# Open-Phase Fault-Tolerant Direct Torque Control Technique for Five-Phase Induction Motor Drives

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Abstract—Direct torque control (DTC) has been widely used as an alternative to traditional field-oriented control (FOC) methods for three-phase drives. The conventional DTC scheme has been successfully extended to multiphase drives in recent times, using hysteresis regulators to independently track the desired torque and flux in symmetrical five-phase induction machines (IM). The fault-tolerant capability of multiphase drives is an interesting intrinsic advantage for safety-critical applications, where recent research has demonstrated the effectiveness of FOC schemes to perform ripple-free post-fault operation. In spite of the utility of DTC methods in normal operation of the multiphase machine, no extension to manage the post-fault operation of the drive is found in the literature. In this paper, a novel fault-tolerant DTC scheme is presented. The performance of the proposed method is experimentally validated in a five-phase IM drive considering an open-phase fault condition. Provided tests analyze steady and transient states, including the transition from pre- to post-fault operation. Obtained results prove the interest of the proposal, which ensures the open-phase fault-tolerant capability of DTC controlled five-phase IM drives.

Index Terms—Direct torque control (DTC), fault-tolerant capability, multiphase induction motor (IM) drives, open-phase fault operation.

#### I. INTRODUCTION

MULTIPHASE drives have gained special relevance in modern times for their use in applications where high overall system reliability and reduction in the total power per phase are required, such as in electric vehicles and trains, all-electric ships, more-electric aircrafts or wind power generation systems [1–3]. Conducted research has recently focused on the

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design of multiphase machines and the effect of the stator winding connection [4,5], on the consideration of power converters' topologies [6] and on new control schemes to exploit the additional degrees of freedom [7].

An extended case example of multiphase drives is the symmetrical five-phase induction machine with sinusoidally distributed stator windings. Regarding the existing control techniques, the Rotor-Field Oriented Control (RFOC) method, based on an outer PI-based speed control loop and inner current controllers, is the most widespread control technique in the multiphase case. This technique has been applied in five-phase IM drives using conventional PI-based current regulators or model-based predictive current controllers in healthy [8,9] and faulty operation [10-12]. Other well-known non-linear controller like DTC, a leading technology for three-phase induction motor drives since 1995 [13], has not been so deeply extended to the multiphase case, where only healthy operation of five-phase IM drives is considered [14,15]. The use of DTC in five-phase IM is limited due to the impossibility of regulating more than two degrees of freedom (electrical torque and stator flux), which are regulated using hysteresis controllers and switching tables that impose the stator voltage of the five-phase IM. The proposed schemes successfully perform in healthy state, including the low-speed operation, using additional virtual voltage vectors and diminishing non-torque stator current components.

Improving the fault-tolerant capability is a hot topic in fivephase induction motor drives [4,5,10–12,16,17]. However, this fault-tolerant capability using DTC methods has not been stated yet, being this a main contribution of our work. Notice that the number of degrees of freedom reduces when faulty situations appear and the inconvenient of using the DTC method is expected to be mitigated, something that has not been verified yet. Although different types of faults can occur, the most considered is the open-phase one that leads to a reduction in the number of active phases in the multiphase drive [3]. Important requirements must be introduced to take into account the openphase fault occurrence [10-12]. For example, stator current references must be modified to preserve the fundamental component of the air gap magnetic field, where different postfault control criteria (e.g. reduce copper losses or ensure maximum torque capability [16-18]) can be applied. If inner current control loops are implemented using linear controllers, the oscillating nature of the current references makes imperative the use of proportional resonant (PR) regulators in the post-fault

operation of the drive, being this the main reason of a change in the control scheme between pre- and post-fault operation. If a model-based predictive current control scheme is used, the model of the electrical drive under the faulty condition must be considered and the applied cost function must change.

This work extends the DTC method used in normal operation of five-phase IM drives to the open-phase fault procedure. The proposed DTC technique, initially presented in [19] but experimentally validated here, requires i) the modification of classic DTC structures using a reduced-order transformation matrix, ii) the redefinition of the utilized virtual voltage vectors by means of the available voltage vectors in faulty operation, and iii) the elaboration of a new look-up table for the control purpose. The paper is organized as follows. Section II analyzes the five-phase IM drive under healthy and faulty operations, showing the effect of the open-phase fault occurrence in the physical system. The proposed fault-tolerant DTC scheme is detailed in Section III. Section IV provides experimental results to show and discuss the performance of the multiphase drive using the proposed post-fault controller. Finally, the conclusions are presented in the last section.

# II. FIVE-PHASE IM DRIVE IN NORMAL AND OPEN-PHASE FAULT OPERATION

The system under study is based on a five-phase IM with a squirrel-cage rotor and symmetrically distributed stator windings (with a fixed spatial displacement of  $\vartheta=2\pi/5$  between windings). A simplified scheme of the drive is shown in Fig. 1. where the machine is powered by a two-level five-phase voltage source inverter (VSI). If the switching state of each power converter leg is called  $S_i$ , where  $i=\{a, b, c, d, e\}$  and  $S_i=0$  if the lower switch is ON and the upper switch is OFF or  $S_i=1$  if the opposite occurs, then the vector  $[S_a S_b S_c S_d S_e]^T$  identifies the 2<sup>5</sup>=32 available switching states and stator voltages. Each stator phase voltage can be obtained from this vector and the DC-link voltage  $(V_{dc})$  as it is stated in (1) and, applying the currentinvariant decoupling Clarke's transformation defined in (2), can be mapped into two orthogonal stationary subspaces,  $\alpha$ - $\beta$  and x-y, plus a zero-sequence component (see Fig. 2, where stator voltage vectors have been identified using a decimal number equivalent to the binary number  $[S_a S_b S_c S_d S_e]$ ).

$$\begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \\ v_{ds} \\ v_{vs} \end{bmatrix} = \underbrace{V_{dc}}_{-1} \begin{bmatrix} 4 & -1 & -1 & -1 & -1 \\ -1 & 4 & -1 & -1 & -1 \\ -1 & -1 & 4 & -1 & -1 \\ -1 & -1 & -1 & 4 & -1 \\ -1 & -1 & -1 & -1 & 4 \end{bmatrix} \begin{bmatrix} S_a \\ S_b \\ S_c \\ S_d \\ S_s \end{bmatrix}$$
(1)

$$\begin{bmatrix} v_{os} \\ v_{\beta s} \\ v_{xs} \\ v_{ys} \\ v_{zs} \end{bmatrix} = \frac{2}{5} \begin{bmatrix} 1 & \cos\vartheta & \cos 2\vartheta & \cos 3\vartheta & \cos 4\vartheta \\ 0 & \sin\vartheta & \sin 2\vartheta & \sin 3\vartheta & \sin 4\vartheta \\ 1 & \cos 2\vartheta & \cos 4\vartheta & \cos\vartheta & \cos 3\vartheta \\ 0 & \sin 2\vartheta & \sin 4\vartheta & \sin\vartheta & \sin 3\vartheta \\ 1/2 & 1/2 & 1/2 & 1/2 & 1/2 \end{bmatrix} \begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \\ v_{ds} \\ v_{es} \end{bmatrix}$$
(2)

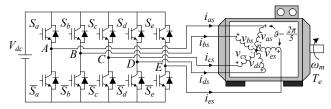


Fig. 1. Schematic diagram of the five-phase IM drive.

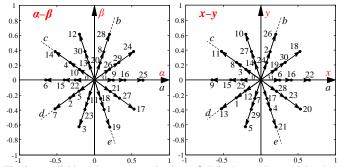


Fig. 2. Available voltage vectors in the  $\alpha$ - $\beta$  (left plot) and x-y (right plot) planes in normal operation.

The five-phase IM can be modeled in a stationary reference frame with a set of voltage equilibrium equations obtained from the stator and rotor electromagnetic circuits. All the standard assumptions normally applied in three-phase IM are considered, including sinusoidal spatial MMF distribution, uniform air gap and some neglected effects like magnetic saturation, core losses and mutual leakage inductance between windings of different phases. Taking this into account, the following set of equations describes the behavior of the multiphase machine:

$$[V_s] = [R_s] \cdot [I_s] + \frac{d}{dt} [\lambda_s]$$

$$= [R_s] \cdot [I_s] + [L_{ss}] \cdot \frac{d}{dt} [I_s] + \frac{d}{dt} ([L_{sr}(\theta)] \cdot [I_r])$$
(3)

$$[V_r] = [R_r] \cdot [I_r] + \frac{d}{dt} [\lambda_r]$$

$$= [R_r] \cdot [I_r] + [L_{rr}] \cdot \frac{d}{dt} [I_r] + \frac{d}{dt} ([L_{rs}(\theta)] \cdot [I_s])$$
(4)

$$[R_s] = R_s \cdot [I_5] \tag{5}$$

$$[R_r] = R_r \cdot [I_5] \tag{6}$$

$$[L_{ss}] = L_{ls} \cdot [I_5] + M \cdot [\Lambda(\vartheta)]$$
(7)

$$[L_{rr}] = L_{lr} \cdot [I_5] + M \cdot [\Lambda(\vartheta)]$$
(8)

$$[L_{sr}(\theta)] = [L_{rs}(\theta)]^T = M \cdot [\Delta(\theta)]$$
(9)

$$\theta = \int_{-\infty}^{t} \omega_r dt \tag{10}$$

$$[\Lambda(\vartheta)] = \begin{bmatrix} 1 & \cos\vartheta & \cos 2\vartheta & \cos 3\vartheta & \cos 4\vartheta \\ \cos 4\vartheta & 1 & \cos\vartheta & \cos 2\vartheta & \cos 3\vartheta \\ \cos 3\vartheta & \cos 4\vartheta & 1 & \cos\vartheta & \cos 2\vartheta \\ \cos 2\vartheta & \cos 3\vartheta & \cos 4\vartheta & 1 & \cos\vartheta \\ \cos\vartheta & \cos 2\vartheta & \cos 3\vartheta & \cos 4\vartheta & 1 \end{bmatrix}$$
(11)

$$[\Delta(\theta)] = \begin{bmatrix} \cos \Delta_1 & \cos \Delta_2 & \cos \Delta_3 & \cos \Delta_4 & \cos \Delta_5 \\ \cos \Delta_5 & \cos \Delta_1 & \cos \Delta_2 & \cos \Delta_3 & \cos \Delta_4 \\ \cos \Delta_4 & \cos \Delta_5 & \cos \Delta_1 & \cos \Delta_2 & \cos \Delta_3 \\ \cos \Delta_3 & \cos \Delta_4 & \cos \Delta_5 & \cos \Delta_1 & \cos \Delta_2 \\ \cos \Delta_2 & \cos \Delta_3 & \cos \Delta_4 & \cos \Delta_5 & \cos \Delta_1 \end{bmatrix}$$
 (12)

where V, I and  $\lambda$  denote voltage, current and flux variables, and the s and r subscripts identify the stator and rotor variables, respectively. The electrical parameters of the machine are  $R_s$  and  $R_r$  (stator and rotor resistances), M (mutual inductance), and  $L_{ls}$  and  $L_{lr}$  (stator and rotor leakage inductances), while  $[I_5]$  represents an identity matrix of order 5 and the angles  $\Delta_k$  are defined as  $\Delta_k = \theta + (k-1)\vartheta$ , where  $k = \{1,2,3,4,5\}$  and  $\theta$  is the instantaneous rotor azimuth with respect to the  $\alpha$ -axis, obtained through the rotor electrical speed  $(\omega_r)$ .

The equilibrium equation (13) is verified during the normal operation of the multiphase drive. However, the machine becomes asymmetrical when an open-phase fault occurs and the sum of healthy stator phase voltages is no longer zero. Since the five-phase machine is symmetrical, the analysis when the fault appears can consider any faulty phase without lack of generality. Then, phase 'a' will be considered like the faulty phase from now on, being  $i_{as}$ =0. In any case, one degree of freedom is lost in the multiphase drive when the fault appears, and a fixed relationship between  $\alpha$  and x current components is obtained as it is stated in (14). It is then necessary to include the induced back-EMF of the phase 'a' in the new equilibrium stator phase voltage equation (15), which is obtained from (1) with  $L_m$ =5M/2.

$$0 = v_{as} + v_{bs} + v_{cs} + v_{ds} + v_{es}$$
 (13)

$$i_{as} = 0 = i_{as} + i_{xs} \implies i_{as} = -i_{xs} \tag{14}$$

$$\begin{bmatrix} v_{bs} \\ v_{cs} \\ v_{ds} \\ v_{es} \end{bmatrix} = \frac{V_{dc}}{4} \begin{bmatrix} 3 & -1 & -1 & -1 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 3 & -1 \\ -1 & -1 & -1 & 3 \end{bmatrix} \begin{bmatrix} S_b \\ S_c \\ S_d \\ S_e \end{bmatrix} - \frac{L_m \left( \frac{di_{os}}{dt} + \frac{di_{os}}{dt} \right)}{4} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} (15)$$

Equation (15) links switching states and stator phase voltages of healthy phases, being the back-EMF of phase 'a' (obtained from the neutral voltage evaluation, [10]) the second term on the right hand side. This back-EMF term can be neglected, as it is shown in [11], and will not be considered in what follows for the sake of simplicity. The modified Clarke's transformation presented in [10] and shown in (16) can be used in the post-fault operation to compensate asymmetries of the machine. Then, a symmetrical post-fault model of the machine is obtained, as well as circular trajectories of the stator currents in the  $\alpha$ - $\beta$  plane, and the same set of equations in  $\alpha - \beta - x - y$  coordinates is generated in normal and post-fault conditions. Consequently, the same model of the drive under healthy and fault conditions is used, which simplifies the treatment of the fault. However, the open-phase fault situation is characterized by four healthy phases, and the number of switching states is reduced from  $2^{5}=32$  to  $2^{4}=16$ , as it is shown in Fig. 3.

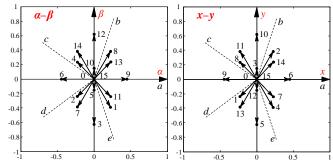


Fig. 3. Available voltage vectors in the  $\alpha$ - $\beta$  (left plot) and x-y (right plot) planes in open-phase fault operation.

$$\begin{bmatrix} v_{\alpha s} \\ v_{\beta s} \\ v_{ys} \\ v_{zs} \end{bmatrix} = \frac{2}{5} \begin{bmatrix} \cos \vartheta - 1 & \cos 2\vartheta - 1 & \cos 3\vartheta - 1 & \cos 4\vartheta - 1 \\ \sin \vartheta & \sin 2\vartheta & \sin 3\vartheta & \sin 4\vartheta \\ \sin 2\vartheta & \sin 4\vartheta & \sin 6\vartheta & \sin 8\vartheta \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} v_{bs} \\ v_{cs} \\ v_{ds} \\ v_{es} \end{bmatrix}$$
(16)

#### III. DTC SCHEME IN OPEN-PHASE OPERATION

Traditional DTC methods have been successfully extended to five-phase drives, where some advances have been recently achieved in the application of switching table DTC techniques at healthy operation of the drive [14,15]. The main control criterion is to maximize torque production while minimizing overall losses, and a stator voltage vector is therefore applied every sampling period for reference torque and stator flux tracking. The controller (see left plot in Fig. 4) is based on a three-level torque hysteresis comparator and two two-level hysteresis-based control loops for regulating the flux, where the low-speed operation of the drive is also taken into account and the effect of neglecting the stator resistance is considered with a speed threshold called  $\omega_{mth}$  (100 rpm in our case). In healthy operation, ten different sectors appear in  $\alpha$ - $\beta$  and x-y planes, with a small, a medium and a large voltage vector in every sector (notice in Fig. 2 that a large vector in the  $\alpha$ - $\beta$  plane results in a small vector in the x-y plane and vice versa). However, these available stator voltage vectors are not applied, and Virtual Voltage Vectors (VV<sub>i</sub> from now on) are created to reduce harmonic components in the x-y plane, which do not produce torque in a distributed winding multiphase IM. Thus, a null voltage vector ( $V_0$  or  $V_{31}$ ) or  $VV_i$  is applied to the five-phase IM during a sampling period  $T_s$ , being  $VV_i$  obtained with one large and one medium voltage vector that must be in-phase in the  $\alpha$ - $\beta$  plane to generate a zero average voltage vector in the x-y plane. As a result, the synthesized  $VV_i$ , shown in Fig. 5(a), has a magnitude of  $((5-\sqrt{5})/5) \cdot V_{dc}$  with normalized dwell times of  $K_v$  $=(3-\sqrt{5})/2$  and  $1-K_v$  referred to  $T_s$ . Electrical torque and flux estimators are used to calculate the hysteresis regulators error signals and identify the sector on the basis of the stator flux position, and the applied voltage vector ( $VV_i$  with i=1 to 10 or the null voltage vectors  $V_0$  and  $V_{31}$ ) is obtained from the lookup table shown in Table I.

Some modifications must be applied when an open-phase fault occurs in order to ensure the post-fault operation of the multiphase drive. The overall aim must be the extension of the control technique to the post-fault situation, where the open-

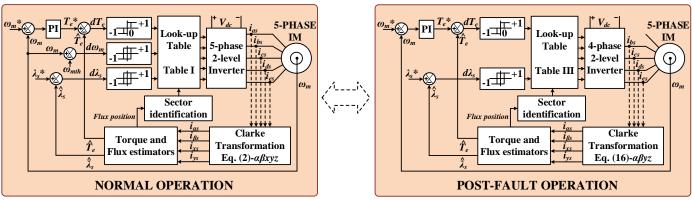


Fig. 4. Proposed fault-tolerant DTC technique in symmetrical five-phase IM drives. The method applied during the healthy or normal operation of the drive (left side) must be modified during open-phase post fault operation (right side). The symbols '^' and '\*' represent estimated and reference variables, respectively. The electrical drive is operated below rated speed, and the stator flux reference ( $\lambda_s$ \*) is mantained constant and equal to its nominal value. The stator flux and the electrical torque are estimated using observers detailed in [14,15].

 $\label{eq:table_interpolation} TABLE\ I$  Look-up table for the DTC controller in healthy operation

$d\lambda_s$	$dT_e$	$d\omega_m$	Position of stator flux (Sector)									
			1	2	3	4	5	6	7	8	9	10
	+1	+1	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$
		-1	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$
+1	-1	+1	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$
+1		-1	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_9$
	0	+1	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_{o}$	$V_{31}$
		-1	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_{o}$	$V_{31}$
-1	+1	+1	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$
		-1	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$	$VV_4$
	-1	+1	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$
		-1	$VV_7$	$VV_8$	$VV_9$	$VV_{10}$	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$
	0	+1	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{3I}$	$V_0$	$V_{31}$	$V_0$	$V_{3I}$	$V_0$
		-1	$V_{31}$	$V_0$	$V_{3I}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$	$V_{31}$	$V_0$

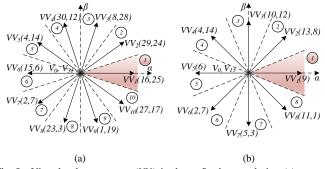


Fig. 5. Virtual voltage vectors  $(VV_i)$  in the  $\alpha$ - $\beta$  subspace during (a) normal and (b) open-phase post-fault operation.

phase fault reduces the number of controllable variables (only  $\alpha$ ,  $\beta$  and y current components, while x current component is found to be  $i_{xs}=-i_{\alpha s}$ ), being  $\alpha-\beta$  and x-y subspaces no longer orthogonal. In this case, the proposed open-phase fault DTC scheme reduces copper losses in the faulty operation and is designed with the following considerations:

- New VV<sub>i</sub> values are obtained to take into account that there are only 16 available voltage vectors in post-fault operation, as it is illustrated in Fig. 3.
- The additional freedom degree (y component) is used to obtain zero average volts-per-seconds in the y direction during the post-fault operation of the drive. This should be equivalent to the minimum copper loss criterion assuming that machine asymmetries do not exist, because the stator

current component in the y axis ( $i_{ys}$ ) will be low and close to zero [16–18]. The existence of some degree of asymmetry is then regarded as a non-modelled effect that may cause some disturbance in the current regulation.

Eight sectors appear in the open-phase fault situation, which leads to eight  $VV_i$  in the  $\alpha$ - $\beta$  plane defined as:

$$VV_i(v_1, v_2) = v_1 K_{v1} + v_2 K_{v2}$$
(17)

where  $v_I$  and  $v_2$  are the two available voltage vectors and  $K_{vI}$  and  $K_{v2}$  are the dwell time ratios that define  $VV_i$  with the condition  $i_{ys}$ =0. Sectors 1 and 5 are exceptions and only use one vector since it does not produce voltage in the y direction. The obtained post-fault  $VV_i$  and sectors are depicted in Fig. 5b, and the new obtained dwell time ratios are shown in Table II. The look-up table that takes into account the open-phase fault situation is detailed in Table III, where the applied stator voltage vector is the null voltage vector ( $V_0$  or  $V_{I5}$ ) or  $VV_i$ , with i=1 to 8.

The post-fault DTC technique is detailed in Fig. 4 (see right plot). The controller includes an outer PI-based speed control loop and two inner torque and flux hysteresis regulators ( $d\lambda_s$  and  $dT_e$  error signals). Notice that the low speed region cannot be considered like in healthy case, because of the defined sectors and  $VV_i$  values. Finally, electrical torque and flux estimators are used to identify the sector on the basis of the stator flux position to obtain the applied voltage vector (see Table III). Notice that the estimators use the same equations under healthy and faulty

TABLE II
DWELL TIMES DURING THE OPEN-PHASE FAULT OPERATION

Dwell Time	Virtual Voltage Vectors									
	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$		
	(9)	(13,8)	(10,12)	(4,14)	(6)	(2,7)	(5,3)	(11,1)		
$K_{vI}$	1	0.382	0.191	0.382	1	0.382	0.191	0.382		
$K_{v2}$	-	0.618	0.809	0.618	-	0.618	0.809	0.618		

TABLE III

LOOK-UP TABLE FOR THE DTC CONTROLLER IN POST-FAULT SITUATION

$d\lambda_s$	$dT_e$	Position of stator flux (Sector)								
$a_{\lambda_s}$		1	2	3	4	5	6	7	8	
+1	+1	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_1$	
	-1	$VV_8$	$VV_1$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	$VV_6$	$VV_7$	
	0	$V_0$	$V_{15}$	$V_0$	$V_{15}$	$V_0$	$V_{15}$	$V_0$	$V_{15}$	
-1	+1	$VV_4$	$VV_5$	$VV_6$	$VV_7$	$VV_8$	$VV_1$	$VV_2$	$VV_3$	
	-1	$VV_6$	$VV_7$	$VV_8$	$VV_I$	$VV_2$	$VV_3$	$VV_4$	$VV_5$	
	0	$V_{15}$	$V_0$	$V_{15}$	$V_0$	$V_{15}$	$V_0$	$V_{15}$	$V_0$	

conditions. However, one stator phase current is null in the open-phase fault condition and the modified Clarke's transformation detailed in [10] is applied, see Eq. (16).

# IV. EXPERIMENTAL RESULTS

To prove the viability and assess the performance of the proposed fault-tolerant control scheme, different experimental tests have been performed on a three-phase IM rewound to have five phases with 30-slots and three pairs of poles. The electrical machine is driven by two conventional three-phase VSIs from Semikron (two SKS-22F modules where five over six power legs are used). The DC-link voltage is set to 300 V during all the experimental tests using an external DC power supply. The electronic control unit is based on a MSK28335 board and a Texas Instruments TMS320F28335 DSP. A digital encoder (GHM510296R/2500) and the enhanced quadrature encoder pulse (eQEP) peripheral of the DSP are used to measure the rotor mechanical speed  $\omega_m$ . The load torque  $(T_L)$ , which is demanded in the tests, is set by an independently controlled DC machine that is mechanically coupled to the five-phase machine.

The performed tests consider that the open-phase fault condition occurs in phase 'a' and the fault occurrence is emulated by opening a power relay connected in series with the faulty phase. The experimental test rig is shown in Fig. 6, where some photographs of the system are included. The electrical parameters of the five-phase IM were determined using AC-time domain and standstill control tests [20,21] (Table IV summarizes the electrical and mechanical specifications of the used five-phase IM). It is important to mention that during the following experimental tests the stator flux reference ( $\lambda_s^*$ ) was set to 0.389 Wb, the applied sampling frequency was 10 kHz and the hysteresis bands of the torque and flux regulators were programmed to be at 1.06% and 1.29% of the rated values, respectively.

The behavior of the proposed DTC controller during the faulty open-phase operation of the drive is first analyzed assuming a null load torque condition and forcing a step in the speed reference from 0 to 500 rpm that is applied at t=0.1 s. Fig. 7 shows the obtained results: the mechanical speed (upper plot), estimated electrical torque (middle figure) and stator flux (lower

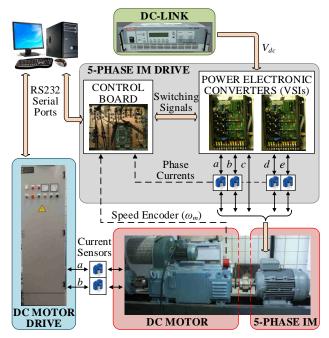


Fig. 6. Graphical scheme of the multiphase experimental test rig based on a symmetrical five-phase distributed-windings IM.

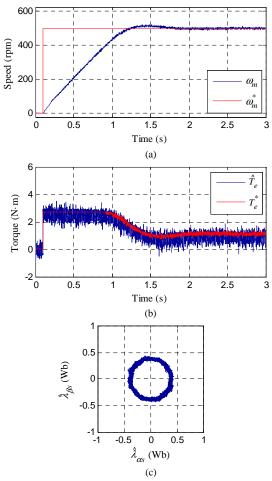
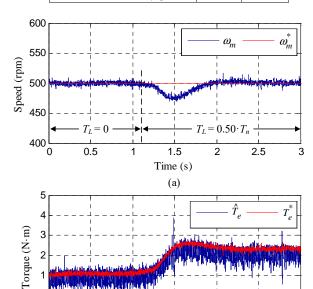
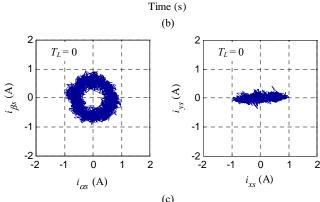


Fig. 7. Step speed response test. The reference speed is changed from 0 to 500 rpm at t=0.1 s. No load torque condition is assumed. The upper plot shows the speed response (a), while the estimated electrical torque and the stator flux in the  $\alpha$ - $\beta$  plane is depicted in plots (b) and (c), respectively. Notice that the stator flux is evaluated from the measured stator currents and the estimated stator voltages (the estimation uses the switching state of the VSI).

TABLE IV ELECTRICAL AND MECHANICAL PARAMETERS OF THE FIVE-PHASE IM

Parameter	Value	Unit
Stator resistance, $R_s$	12.85	Ω
Rotor resistance, $R_r$	4.80	Ω
Stator leakage inductance, $L_{ls}$	79.93	mH
Rotor leakage inductance, $L_{lr}$	79.93	mH
Mutual inductance, M	681.7	mH
Moment of inertia, $J$	0.02	kg-m <sup>2</sup>
Number of pole pairs, p	3	-
Rated torque, $T_n$	4.70	N-m
Rated stator flux, $\lambda_s^*$	0.389	Wb





1.5

2.5

0

0.5

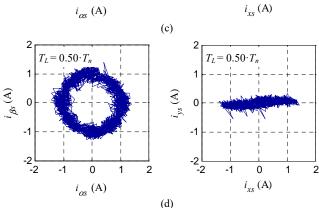


Fig. 8. Load torque rejection test where a change from 0 to 50% of the nominal load torque is applied at t=1.1 s. (a) Speed response. (b) Estimated electrical torque behavior. Stator current performance in  $\alpha$ – $\beta$  and x–y planes in steady state with (c) null and (d) 50% of the nominal torque, respectively.

illustration) behaviors. It can be observed that the proposed post-fault DTC scheme provides an accurate tracking of the reference speed and electrical torque. The performance of the estimated stator flux is also shown in Fig. 7(c), where a circle is obtained in the  $\alpha$ - $\beta$  plane polar diagram and the estimated stator flux vector has a controlled behavior in order to drive the multiphase system.

The rejection properties of the proposed DTC scheme are also analyzed when a change in the load torque is applied. The obtained results are summarized in Fig. 8, where the demanded load torque is changed while the reference speed is kept constant at 500 rpm. The DC machine is initially programmed to apply a zero load torque in opposition to the multiphase drive's electrical torque. Then, the load torque is forced to become about half of the nominal one ( $T_L$ =0.5· $T_n$ ) at t=1.1 s. It is observed a slight drop in the speed, although the controller successfully manages the disturbance, Fig. 8(a). The estimated electrical torque is also regulated to be the referred one in steady and transient states, as it is shown in Fig. 8(b), while stator currents in the  $\alpha$ - $\beta$  plane produce a circular trajectory in steady state with  $T_L$ =0 and  $T_L$ =0.5· $T_n$  conditions, as it is illustrated in

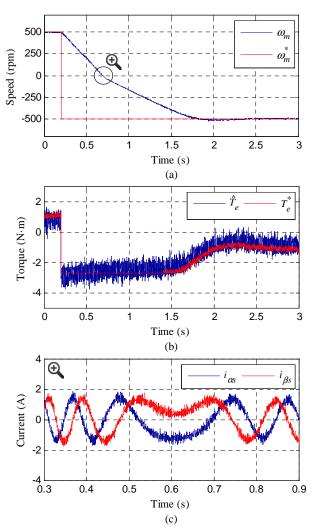


Fig. 9. Speed reversal test. The reference speed is changed from 500 to -500 rpm at 0.2 s. Speed and torque reference tracking are shown in (a) and (b) plots, respectively, while stator currents in the  $\alpha$ – $\beta$  plane is ploted at the zero-speed crossing point in (c).

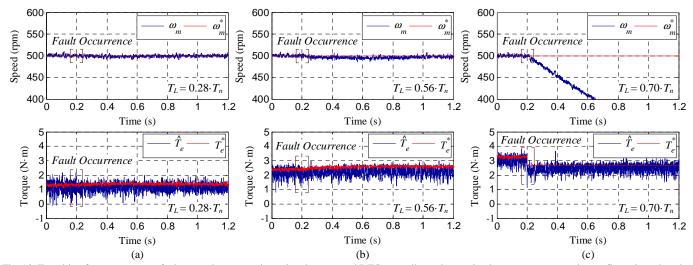


Fig. 10. Transition from pre- to post-fault open-phase operation using the proposed DTC controller and assuming instantaneous control reconfiguration when the fault appears at *t*=0.2 s. A reference speed of 500 rpm is assumed with an applied load torque of (a) 28%, (b) 56% and (c) 70% of the nominal one. The speed and estimated torque response is depicted in the upper and lower plots, respectively.

left plots of Fig. 8(c) and Fig. 8(d), respectively. This is the desired situation to guarantee a controlled electrical torque in the multiphase drive. Flat lines are also observed in the x-y plane polar plots in steady state, right drawings in Figs. 8(c) and 8(d), which is in accordance with the applied post-fault open-phase minimum copper loss criterion where  $i_{xs}$ = $-i_{\alpha s}$  and  $i_{ys}$  should be regulated around a null reference value.

A reversal speed test is afterwards generated, and a change in the reference speed from 500 to -500 rpm is forced. The change is imposed at t=0.2 s, and the results are shown in Fig. 9. The system is again operated in open-phase post-fault procedure, being null the load torque imposed by the DC machine. Appropriate tracking is again observed in the speed and the estimated electrical torque evolution, as it can be seen in Figs. 9(a) and 9(b), respectively, and the stator current performance in the  $\alpha$ - $\beta$  plane around the zero-crossing speed operating point is shown in detail in Fig. 9(c).

The transition between pre- and post-fault operation is analyzed in Fig. 10, where an open-phase fault is generated in phase 'a' using the power relay at t=0.2 s with a constant speed of 500 rpm and the system is instantaneously reconfigured. Upper plots show the speed evolution while lower figures display the estimated electrical torque response considering a demanded load torque of 28%, 56% and 70% of the nominal one in Figs. 10(a), 10(b) and 10(c), respectively. It is found that the fault occurrence does not affect the speed operation and the torque reference is accurately followed when the multiphase drive is working in the low load torque condition  $(T_L=0.28 \cdot T_n)$ , Fig. 10(a). A quite similar situation (not exactly the same because a small deviation on the reference speed tracking is obtained just after the fault occurrence) is observed when the load torque is about 56% of the nominal one, Fig. 10(b), which corresponds to the maximum controllable post-fault open-phase torque operation when the minimum copper loss post-fault control criterion is used. On the contrary, the proposed DTC scheme is not able to control the mechanical speed when the applied load torque exceeds the maximum controllable one in post-fault operation, as it is shown in Fig. 10(c). The obtained healthy stator currents before and after the fault are shown in Fig. 11, where an increment in their magnitudes is noticed to compensate the open-phase faulty situation; the magnitude of 'b' and 'e' stator currents are equal and larger than the magnitude of stator currents in 'c' and 'd' phases, which is in accordance with the minimum copper loss criterion [10].

The low speed operation of the drive is then observed in Fig. 12, where a constant reference speed of 50 rpm is maintained from pre- to post-fault operation with constant load torques of 28% and 56% of the nominal one, Fig. 12(a) and 12(b), respectively. Appropriate tracking of the reference speed (upper figures) and the electrical torque (lower plots) is obtained.

The obtained performance proves that the proposed DTC controller is effective for managing the open-phase post-fault operation of the five-phase IM drive. Note that the current ripple

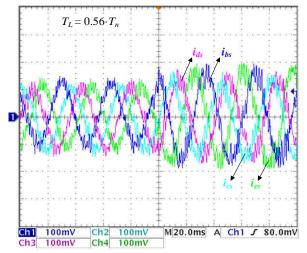


Fig. 11. Healthy stator phase currents when the open-phase fault appears and instantaneous control reconfiguration is used. The applied speed reference is 500 rpm and the demanded load torque is about 56% of the nominal one.

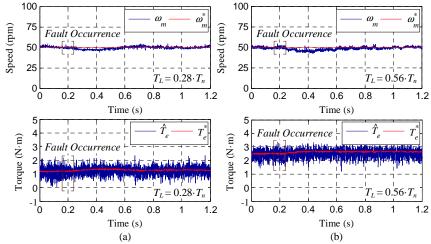


Fig. 12. Low speed operation of the five-phase drive using the proposed DTC controller. The reference speed is set to 50 rpm, while load torques of (a) 28% and (b) 56% of the nominal one are applied. The speed response and the estimated electrical torque are depicted in the upper and lower plots, respectively. The open-phase fault is forced at t=0.2 s.

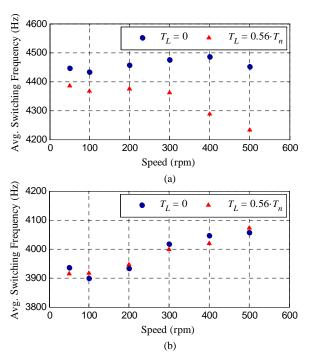


Fig. 13. Obtained average switching frequency using the proposed DTC controller in (a) healthy and (b) faulty operation when different load torques and reference speeds are applied.

is higher in DTC compared to other FOC-based control methods for similar five-phase IM drives (see [12]). However, the DTC technique provides a simpler modification of the post-fault control scheme to preserve the controllability of the system. This is an interesting characteristic in favor of the DTC method in applications where the highest reliability must be preserved and the drive must be operated in safety conditions until a corrective maintenance is carried out.

Fig. 13 shows finally the obtained average switching frequency using the proposed DTC technique. Different load torques (zero and 56% of the nominal one) and reference speeds (50, 100, 200, 300, 400 and 500 rpm) are applied, and the average switching frequency is obtained from the number of

IGBT gates' pulses per second. It is interesting to note that the value is higher in healthy than in post-fault operation (see Fig. 13(a) and Fig. 13(b), respectively). This is an interesting benefit of the proposed DTC method that reduces the thermal stress in the operating IGBT devices during the faulty operation, where the obtained switching frequency remains nearly constant with applied load torques and does not vary as much as in healthy operation.

# V. CONCLUSIONS

The recent interest in multiphase drives from the research community is due to, among other reasons, their high faulttolerant capability. Field oriented control and predictive control schemes have been recently extended to the multiphase drive case, where their interests have been analyzed in healthy and open-phase faulty operation modes. DTC has been also proposed in recent times in five-phase induction motor drives during the normal operation of the system, but its utility managing the open-phase fault operation of the drive has not been stated yet. This paper extends the DTC technique to the open-phase fault operation of a symmetrical five-phase induction motor drive. Obtained experimental results analyze the performance of the proposed controller during the faulty operation of the drive, concluding that the speed, torque and flux references are maintained after the fault occurrence if the applied load torque is within the maximum torque that the postfault control scheme can manage.

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