c_5 X_5 + (b_7 + c_3) X_6$$

$$\mu(X_4, X_8) = c_8 X_2 + (b_{10} + c_6) X_3 + (2b_8 + c_4) X_4 + c_7 X_5 + (b_9 + c_5) X_6 + (2b_7 + c_3) X_7$$

$$\mu(X_5, X_8) = d_6 X_2 + d_5 X_5$$

$$\mu(X_6, X_7) = e_2 X_2 + e_1 X_5$$

$$\mu(X_6, X_8) = e_4 X_2 + (d_6 + e_2) X_3 + e_3 X_5 + (d_5 + e_1) X_6$$

$$\mu(X_7, X_8) = f_2 X_2 + e_4 X_3 + (d_6 + e_2) X_4 + f_1 X_5 + e_3 X_6 + (d_5 + e_1) X_7$$

RELACIONES

$$R_1: X_2 \text{ central} \Leftarrow E1A$$

RELACIONES DE JACOBI

$$J_1 : b_7 b_8 + 2 b_8 c_3 + c_3 c_4 = 0$$

$$J_2 : 2 b_7^2 + 3 b_1 b_8 + b_1 c_4 - b_1 d_5 = 0$$

$$J_3 : 3 b_2 b_8 + 2 b_7 b_8 + b_8 c_3 + b_2 c_4 - b_7 c_4 - b_1 d_6 = 0$$

$$J_4 : 2 b_8 c_3 + c_3 c_4 - b_1 d_6 - 2 b_7 e_1 - b_1 e_2 = 0$$

$$J_5 : b_7 b_8 + b_1 d_6 + 2 b_7 e_1 + b_1 e_2 = 0$$

$$J_6 : b_8^2 + b_8 d_5 + b_2 d_6 - b_7 d_6 + b_8 e_1 + b_2 e_2 + b_7 e_2 = 0$$

$$J_7 : 2 b_8 c_4 + c_4^2 + c_4 d_5 - b_2 d_6 - c_3 d_6 + c_4 e_1 - b_2 e_2 - 2 b_7 e_2 - c_3 e_2 = 0$$

$$J_8 : b_8^2 + 2 b_8 c_4 + c_4^2 + b_8 d_5 + c_4 d_5 - b_7 d_6 - c_3 d_6 + b_8 e_1 + c_4 e_1 - b_7 e_2 - c_3 e_2 = 0$$

$$J_9 : b_7 d_6 - c_3 d_6 + d_5 e_1 + 2 e_1^2 + b_7 e_2 - c_3 e_2 = 0$$

$$J_{10} : b_8 d_6 - c_4 d_6 - d_6 e_1 + b_8 e_2 - c_4 e_2 + 2 d_5 e_2 + 2 e_1 e_2 = 0$$

$$J_{11} : - (b_8 b_9) + b_7 b_{10} - b_9 c_4 + 2 b_8 c_5 + c_4 c_5 + b_7 c_6 + b_9 e_1 + 2 c_5 e_1 - b_7 e_3 - b_1 e_4 = 0$$

$$J_{12} : - (b_{10} c_4) + 3 b_8 c_6 + c_4 c_6 + c_6 d_5 - c_5 d_6 + c_6 e_1 + b_9 e_2 + c_5 e_2 + c_4 e_3 - b_2 e_4 - b_7 e_4 - c_3 e_4 = 0$$

RELACIONES DE NILPOTENCIA

$$N_1 : 3 b_8 + c_4 + 3 d_5 + 2 e_1 = 0$$

$$N_2 : 2 b_8^2 + b_8 c_4 + 9 b_8 d_5 + 3 c_4 d_5 + 3 d_5^2 - 3 b_7 d_6 - c_3 d_6 + 6 b_8 e_1 + 2 c_4 e_1 + 4 d_5 e_1 + e_1^2 - 3 b_7 e_2 - c_3 e_2 = 0$$

$$N_3 : (\text{demasiado grande } \dots)$$

$$N_4 : (\text{demasiado grande } \dots)$$

$$N_5 : 2 b_8^2 d_5^3 + b_8 c_4 d_5^3 - 4 b_7 b_8 d_5^2 d_6 - b_8 c_3 d_5^2 d_6 - b_7 c_4 d_5^2 d_6 + 2 b_7^2 d_5 d_6^2 + b_7 c_3 d_5 d_6^2 + 4 b_8^2 d_5^2 e_1 + 2 b_8 c_4 d_5^2 e_1 - 4 b_7 b_8 d_5 d_6 e_1 - b_8 c_3 d_5 d_6 e_1 - b_7 c_4 d_5 d_6 e_1 + 2 b_8^2 d_5 e_1^2 + b_8 c_4 d_5 e_1^2 - 4 b_7 b_8 d_5^2 e_2 - b_8 c_3 d_5^2 e_2 - b_7 c_4 d_5^2 e_2 + 4 b_7^2 d_5 d_6 e_2 + 2 b_7 c_3 d_5 d_6 e_2 - 4 b_7 b_8 d_5 e_1 e_2 - b_8 c_3 d_5 e_1 e_2 - b_7 c_4 d_5 e_1 e_2 + 2 b_7^2 d_5 e_2^2 + b_7 c_3 d_5 e_2^2 = 0$$

RELACIONES DE LA SUC. CARACT. (1)

$$S_1 : -2 b_8^2 d_6 - b_8 c_4 d_6 - 2 b_8 d_5 d_6 - c_4 d_5 d_6 - d_5^2 d_6 - b_7 d_6^2 - d_5 d_6 e_1 - 2 b_8 d_5 e_2 - c_4 d_5 e_2 - d_5^2 e_2 - b_7 d_6 e_2 - d_5 e_1 e_2 = 0$$

$$S_2 : (\text{demasiado grande } \dots)$$

$$S_3 : (\text{demasiado grande } \dots)$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1B

9/3/1992

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_4] = X_3$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_5$$

$$[X_2, X_4] = a_4 X_2 + a_3 X_5 + a_1 X_6$$

$$[X_2, X_7] = -(a_4 X_5)$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_5 - a_4 X_6$$

$$[X_3, X_4] = b_2 X_2 + a_4 X_3 + b_1 X_5 + a_3 X_6 + a_1 X_7$$

$$[X_3, X_6] = a_4 X_5$$

$$[X_3, X_7] = b_8 X_2 + b_7 X_5$$

$$[X_3, X_8] = b_{10} X_2 + (a_{12} + b_8) X_3 + b_9 X_5 + (a_{11} + b_7) X_6 - a_4 X_7$$

$$[X_4, X_6] = c_4 X_2 + c_3 X_5 + a_4 X_6$$

$$[X_4, X_7] = c_6 X_2 + (b_8 + c_4) X_3 + c_5 X_5 + (b_7 + c_3) X_6 + a_4 X_7$$

$$[X_4, X_8] = c_8 X_2 + (b_{10} + c_6) X_3 + (a_{12} + 2b_8 + c_4) X_4 + c_7 X_5 + (b_9 + c_5) X_6 + (a_{11} + 2b_7 + c_3) X_7$$

$$[X_6, X_7] = e_2 X_2 + e_1 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_2 X_3 + e_3 X_5 + e_1 X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + e_2 X_4 + f_1 X_5 + e_3 X_6 + e_1 X_7$$

RELACIONES

$$R_1: X_5 \text{ central} \Leftrightarrow E1B$$

RELACIONES DE JACOBI

$$J_1: a_1 b_8 = 0$$

$$J_2: 2 a_4^2 + 2 a_1 a_{12} + a_1 b_8 = 0$$

$$J_3: a_1 b_8 + a_1 c_4 - a_1 e_1 = 0$$

$$J_4: 2 a_4^2 + 2 a_1 a_{12} + 2 a_1 b_8 + a_1 c_4 - a_1 e_1 = 0$$

$$J_5: 2 a_4^2 + 2 a_1 a_{12} + 3 a_1 b_8 + a_1 c_4 - a_1 e_1 = 0$$

$$J_6: -(a_1 c_4) + a_1 e_1 = 0$$

$$J_7: a_4 b_2 + a_4 b_7 + a_3 b_8 + a_4 c_3 - a_1 c_6 - a_3 e_1 = 0$$

$$J_8: -(a_1 e_2) = 0$$

$$J_9: a_1 e_2 = 0$$

$$J_{10}: -3 a_4 e_2 = 0$$

$$J_{11}: -2 a_4 e_2 = 0$$

$$J_{12}: -(a_4 e_2) = 0$$

$$J_{13}: a_4 e_2 = 0$$

$$J_{14}: a_4 b_8 - a_3 e_2 = 0$$

$$J_{15}: a_4 b_8 + 2 a_4 c_4 - 2 a_4 e_1 - a_3 e_2 = 0$$

$$J_{16}: a_4 b_8 + a_3 e_2 = 0$$

$$J_{17}: b_8^2 + b_8 e_1 + a_{11} e_2 + b_2 e_2 + b_7 e_2 = 0$$

$$J_{18}: -(a_{12} e_2) + b_8 e_2 - c_4 e_2 + 2 e_1 e_2 = 0$$

$$J_{19}: -2 a_4 a_{11} + 2 a_3 a_{12} - 2 a_4 b_7 + 2 a_3 b_8 + a_1 b_{10} + a_3 c_4 + a_1 c_6 - a_1 e_3 = 0$$

$$J_{20}: -2 a_4 a_{11} + 2 a_3 a_{12} + a_4 b_2 - a_4 b_7 + 3 a_3 b_8 + a_1 b_{10} + a_4 c_3 + a_3 c_4 - a_3 e_1 - a_1 e_3 = 0$$

$$J_{21}: a_4 a_{12} + 2 a_4 b_8 + 2 a_4 c_4 - a_1 e_4 = 0$$

$$J_{22}: a_4 a_{12} + 3 a_4 b_8 + 2 a_4 c_4 - a_1 e_4 = 0$$

$$J_{23}: a_4 a_{12} + a_4 b_8 + 2 a_4 e_1 - a_1 e_4 = 0$$

$$J_{24}: a_4 a_{12} + 2 a_4 b_8 + 2 a_4 c_4 - a_3 e_2 - a_1 e_4 = 0$$

$$J_{25}: a_4 a_{12} + 3 a_4 b_8 + 2 a_4 c_4 - a_3 e_2 - a_1 e_4 = 0$$

$$J_{26}: -(a_4 a_{12}) - 2 a_4 e_1 + a_3 e_2 + a_1 e_4 = 0$$

$$J_{27}: a_4 b_{10} + a_{12} c_3 + 2 b_8 c_3 - a_{11} c_4 + c_3 c_4 + a_4 c_6 - a_{11} e_1 - 2 b_7 e_1 - b_1 e_2 - a_4 e_3 - a_3 e_4 = 0$$

$$J_{28}: 2 b_8 c_4 + c_4^2 + c_4 e_1 - a_{11} e_2 - b_2 e_2 - 2 b_7 e_2 - c_3 e_2 - 2 a_4 e_4 = 0$$

$$J_{29}: b_8^2 + 2 b_8 c_4 + c_4^2 + b_8 e_1 + c_4 e_1 - b_7 e_2 - c_3 e_2 - 2 a_4 e_4 = 0$$

$$J_{30}: 2 e_1^2 - a_{11} e_2 + b_7 e_2 - c_3 e_2 - 2 a_4 e_4 = 0$$

$$J_{31} : 2 a_{12} b_1 - a_{11} b_2 + a_{11} b_7 + 2 b_7^2 + 3 b_1 b_8 + a_3 b_{10} - a_{11} c_3 + b_1 c_4 + 2 a_4 c_5 - a_1 c_8 - a_3 e_3 - a_1 f_1 = 0$$

$$J_{32} : a_{12} b_7 - a_{11} b_8 + b_7 b_8 - a_4 b_{10} + a_{11} e_1 + 2 b_7 e_1 + b_1 e_2 + a_4 e_3 - a_1 f_2 = 0$$

$$J_{33} : a_{12} b_2 + a_{11} b_8 + 3 b_2 b_8 + 2 b_7 b_8 + b_8 c_3 - a_{11} c_4 + b_2 c_4 - b_7 c_4 + a_4 c_6 - a_3 e_4 - a_1 f_2 = 0$$

$$J_{34} : a_{12} b_7 - a_{11} b_8 + b_7 b_8 + a_{12} c_3 + 2 b_8 c_3 - a_{11} c_4 + c_3 c_4 + a_4 c_6 - a_3 e_4 - a_1 f_2 = 0$$

$$J_{35} : -(b_8 b_9) + b_7 b_{10} - b_9 c_4 + a_{12} c_5 + 2 b_8 c_5 + c_4 c_5 - a_{11} c_6 + b_7 c_6 - a_4 c_8 + b_9 e_1 + 2 c_5 e_1 - b_7 e_3 - b_1 e_4 - a_4 f_1 - a_3 f_2 = 0$$

$$J_{36} : -(b_{10} c_4) + 3 b_8 c_6 + c_4 c_6 + c_6 e_1 + b_9 e_2 + c_5 e_2 + c_4 e_3 - b_2 e_4 - b_7 e_4 - c_3 e_4 - 2 a_4 f_2 = 0$$

RELACIONES DE NILPOTENCIA

$$N_1 : -2 a_4^2 + a_1 b_8 + 2 a_1 c_4 = 0$$

$$N_2 : a_4^4 - a_1 a_4^2 b_8 - 2 a_1 a_4^2 c_4 + a_1^2 b_8 c_4 + a_1^2 c_4^2 = 0$$

$$N_3 : 3 a_{12} + 3 b_8 + c_4 + 2 e_1 = 0$$

$$N_4 : 3 a_{12}^2 + 6 a_{12} b_8 + 2 b_8^2 + 2 a_{12} c_4 + b_8 c_4 + 6 a_{12} e_1 + 6 b_8 e_1 + 2 c_4 e_1 + e_1^2 - 2 a_{11} e_2 - 3 b_7 e_2 - c_3 e_2 + 2 a_4 e_4 = 0$$

$$N_5 : (\text{demasiado grande } \dots)$$

$$N_6 : (\text{demasiado grande } \dots)$$

$$N_7 : (\text{demasiado grande } \dots)$$

RELACIONES DE LA SUC. CARACT. (1)

$$S_1 : a_4 e_2 = 0$$

$$S_2 : -a_{12}^3 - 3 a_{12}^2 b_8 - 2 a_{12} b_8^2 - a_{12}^2 c_4 - a_{12} b_8 c_4 - 2 a_{11} a_{12} e_2 - a_{12} b_7 e_2 - 2 a_{11} b_8 e_2 - 2 a_4 b_{10} e_2 - a_{11} c_4 e_2 - a_4 c_6 e_2 - a_{11} e_1 e_2 - a_4 e_2 e_3 + a_4 a_{12} e_4 + 2 a_4 b_8 e_4 + a_4 c_4 e_4 = 0$$

$$S_3 : (\text{demasiado grande } \dots)$$

$$S_4 : (\text{demasiado grande } \dots)$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1BA

9/3/1992

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_4] = X_3$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_3] = a_1 X_5$$

$$[X_2, X_4] = a_3 X_5 + a_1 X_6$$

$$[X_2, X_8] = a_{11} X_5$$

$$[X_3, X_4] = b_2 X_2 + b_1 X_5 + a_3 X_6 + a_1 X_7$$

$$[X_3, X_7] = b_7 X_5$$

$$[X_3, X_8] = e_3 X_2 + b_9 X_5 + (a_{11} + b_7) X_6$$

$$[X_4, X_6] = c_3 X_5$$

$$[X_4, X_7] = c_5 X_5 + (b_7 + c_3) X_6$$

$$[X_4, X_8] = c_8 X_2 + e_3 X_3 + c_7 X_5 + (b_9 + c_5) X_6 + (a_{11} + 2b_7 + c_3) X_7$$

$$[X_6, X_8] = e_3 X_5$$

$$[X_7, X_8] = f_1 X_5 + e_3 X_6$$

RELACIONES

$$R_1: a_1 \neq 0 \Leftrightarrow E1BA$$

$$R_2: a_{12}^2 - > e_4 a_4 \Leftrightarrow J, N$$

$$R_3: a_4^2 - > a_1 a_{12} \Leftrightarrow J, N$$

$$R_4: X_5 \text{ central} \Leftrightarrow E1B$$

JACOBI, NILPOTENCIA Y SC

$$G_1 : -(a_{11} b_2) + a_{11} b_7 + 2 b_7^2 - a_{11} c_3 - a_1 c_8 - a_1 f_1 = 0$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1BB

9/3/1992

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_4] = X_3$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_4] = a_3 X_5$$

$$[X_2, X_8] = a_{11} X_5$$

$$[X_3, X_4] = b_2 X_2 + b_1 X_5 + a_3 X_6$$

$$[X_3, X_7] = b_7 X_5$$

$$[X_3, X_8] = b_{10} X_2 + b_9 X_5 + (a_{11} + b_7) X_6$$

$$[X_4, X_6] = c_3 X_5$$

$$[X_4, X_7] = c_6 X_2 + c_5 X_5 + (b_7 + c_3) X_6$$

$$[X_4, X_8] = c_8 X_2 + (b_{10} + c_6) X_3 + c_7 X_5 + (b_9 + c_5) X_6 + (a_{11} + 2b_7 + c_3) X_7$$

$$[X_6, X_8] = e_3 X_5$$

$$[X_7, X_8] = f_2 X_2 + f_1 X_5 + e_3 X_6$$

RELACIONES

$$R_1: a_1 = 0, a_3 \neq 0 \Leftrightarrow E1BB$$

$$R_2: a_1 = 0 \Leftrightarrow E1BB$$

$$R_3: X_5 \text{ central} \Leftrightarrow E1B$$

JACOBI, NILPOTENCIA Y SC

$$G_1 : b_7 b_{10}^2 - a_{11} b_{10} c_6 + b_7 b_{10} c_6 - 2 b_7 b_{10} e_3 + a_{11} c_6 e_3 - b_7 c_6 e_3 + b_7 e_3^2 - a_{11} b_2 f_2 + a_{11} b_7 f_2 + 2 b_7^2 f_2 - a_{11} c_3 f_2 = 0$$

$$G_2 : b_7 b_{10} - a_{11} c_6 + b_7 c_6 - b_7 e_3 - a_3 f_2 = 0$$

$$G_3 : -(a_{11} b_2) + a_{11} b_7 + 2 b_7^2 + a_3 b_{10} - a_{11} c_3 - a_3 e_3 = 0$$

SUCESIÓN CARACTERÍSTICA (4, 3, 1)

ETAPA 1BC

9/3/1992

LEY DEL ÁLGEBRA

$$[X_1, X_3] = X_2$$

$$[X_1, X_4] = X_3$$

$$[X_1, X_6] = X_5$$

$$[X_1, X_7] = X_6$$

$$[X_1, X_8] = X_7$$

$$[X_2, X_8] = a_{12} X_2 + a_{11} X_5$$

$$[X_3, X_4] = b_2 X_2 + b_1 X_5$$

$$[X_3, X_7] = b_8 X_2 + b_7 X_5$$

$$[X_3, X_8] = b_{10} X_2 + (a_{12} + b_8) X_3 + b_9 X_5 + (a_{11} + b_7) X_6$$

$$[X_4, X_6] = c_4 X_2 + c_3 X_5$$

$$[X_4, X_7] = c_6 X_2 + (b_8 + c_4) X_3 + c_5 X_5 + (b_7 + c_3) X_6$$

$$[X_4, X_8] = c_8 X_2 + (b_{10} + c_6) X_3 + (a_{12} + 2b_8 + c_4) X_4 + c_7 X_5 + (b_9 + c_5) X_6 + (a_{11} + 2b_7 + c_3) X_7$$

$$[X_6, X_7] = e_2 X_2 + e_1 X_5$$

$$[X_6, X_8] = e_4 X_2 + e_2 X_3 + e_3 X_5 + e_1 X_6$$

$$[X_7, X_8] = f_2 X_2 + e_4 X_3 + e_2 X_4 + f_1 X_5 + e_3 X_6 + e_1 X_7$$

RELACIONES

$$R_1: a_1 = a_3 = 0 \Leftrightarrow E1BC$$

$$R_2: X_5 \text{ central} \Leftrightarrow E1B$$

RELACIONES DE JACOBI

$$J_1 : 0 = 0$$

$$J_2 : 0 = 0$$

$$J_3 : 0 = 0$$

$$J_4 : 0 = 0$$

$$J_5 : 0 = 0$$

$$J_6 : 0 = 0$$

$$J_7 : 0 = 0$$

$$J_8 : 2 a_{12} b_1 - a_{11} b_2 + a_{11} b_7 + 2 b_7^2 + 3 b_1 b_8 - a_{11} c_3 + b_1 c_4 = 0$$

$$J_9 : a_{12} b_2 + a_{11} b_8 + 3 b_2 b_8 + 2 b_7 b_8 + b_8 c_3 - a_{11} c_4 + b_2 c_4 - b_7 c_4 = 0$$

$$J_{10} : a_{12} b_7 - a_{11} b_8 + b_7 b_8 + a_{12} c_3 + 2 b_8 c_3 - a_{11} c_4 + c_3 c_4 = 0$$

$$J_{11} : 0 = 0$$

$$J_{12} : 0 = 0$$

$$J_{13} : 0 = 0$$

$$J_{14} : 0 = 0$$

$$J_{15} : 0 = 0$$

$$J_{16} : 0 = 0$$

$$J_{17} : 0 = 0$$

$$J_{18} : b_8^2 + b_8 e_1 + a_{11} e_2 + b_2 e_2 + b_7 e_2 = 0$$

$$J_{19} : -(a_{12} e_2) + b_8 e_2 - c_4 e_2 + 2 e_1 e_2 = 0$$

$$J_{20} : a_{12} c_3 + 2 b_8 c_3 - a_{11} c_4 + c_3 c_4 - a_{11} e_1 - 2 b_7 e_1 - b_1 e_2 = 0$$

$$J_{21} : a_{12} b_7 - a_{11} b_8 + b_7 b_8 + a_{11} e_1 + 2 b_7 e_1 + b_1 e_2 = 0$$

$$J_{22} : 2 b_8 c_4 + c_4^2 + c_4 e_1 - a_{11} e_2 - b_2 e_2 - 2 b_7 e_2 - c_3 e_2 = 0$$

$$J_{23} : b_8^2 + 2 b_8 c_4 + c_4^2 + b_8 e_1 + c_4 e_1 - b_7 e_2 - c_3 e_2 = 0$$

$$J_{24} : 2 e_1^2 - a_{11} e_2 + b_7 e_2 - c_3 e_2 = 0$$

$$J_{25} : -(b_8 b_9) + b_7 b_{10} - b_9 c_4 + a_{12} c_5 + 2 b_8 c_5 + c_4 c_5 - a_{11} c_6 + b_7 c_6 + b_9 e_1 + 2 c_5 e_1 - b_7 e_3 - b_1 e_4 = 0$$

$$J_{26} : -(b_{10} c_4) + 3 b_8 c_6 + c_4 c_6 + c_6 e_1 + b_9 e_2 + c_5 e_2 + c_4 e_3 - b_2 e_4 - b_7 e_4 - c_3 e_4 = 0$$

RELACIONES DE NILPOTENCIA

$$N_1 : 3 a_{12} + 3 b_8 + c_4 + 2 e_1 = 0$$

$$N_2 : 3 a_{12}^2 + 6 a_{12} b_8 + 2 b_8^2 + 2 a_{12} c_4 + b_8 c_4 + 6 a_{12} e_1 + 6 b_8 e_1 + 2 c_4 e_1 + e_1^2 - 2 a_{11} e_2 - 3 b_7 e_2 - c_3 e_2 = 0$$

$$N_3 : a_{12}^3 + 3 a_{12}^2 b_8 + 2 a_{12} b_8^2 + a_{12}^2 c_4 + a_{12} b_8 c_4 + 6 a_{12}^2 e_1 + 12 a_{12} b_8 e_1 + 4 b_8^2 e_1 + 4 a_{12} c_4 e_1 + 2 b_8 c_4 e_1 + 3 a_{12} e_1^2 + 3 b_8 e_1^2 + c_4 e_1^2 - 4 a_{11} a_{12} e_2 - 6 a_{12} b_7 e_2 - 3 a_{11} b_8 e_2 - 4 b_7 b_8 e_2 - 2 a_{12} c_3 e_2 - b_8 c_3 e_2 - a_{11} c_4 e_2 - b_7 c_4 e_2 - 2 a_{11} e_1 e_2 - 3 b_7 e_1 e_2 - c_3 e_1 e_2 = 0$$

N_4 : (demasiado grande ...)

$$N_5 : a_{12}^3 e_1^2 + 3 a_{12}^2 b_8 e_1^2 + 2 a_{12} b_8^2 e_1^2 + a_{12}^2 c_4 e_1^2 + a_{12} b_8 c_4 e_1^2 - 2 a_{11} a_{12}^2 e_1 e_2 - 3 a_{12}^2 b_7 e_1 e_2 - 3 a_{11} a_{12} b_8 e_1 e_2 - 4 a_{12} b_7 b_8 e_1 e_2 - a_{12}^2 c_3 e_1 e_2 - a_{12} b_8 c_3 e_1 e_2 - a_{11} a_{12} c_4 e_1 e_2 - a_{12} b_7 c_4 e_1 e_2 + a_{11}^2 a_{12} e_2^2 + 3 a_{11} a_{12} b_7 e_2^2 + 2 a_{12} b_7^2 e_2^2 + a_{11} a_{12} c_3 e_2^2 + a_{12} b_7 c_3 e_2^2 = 0$$

RELACIONES DE LA SUC. CARACT. (1)

$$S_1 : -a_{12}^3 - 3 a_{12}^2 b_8 - 2 a_{12} b_8^2 - a_{12}^2 c_4 - a_{12} b_8 c_4 - 2 a_{11} a_{12} e_2 - a_{12} b_7 e_2 - 2 a_{11} b_8 e_2 - a_{11} c_4 e_2 - a_{11} e_1 e_2 = 0$$

S_2 : (demasiado grande ...)

S_3 : (demasiado grande ...)

SUCESIÓN CARACTERÍSTICA (3, 3, 1, 1)

ETAPA 1

27/2/1992

LEY DEL ÁLGEBRA

$$[x_1, x_4] = x_3$$

$$[x_1, x_5] = x_4$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_4] = c_5 x_3 + c_4 x_6$$

$$[x_2, x_5] = c_9 x_2 + c_8 x_3 + c_5 x_4 + c_7 x_6 + c_4 x_7$$

$$[x_2, x_6] = c_{11} x_3$$

$$[x_2, x_7] = c_{14} x_3 + c_{11} x_4 + c_{13} x_6$$

$$[x_2, x_8] = c_{18} x_2 + c_{17} x_3 + c_{14} x_4 + c_{11} x_5 + c_{16} x_6 + c_{13} x_7$$

$$[x_3, x_5] = d_5 x_3 + d_4 x_6$$

$$[x_3, x_7] = d_{10} x_6$$

$$[x_3, x_8] = d_{15} x_2 + d_{14} x_3 + d_{13} x_6 + d_{10} x_7$$

$$[x_4, x_5] = e_3 x_2 + e_2 x_3 + d_5 x_4 + e_1 x_6 + d_4 x_7$$

$$[x_4, x_7] = -(d_{15} x_2) + e_8 x_3 + e_7 x_6$$

$$[x_4, x_8] = e_{12} x_2 + e_{11} x_3 + (d_{14} + e_8) x_4 + e_{10} x_6 + (d_{13} + e_7) x_7$$

$$[x_5, x_6] = d_{15} x_2 + f_2 x_3 + e_5 x_4 + (-d_{13} - 2 e_7) x_6$$

$$[x_5, x_7] = -(e_{12} x_2) + f_5 x_3 + (e_8 + f_2) x_4 + f_4 x_6 + (-d_{13} - e_7) x_7$$

$$[x_5, x_8] = f_9 x_2 + f_8 x_3 + (e_{11} + f_5) x_4 + (d_{14} + 2 e_8 + f_2) x_5 + f_7 x_6 + (e_{10} + f_4) x_7$$

$$[x_6, x_7] = g_2 x_3$$

$$[x_6, x_8] = g_5 x_3 + g_2 x_4 + g_4 x_6$$

$$[x_7, x_8] = h_3 x_2 + h_2 x_3 + g_5 x_4 + g_2 x_5 + h_1 x_6 + g_4 x_7$$

ADJUNTAS

$$\text{adj}(x_1) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_2) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & c_9 & 0 & 0 & c_{18} \\ 0 & 0 & 0 & c_5 & c_8 & c_{11} & c_{14} & c_{17} \\ 0 & 0 & 0 & 0 & c_5 & 0 & c_{11} & c_{14} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & c_{11} \\ 0 & 0 & 0 & c_4 & c_7 & 0 & c_{13} & c_{16} \\ 0 & 0 & 0 & 0 & c_4 & 0 & 0 & c_{13} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_3) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_{15} \\ 0 & 0 & 0 & 0 & d_5 & 0 & 0 & d_{14} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & d_4 & 0 & d_{10} & d_{13} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_{10} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_4) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & e_3 & 0 & -d_{15} & e_{12} \\ -1 & -c_5 & 0 & 0 & e_2 & 0 & e_8 & e_{11} \\ 0 & 0 & 0 & 0 & d_5 & 0 & 0 & d_{14} + e_8 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -c_4 & 0 & 0 & e_1 & 0 & e_7 & e_{10} \\ 0 & 0 & 0 & 0 & d_4 & 0 & 0 & d_{13} + e_7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_5) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -c_9 & 0 & -e_3 & 0 & d_{15} & -e_{12} & f_9 \\ 0 & -c_8 & -d_5 & -e_2 & 0 & f_2 & f_5 & f_8 \\ -1 & -c_5 & 0 & -d_5 & 0 & e_5 & e_8 + f_2 & e_{11} + f_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & d_{14} + 2e_8 + f_2 \\ 0 & -c_7 & -d_4 & -e_1 & 0 & -d_{13} - 2e_7 & f_4 & f_7 \\ 0 & -c_4 & 0 & -d_4 & 0 & 0 & -d_{13} - e_7 & e_{10} + f_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_6) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & -d_{15} & 0 & 0 & 0 \\ 0 & -c_{11} & 0 & 0 & -f_2 & 0 & g_2 & g_5 \\ 0 & 0 & 0 & 0 & -e_5 & 0 & 0 & g_2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{13} + 2e_7 & 0 & 0 & g_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_7) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & d_{15} & e_{12} & 0 & 0 & h_3 \\ 0 & -c_{14} & 0 & -e_8 & -f_5 & -g_2 & 0 & h_2 \\ 0 & -c_{11} & 0 & 0 & -e_8 - f_2 & 0 & 0 & g_5 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & g_2 \\ -1 & -c_{13} & -d_{10} & -e_7 & -f_4 & 0 & 0 & h_1 \\ 0 & 0 & 0 & 0 & d_{13} + e_7 & 0 & 0 & g_4 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\text{adj}(x_8) = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -c_{18} & -d_{15} & -e_{12} & -f_9 & 0 & -h_3 & 0 & 0 \\ 0 & -c_{17} & -d_{14} & -e_{11} & -f_8 & -g_5 & -h_2 & 0 & 0 \\ 0 & -c_{14} & 0 & -d_{14} - e_8 & -e_{11} - f_5 & -g_2 & -g_5 & 0 & 0 \\ 0 & -c_{11} & 0 & 0 & -d_{14} - 2e_8 - f_2 & 0 & -g_2 & 0 & 0 \\ 0 & -c_{16} & -d_{13} & -e_{10} & -f_7 & -g_4 & -h_1 & 0 & 0 \\ -1 & -c_{13} & -d_{10} & -d_{13} - e_7 & -e_{10} - f_4 & 0 & -g_4 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

SUCESIÓN CARACTERÍSTICA (3, 3, 1, 1)

ETAPA 2

27/2/1992

LEY DEL ÁLGEBRA

$$[x_1, x_4] = x_3$$

$$[x_1, x_5] = x_4$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_4] = c_5 x_3 + c_4 x_6$$

$$[x_2, x_5] = c_9 x_2 + c_8 x_3 + c_5 x_4 + c_7 x_6 + c_4 x_7$$

$$[x_2, x_6] = c_{11} x_3$$

$$[x_2, x_7] = c_{14} x_3 + c_{11} x_4 + c_{13} x_6$$

$$[x_2, x_8] = c_{18} x_2 + c_{17} x_3 + c_{14} x_4 + c_{11} x_5 + c_{16} x_6 + c_{13} x_7$$

$$[x_3, x_5] = d_5 x_3 + d_4 x_6$$

$$[x_3, x_8] = d_{15} x_2 + d_{14} x_3 + d_{13} x_6$$

$$[x_4, x_5] = e_3 x_2 + e_2 x_3 + d_5 x_4 + e_1 x_6 + d_4 x_7$$

$$[x_4, x_7] = -(d_{15} x_2) + e_8 x_3 + e_7 x_6$$

$$[x_4, x_8] = e_{12} x_2 + e_{11} x_3 + (d_{14} + e_8) x_4 + e_{10} x_6 + (d_{13} + e_7) x_7$$

$$[x_5, x_6] = d_{15} x_2 + f_2 x_3 + (-d_{13} - 2e_7) x_6$$

$$[x_5, x_7] = -(e_{12} x_2) + f_5 x_3 + (e_8 + f_2) x_4 + f_4 x_6 + (-d_{13} - e_7) x_7$$

$$[x_5, x_8] = f_9 x_2 + f_8 x_3 + (e_{11} + f_5) x_4 + (d_{14} + 2 e_8 + f_2) x_5 + f_7 x_6 + (e_{10} + f_4) x_7$$

$$[x_6, x_7] = g_2 x_3$$

$$[x_6, x_8] = g_5 x_3 + g_2 x_4 + g_4 x_6$$

$$[x_7, x_8] = h_3 x_2 + h_2 x_3 + g_5 x_4 + g_2 x_5 + h_1 x_6 + g_4 x_7$$

CONDICIONES DE JACOBI

$$J_1 : -(c_{11} d_4) = 0$$

$$J_2 : c_{11} d_4 = 0$$

$$J_3 : 0 = 0$$

$$J_4 : 0 = 0$$

$$J_5 : 0 = 0$$

$$J_6 : 0 = 0$$

$$J_7 : 0 = 0$$

$$J_8 : 0 = 0$$

$$J_9 : -(c_{11} d_4) = 0$$

$$J_{10} : -(c_{11} d_5) + c_{11} d_{13} = 0$$

$$J_{11} : -(c_4 d_{15}) = 0$$

$$J_{12} : 2 c_4 d_{15} = 0$$

$$J_{13} : -(c_{11} d_{15}) = 0$$

$$J_{14} : c_{11} d_{15} = 0$$

$$J_{15} : 0 = 0$$

$$J_{16} : 0 = 0$$

$$J_{17} : c_4 d_{15} = 0$$

$$J_{18} : -(c_9 d_{15}) + d_5 d_{15} + d_{13} d_{15} = 0$$

$$J_{19} : -(c_5 d_{15}) + c_{13} d_{15} - c_{11} e_3 = 0$$

$$J_{20} : c_5 d_{15} - c_{13} d_{15} + c_{11} e_3 = 0$$

$$J_{21} : 0 = 0$$

$$J_{22} : 0 = 0$$

$$J_{23} : 0 = 0$$

$$J_{24} : 0 = 0$$

$$J_{25} : 0 = 0$$

$$J_{26} : c_{11} d_4 = 0$$

$$J_{27} : c_4 c_9 - c_5 d_4 + c_{13} d_4 + c_4 d_5 - c_4 d_{13} - 3 c_4 e_7 = 0$$

$$J_{28} : -(c_9 c_{11}) + c_{11} d_5 - c_{11} d_{13} - c_{11} e_7 = 0$$

$$J_{29} : 0 = 0$$

$$J_{30} : c_4 d_{15} = 0$$

$$J_{31} : -(c_5 d_{15}) - c_{11} e_3 = 0$$

$$J_{32} : c_5 d_{15} = 0$$

$$J_{33} : -(c_7 d_{15}) - c_{13} e_3 - d_5 e_7 + e_7^2 + d_4 e_8 + c_4 e_{12} = 0$$

$$J_{34} : c_9 d_{15} - d_5 d_{15} - d_{13} d_{15} = 0$$

$$J_{35} : c_5 c_9 + c_{14} d_4 + c_{11} e_1 - c_4 e_8 + c_4 f_2 = 0$$

$$J_{36} : -(c_9 c_{13}) + c_{14} d_4 + c_{11} e_1 - c_5 e_7 + c_{13} e_7 + c_4 e_8 + c_4 f_2 = 0$$

$$J_{37} : 0 = 0$$

$$J_{38} : -3 d_{15} g_2 = 0$$

$$J_{39} : 0 = 0$$

$$J_{40} : -(c_9 c_{11}) - c_4 g_2 = 0$$

$$J_{41} : c_{11} e_7 - c_4 g_2 = 0$$

$$J_{42} : -(c_{11} d_5) + c_{11} d_{13} + c_{11} e_7 - c_4 g_2 = 0$$

$$J_{43} : -2 c_{11} d_{13} - 2 c_{11} e_7 + c_4 g_2 = 0$$

$$J_{44} : -2 c_{11} d_{13} - 2 c_{11} e_7 + c_4 g_2 = 0$$

$$J_{45} : -(c_9 c_{11}) + c_{11} d_5 - c_{11} d_{13} - 2 c_{11} e_7 + c_4 g_2 = 0$$

$$J_{46} : -(c_9 c_{14}) + c_{14} d_5 - c_{14} d_{13} + c_{11} e_2 - c_{14} e_7 + c_5 f_2 - c_{13} f_2 + c_{11} f_4 - c_7 g_2 = 0$$

$$J_{47} : -2 c_{14} d_{15} - 2 c_{11} e_{12} + c_9 g_2 = 0$$

$$J_{48} : -(c_{11} e_3) - d_4 g_2 = 0$$

$$J_{49} : -(d_4 g_2) = 0$$

$$J_{50} : -(c_{13} d_{15}) - d_4 g_2 = 0$$

$$J_{51} : -(c_{13} d_{15}) - d_4 g_2 = 0$$

$$J_{52} : c_5 d_{15} - d_4 g_2 = 0$$

$$J_{53} : c_{13} d_{15} + d_4 g_2 = 0$$

$$J_{54} : -(c_5 d_{15}) - c_{11} e_3 + d_4 g_2 = 0$$

$$J_{55} : c_{13} d_{15} + d_4 g_2 = 0$$

$$J_{56} : c_{11} d_{15} = 0$$

$$J_{57} : -(c_8 d_{15}) - c_{14} e_3 - d_{13} e_8 - e_7 e_8 + c_5 e_{12} - e_7 f_2 - e_1 g_2 = 0$$

$$J_{58} : c_{14} d_{15} + c_{11} e_{12} + d_5 g_2 - e_7 g_2 = 0$$

$$J_{59} : c_{11} e_{12} - d_{13} g_2 - e_7 g_2 = 0$$

$$J_{60} : c_{11} e_{12} + d_{13} g_2 + e_7 g_2 = 0$$

$$J_{61} : -(c_{14} d_{15}) - c_{11} e_{12} - d_5 g_2 + 2 d_{13} g_2 + 3 e_7 g_2 = 0$$

$$J_{62} : c_4 c_{18} - c_5 d_{13} + c_{13} d_{13} + c_4 d_{14} - c_{11} e_1 + c_4 e_8 - c_4 g_4 = 0$$

$$J_{63} : -(c_9 c_{13}) + c_4 c_{18} + c_{14} d_4 - c_5 d_{13} + c_{13} d_{13} + c_4 d_{14} - c_5 e_7 + c_{13} e_7 + 2 c_4 e_8 + c_4 f_2 - c_4 g_4 = 0$$

$$J_{64} : c_{11} c_{18} - c_{11} d_{14} + c_{11} f_2 + c_5 g_2 - c_{13} g_2 + c_{11} g_4 = 0$$

$$J_{65} : -(d_5 d_{13}) + d_{13}^2 + 2 d_4 d_{14} + c_7 d_{15} + 2 d_{13} e_7 + 2 d_4 e_8 + d_4 f_2 - d_4 g_4 = 0$$

$$J_{66} : -(d_5 d_{13}) + d_{13}^2 + 2 d_4 d_{14} - c_{13} e_3 - d_5 e_7 + 2 d_{13} e_7 + e_7^2 + 3 d_4 e_8 + c_4 e_{12} + d_4 f_2 - d_4 g_4 = 0$$

$$J_{67} : c_{18} d_{15} - d_{14} d_{15} - 2 d_{15} e_8 + e_3 g_2 - d_{15} g_4 = 0$$

$$J_{68} : -(c_{18} d_{15}) + d_{14} d_{15} + 2 d_{15} e_8 - e_3 g_2 + d_{15} g_4 = 0$$

$$J_{69} : -(c_{14} d_{15}) - d_5 g_2 + d_{13} g_2 + 2 e_7 g_2 = 0$$

$$J_{70} : c_5 c_{18} + c_{14} d_{13} - c_{11} e_2 + c_{14} e_7 + c_5 e_8 - c_{13} e_8 + c_{11} e_{10} - c_4 g_5 = 0$$

$$J_{71} : -(c_9 c_{14}) + c_5 c_{18} + c_{14} d_5 + c_5 e_8 - c_{13} e_8 + c_{11} e_{10} + c_5 f_2 - c_{13} f_2 + c_{11} f_4 - c_7 g_2 - c_4 g_5 = 0$$

$$J_{72} : c_{13} c_{18} - c_{14} d_{13} + c_{14} e_7 - c_{11} e_{10} + c_{11} f_4 + c_7 g_2 + c_4 g_5 = 0$$

$$J_{73} : d_5 d_{14} + c_8 d_{15} + 2 d_5 e_8 + d_5 f_2 - d_{13} f_2 - d_4 g_5 = 0$$

$$J_{74} : -(d_{13} d_{14}) - c_{16} d_{15} - 2 d_{14} e_7 - 2 d_{13} e_8 - 4 e_7 e_8 - 2 d_{13} f_2 - 2 e_7 f_2 - e_1 g_2 - d_4 g_5 = 0$$

$$J_{75} : d_5 d_{14} - c_{14} e_3 + 2 d_5 e_8 - d_{13} e_8 - e_7 e_8 + c_5 e_{12} + d_5 f_2 - d_{13} f_2 - e_7 f_2 - e_1 g_2 - d_4 g_5 = 0$$

$$J_{76} : c_{14} d_{15} + d_5 g_2 + d_{13} g_2 = 0$$

$$J_{77} : 3 e_7 g_2 = 0$$

$$J_{78} : -(c_{17} d_{15}) + 2 e_8 f_2 + f_2^2 + c_{11} f_9 - e_2 g_2 - e_{10} g_2 - f_4 g_2 + f_2 g_4 - d_5 g_5 + d_{13} g_5 + 2 e_7 g_5 = 0$$

$$J_{79} : -(c_9 c_{16}) + c_7 c_{18} + c_{17} d_4 - c_8 d_{13} + c_{16} d_{13} + c_7 d_{14} + c_{14} e_1 + 2 c_{16} e_7 + 2 c_7 e_8 - c_5 e_{10} + c_{13} e_{10} + c_4 e_{11} + c_7 f_2 + c_4 f_5 - c_7 g_4 - c_4 h_1 = 0$$

$$J_{80} : c_{14} c_{18} - c_{14} d_{14} + c_{14} e_8 - c_{11} e_{11} + c_{11} f_5 + c_8 g_2 + c_{16} g_2 + c_{14} g_4 + c_5 g_5 - c_{13} g_5 + c_{11} h_1 = 0$$

$$J_{81} : 2 d_{14} e_1 - d_{13} e_2 - c_{16} e_3 + 3 e_1 e_8 - d_5 e_{10} + d_{13} e_{10} + 3 e_7 e_{10} + d_4 e_{11} + c_7 e_{12} + e_1 f_2 - d_{13} f_4 - c_4 f_9 - e_1 g_4 - d_4 h_1 = 0$$

$$J_{82} : -(c_9 c_{17}) + c_8 c_{18} + c_{17} d_5 + c_{14} e_2 + 2 c_8 e_8 + c_{14} e_{10} + c_8 f_2 - c_{16} f_2 + c_{14} f_4 + c_5 f_5 - c_{13} f_5 + c_{11} f_7 - c_7 g_5 - c_4 h_2 = 0$$

$$J_{83} : d_{14} e_2 - c_{17} e_3 + 3 e_2 e_8 + e_8 e_{10} + c_8 e_{12} + e_2 f_2 - e_{10} f_2 + e_8 f_4 - d_{13} f_5 - e_7 f_5 - c_5 f_9 - e_1 g_5 - d_4 h_2 = 0$$

$$J_{84} : c_9 d_{14} - c_8 d_{15} - c_{16} d_{15} + c_{14} e_3 + 2 c_9 e_8 - c_5 e_{12} + c_{13} e_{12} + c_9 f_2 - c_4 h_3 = 0$$

$$J_{85} : c_{16} d_{15} + d_{14} e_7 - d_{13} e_8 + e_7 e_8 + c_{13} e_{12} + e_1 g_2 - c_4 h_3 = 0$$

$$J_{86} : -(d_{13} d_{14}) - d_{14} e_7 - 3 d_{13} e_8 - 3 e_7 e_8 + c_{13} e_{12} - 2 d_{13} f_2 - 2 e_7 f_2 - d_4 g_5 - c_4 h_3 = 0$$

$$J_{87} : c_{17} d_{15} + e_8^2 + c_{14} e_{12} + e_2 g_2 + e_{10} g_2 + e_8 g_4 - e_7 g_5 - c_5 h_3 = 0$$

$$J_{88} : e_8^2 + c_{14} e_{12} + 2 e_8 f_2 + f_2^2 + c_{11} f_9 - f_4 g_2 + e_8 g_4 + f_2 g_4 - d_5 g_5 + d_{13} g_5 + e_7 g_5 - c_5 h_3 = 0$$

$$J_{89} : -(e_8 e_{10}) + e_7 e_{11} + c_{16} e_{12} - e_{10} f_2 + d_{14} f_4 + 2 e_8 f_4 + f_2 f_4 - d_{13} f_5 + e_7 f_5 + c_{13} f_9 - e_1 g_5 - e_7 h_1 - d_4 h_2 - c_7 h_3 = 0$$

$$J_{90} : c_{17} e_{12} - e_{11} f_2 + 3 e_8 f_5 + f_2 f_5 + c_{14} f_9 + f_7 g_2 + f_5 g_4 - e_2 g_5 - f_4 g_5 + f_2 h_1 - d_5 h_2 + d_{13} h_2 + e_7 h_2 - c_8 h_3 = 0$$

$$J_{91} : -(d_{14} g_2) + e_8 g_2 - f_2 g_2 + 2 g_2 g_4 - c_{11} h_3 = 0$$

$$J_{92} : -(d_{15} e_2) - c_{18} e_3 + 2 d_{14} e_3 + 3 e_3 e_8 - 2 d_{15} e_{10} + c_9 e_{12} - d_5 e_{12} + d_{13} e_{12} + e_7 e_{12} + e_3 f_2 - d_{15} f_4 - d_4 h_3 = 0$$

$$J_{93} : -(d_{15} e_{11}) + c_{18} e_{12} - d_{14} e_{12} - 3 e_8 e_{12} - 2 e_{12} f_2 - 2 d_{15} f_5 - e_{12} g_4 - e_3 g_5 + d_{15} h_1 - c_9 h_3 + d_{13} h_3 + e_7 h_3 = 0$$

CONDICIONES DE NILPOTENCIA

$$N_1 : c_{11} d_{15} = 0$$

$$N_2 : c_9 + 2 d_5 + 2 d_{13} + 3 e_7 = 0$$

$$N_3 : 2 c_9 d_5 + d_5^2 + 2 c_9 d_{13} + 4 d_5 d_{13} + d_{13}^2 + c_7 d_{15} - c_5 e_3 + 3 c_9 e_7 + 6 d_5 e_7 + 3 d_{13} e_7 + 2 e_7^2 + d_4 e_8 - c_4 e_{12} + 2 d_4 f_2 = 0$$

$$N_4 : (\text{demasiado grande } \dots)$$

$$N_5 : (\text{demasiado grande } \dots)$$

$$N_6 : (\text{demasiado grande } \dots)$$

$$N_7 : c_{18} + 3 d_{14} + 3 e_8 + f_2 + 2 g_4 = 0$$

$$N_8 : 3 c_{18} d_{14} + 3 d_{14}^2 - c_{17} d_{15} + 3 c_{18} e_8 + 6 d_{14} e_8 + 2 e_8^2 - c_{14} e_{12} + c_{18} f_2 + 2 d_{14} f_2 + e_8 f_2 - c_{11} f_9 - 2 e_{10} g_2 - f_4 g_2 + 2 c_{18} g_4 + 6 d_{14} g_4 + 6 e_8 g_4 + 2 f_2 g_4 + g_4^2 - 2 d_{13} g_5 - e_7 g_5 - c_{13} h_3 = 0$$

$$N_9 : (\text{demasiado grande } \dots)$$

$$N_{10} : (\text{demasiado grande } \dots)$$

$$N_{11} : (\text{demasiado grande } \dots)$$

$$N_{12} : (\text{demasiado grande } \dots)$$

SUCESIÓN CARACTERÍSTICA (3, 3, 1, 1)

ETAPA 3

27/2/1992

LEY DEL ÁLGEBRA

$$[x_1, x_4] = x_3$$

$$[x_1, x_5] = x_4$$

$$[x_1, x_7] = x_6$$

$$[x_1, x_8] = x_7$$

$$[x_2, x_4] = c_5 x_3 + c_4 x_6$$

$$[x_2, x_5] = c_9 x_2 + c_8 x_3 + c_5 x_4 + c_7 x_6 + c_4 x_7$$

$$[x_2, x_7] = c_{14} x_3 + c_{13} x_6$$

$$[x_2, x_8] = c_{17} x_3 + c_{14} x_4 + c_{16} x_6 + c_{13} x_7$$

$$[x_3, x_5] = d_5 x_3 + d_4 x_6$$

$$[x_3, x_8] = d_{14} x_3 + d_{13} x_6$$

$$[x_4, x_5] = e_3 x_2 + e_2 x_3 + d_5 x_4 + e_1 x_6 + d_4 x_7$$

$$[x_4, x_7] = e_8 x_3 + e_7 x_6$$

$$[x_4, x_8] = e_{12} x_2 + e_{11} x_3 + (d_{14} + e_8) x_4 + e_{10} x_6 + (d_{13} + e_7) x_7$$

$$[x_5, x_6] = f_2 x_3 + (-d_{13} - 2e_7) x_6$$

$$[x_5, x_7] = -(e_{12} x_2) + f_5 x_3 + (e_8 + f_2) x_4 + f_4 x_6 + (-d_{13} - e_7) x_7$$

$$[x_5, x_8] = f_9 x_2 + f_8 x_3 + (e_{11} + f_5) x_4 + (d_{14} + 2e_8 + f_2) x_5 + f_7 x_6 + (e_{10} + f_4) x_7$$

$$[x_6, x_7] = g_2 x_3$$

$$[x_6, x_8] = g_5 x_3 + g_2 x_4 + g_4 x_6$$

$$[x_7, x_8] = h_3 x_2 + h_2 x_3 + g_5 x_4 + g_2 x_5 + h_1 x_6 + g_4 x_7$$

CONDICIONES DE JACOBI

$$J_1 : 0 = 0$$

$$J_2 : 0 = 0$$

$$J_3 : 0 = 0$$

$$J_4 : 0 = 0$$

$$J_5 : 0 = 0$$

$$J_6 : 0 = 0$$

$$J_7 : 0 = 0$$

$$J_8 : 0 = 0$$

$$J_9 : 0 = 0$$

$$J_{10} : 0 = 0$$

$$J_{11} : 0 = 0$$

$$J_{12} : 0 = 0$$

$$J_{13} : 0 = 0$$

$$J_{14} : 0 = 0$$

$$J_{15} : 0 = 0$$

$$J_{16} : 0 = 0$$

$$J_{17} : 0 = 0$$

$$J_{18} : 0 = 0$$

$$J_{19} : 0 = 0$$

$$J_{20} : 0 = 0$$

$$J_{21} : 0 = 0$$

$$J_{22} : 0 = 0$$

$$J_{23} : 0 = 0$$

$$J_{24} : 0 = 0$$

$$J_{25} : 0 = 0$$

$$J_{26} : 0 = 0$$

$$J_{27} : c_4 c_9 - c_5 d_4 + c_{13} d_4 + c_4 d_5 - c_4 d_{13} - 3 c_4 e_7 = 0$$

$$J_{28} : 0 = 0$$

$$J_{29} : 0 = 0$$

$$J_{30} : 0 = 0$$

$$J_{31} : 0 = 0$$

$$J_{32} : 0 = 0$$

$$J_{33} : -(c_{13} e_3) - d_5 e_7 + e_7^2 + d_4 e_8 + c_4 e_{12} = 0$$

$$J_{34} : 0 = 0$$

$$J_{35} : c_5 c_9 + c_{14} d_4 - c_4 e_8 + c_4 f_2 = 0$$

$$J_{36} : -(c_9 c_{13}) + c_{14} d_4 - c_5 e_7 + c_{13} e_7 + c_4 e_8 + c_4 f_2 = 0$$

$$J_{37} : 0 = 0$$

$$J_{38} : 0 = 0$$

$$J_{39} : 0 = 0$$

$$J_{40} : -(c_4 g_2) = 0$$

$$J_{41} : -(c_4 g_2) = 0$$

$$J_{42} : -(c_4 g_2) = 0$$

$$J_{43} : c_4 g_2 = 0$$

$$J_{44} : c_4 g_2 = 0$$

$$J_{45} : c_4 g_2 = 0$$

$$J_{46} : -(c_9 c_{14}) + c_{14} d_5 - c_{14} d_{13} - c_{14} e_7 + c_5 f_2 - c_{13} f_2 - c_7 g_2 = 0$$

$$J_{47} : c_9 g_2 = 0$$

$$J_{48} : -(d_4 g_2) = 0$$

$$J_{49} : -(d_4 g_2) = 0$$

$$J_{50} : -(d_4 g_2) = 0$$

$$J_{51} : -(d_4 g_2) = 0$$

$$J_{52} : -(d_4 g_2) = 0$$

$$J_{53} : d_4 g_2 = 0$$

$$J_{54} : d_4 g_2 = 0$$

$$J_{55} : d_4 g_2 = 0$$

$$J_{56} : 0 = 0$$

$$J_{57} : -(c_{14} e_3) - d_{13} e_8 - e_7 e_8 + c_5 e_{12} - e_7 f_2 - e_1 g_2 = 0$$

$$J_{58} : (d_5 - e_7) g_2 = 0$$

$$J_{59} : -((d_{13} + e_7) g_2) = 0$$

$$J_{60} : (d_{13} + e_7) g_2 = 0$$

$$J_{61} : (-d_5 + 2 d_{13} + 3 e_7) g_2 = 0$$

$$J_{62} : -(c_5 d_{13}) + c_{13} d_{13} + c_4 d_{14} + c_4 e_8 - c_4 g_4 = 0$$

$$J_{63} : -(c_9 c_{13}) + c_{14} d_4 - c_5 d_{13} + c_{13} d_{13} + c_4 d_{14} - c_5 e_7 + c_{13} e_7 + 2 c_4 e_8 + c_4 f_2 - c_4 g_4 = 0$$

$$J_{64} : (c_5 - c_{13}) g_2 = 0$$

$$J_{65} : -(d_5 d_{13}) + d_{13}^2 + 2 d_4 d_{14} + 2 d_{13} e_7 + 2 d_4 e_8 + d_4 f_2 - d_4 g_4 = 0$$

$$J_{66} : -(d_5 d_{13}) + d_{13}^2 + 2 d_4 d_{14} - c_{13} e_3 - d_5 e_7 + 2 d_{13} e_7 + e_7^2 + 3 d_4 e_8 + c_4 e_{12} + d_4 f_2 - d_4 g_4 = 0$$

$$J_{67} : e_3 g_2 = 0$$

$$J_{68} : -(e_3 g_2) = 0$$

$$J_{69} : (-d_5 + d_{13} + 2 e_7) g_2 = 0$$

$$J_{70} : c_{14} d_{13} + c_{14} e_7 + c_5 e_8 - c_{13} e_8 - c_4 g_5 = 0$$

$$J_{71} : -(c_9 c_{14}) + c_{14} d_5 + c_5 e_8 - c_{13} e_8 + c_5 f_2 - c_{13} f_2 - c_7 g_2 - c_4 g_5 = 0$$

$$J_{72} : -(c_{14} d_{13}) + c_{14} e_7 + c_7 g_2 + c_4 g_5 = 0$$

$$J_{73} : d_5 d_{14} + 2 d_5 e_8 + d_5 f_2 - d_{13} f_2 - d_4 g_5 = 0$$

$$J_{74} : -(d_{13} d_{14}) - 2 d_{14} e_7 - 2 d_{13} e_8 - 4 e_7 e_8 - 2 d_{13} f_2 - 2 e_7 f_2 - e_1 g_2 - d_4 g_5 = 0$$

$$J_{75} : d_5 d_{14} - c_{14} e_3 + 2 d_5 e_8 - d_{13} e_8 - e_7 e_8 + c_5 e_{12} + d_5 f_2 - d_{13} f_2 - e_7 f_2 - e_1 g_2 - d_4 g_5 = 0$$

$$J_{76} : (d_5 + d_{13}) g_2 = 0$$

$$J_{77} : 3 e_7 g_2 = 0$$

$$J_{78} : 2 e_8 f_2 + f_2^2 - e_2 g_2 - e_{10} g_2 - f_4 g_2 + f_2 g_4 - d_5 g_5 + d_{13} g_5 + 2 e_7 g_5 = 0$$

$$J_{79} : -(c_9 c_{16}) + c_{17} d_4 - c_8 d_{13} + c_{16} d_{13} + c_7 d_{14} + c_{14} e_1 + 2 c_{16} e_7 + 2 c_7 e_8 - c_5 e_{10} + c_{13} e_{10} + c_4 e_{11} + c_7 f_2 + c_4 f_5 - c_7 g_4 - c_4 h_1 = 0$$

$$J_{80} : -(c_{14} d_{14}) + c_{14} e_8 + c_8 g_2 + c_{16} g_2 + c_{14} g_4 + c_5 g_5 - c_{13} g_5 = 0$$

$$J_{81} : 2 d_{14} e_1 - d_{13} e_2 - c_{16} e_3 + 3 e_1 e_8 - d_5 e_{10} + d_{13} e_{10} + 3 e_7 e_{10} + d_4 e_{11} + c_7 e_{12} + e_1 f_2 - d_{13} f_4 - c_4 f_9 - e_1 g_4 - d_4 h_1 = 0$$

$$J_{82} : -(c_9 c_{17}) + c_{17} d_5 + c_{14} e_2 + 2 c_8 e_8 + c_{14} e_{10} + c_8 f_2 - c_{16} f_2 + c_{14} f_4 + c_5 f_5 - c_{13} f_5 - c_7 g_5 - c_4 h_2 = 0$$

$$J_{83} : d_{14} e_2 - c_{17} e_3 + 3 e_2 e_8 + e_8 e_{10} + c_8 e_{12} + e_2 f_2 - e_{10} f_2 + e_8 f_4 - d_{13} f_5 - e_7 f_5 - c_5 f_9 - e_1 g_5 - d_4 h_2 = 0$$

$$J_{84} : c_9 d_{14} + c_{14} e_3 + 2 c_9 e_8 - c_5 e_{12} + c_{13} e_{12} + c_9 f_2 - c_4 h_3 = 0$$

$$J_{85} : d_{14} e_7 - d_{13} e_8 + e_7 e_8 + c_{13} e_{12} + e_1 g_2 - c_4 h_3 = 0$$

$$J_{86} : -(d_{13} d_{14}) - d_{14} e_7 - 3 d_{13} e_8 - 3 e_7 e_8 + c_{13} e_{12} - 2 d_{13} f_2 - 2 e_7 f_2 - d_4 g_5 - c_4 h_3 = 0$$

$$J_{87} : e_8^2 + c_{14} e_{12} + e_2 g_2 + e_{10} g_2 + e_8 g_4 - e_7 g_5 - c_5 h_3 = 0$$

$$J_{88} : e_8^2 + c_{14} e_{12} + 2 e_8 f_2 + f_2^2 - f_4 g_2 + e_8 g_4 + f_2 g_4 - d_5 g_5 + d_{13} g_5 + e_7 g_5 - c_5 h_3 = 0$$

$$J_{89} : -(e_8 e_{10}) + e_7 e_{11} + c_{16} e_{12} - e_{10} f_2 + d_{14} f_4 + 2 e_8 f_4 + f_2 f_4 - d_{13} f_5 + e_7 f_5 + c_{13} f_9 - e_1 g_5 - e_7 h_1 - d_4 h_2 - c_7 h_3 = 0$$

$$J_{90} : c_{17} e_{12} - e_{11} f_2 + 3 e_8 f_5 + f_2 f_5 + c_{14} f_9 + f_7 g_2 + f_5 g_4 - e_2 g_5 - f_4 g_5 + f_2 h_1 - d_5 h_2 + d_{13} h_2 + e_7 h_2 - c_8 h_3 = 0$$

$$J_{91} : g_2 (-d_{14} + e_8 - f_2 + 2 g_4) = 0$$

$$J_{92} : 2 d_{14} e_3 + 3 e_3 e_8 + c_9 e_{12} - d_5 e_{12} + d_{13} e_{12} + e_7 e_{12} + e_3 f_2 - d_4 h_3 = 0$$

$$J_{93} : -(d_{14} e_{12}) - 3 e_8 e_{12} - 2 e_{12} f_2 - e_{12} g_4 - e_3 g_5 - c_9 h_3 + d_{13} h_3 + e_7 h_3 = 0$$

UNIVERSIDAD DE VALPARAISO

Presentado al Excmo. Consejo de la Universidad de Valparaíso para su calificación y grado de Doctor en Ciencias Exactas y Naturales

GERARDO VAZEIRAS REINA

SOBRE LAS COMPONENTES IRREDUCIBLES DE LA VARIETADE DE LEYES DE ALGEBRA DE LIE NILPOTENTES COMPLEJAS DE DIMENSION 8

Apto "cum Laude"

5 MAYO

1992

José Vicente

El Vocal,

El Doctorado,

El Doctorado,