



# A simple method for efficiency calibration of HPGe detectors in $\gamma$ -spectrometric measurements

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## Abstract

In this paper a simple, rapid and general method for  $\gamma$ -ray efficiency calibration of Ge detectors for environmental samples is presented. This method is based on the use of an active natural solid sample with several  $\gamma$ -emissions (in our case,  $^{226}\text{Ra}$ ) as the calibrating matrix for determining the full energy peak efficiency (FEPE)  $\varepsilon_c$  vs  $\gamma$ -emission energy  $E_\gamma$  and the sample height  $h$  in a counting cylindrical geometry. The  $^{226}\text{Ra}$  activity concentration is determined by  $\alpha$ -particle spectrometry, a method that has previously been validated. © 2001 Elsevier Science Ltd. All rights reserved.

*Keywords:* Gamma-spectrometry; Efficiency-calibration; Self-absorption; Sample-height

## 1. Introduction

In  $\gamma$ -measurements of solid samples using Ge detectors, it is interesting to obtain the full energy peak efficiency (FEPE) in the calibrating matrix  $\varepsilon_c$  curve as a function of the  $\gamma$ -emission energy  $E_\gamma$  and the sample height  $h$ , in the special case of a cylindrical geometry. The objective of this paper is to design a simple, rapid and general method to find the FEPE curve in the calibrating matrix as a function of  $E_\gamma$  and  $h$ . For this, the only requirement is an active solid calibrating matrix with several  $\gamma$ -emissions in the energy range of interest; in our case 150–1800 keV.

The FEPE in the calibration sample for a  $\gamma$  energy  $E_\gamma$  and height  $h$  is given by the expression  $\varepsilon_c = \varepsilon'/a$ , where  $\varepsilon' = N/(P_\gamma TM)$ ;  $a$  is the activity concentration of a specified radionuclide;  $P_\gamma$ , the probability of  $\gamma$ -emission;  $T$ , the counting time;  $M$ , the mass of the sample;  $N$ , the net counts under the full energy peak; and  $\varepsilon'$  (which we refer to as the “normalised efficiency”).

## 2. Present investigation

Obviously,  $\varepsilon'$  has the same functional relation on  $E_\gamma$  and  $h$  that  $\varepsilon$  has, since the activity concentration  $a$  is constant for every  $h$ , that is to say, the  $\gamma$ -emitter radionuclide is homogeneously distributed in the matrix. Our method consisted of finding the function  $\varepsilon' = f(E_\gamma, h)$  using a sample which contains a radionuclide with several  $\gamma$ -emissions in the energy interval of interest.

For the calibrating sample we used phosphate rock, containing mainly  $\text{Ca}_{10}(\text{PO}_4)_6\text{F}_2$  and having an apparent density of  $1.60 \text{ g cm}^{-3}$ . For this mineral we can suppose that  $^{226}\text{Ra}$ ,  $^{214}\text{Pb}$  and  $^{214}\text{Bi}$  are in secular equilibrium if the counting is done at least one month after filling and sealing of the sample container, the latter being a cylinder of 6.5 mm diameter and variable sample height. The content of  $^{226}\text{Ra}$  in the mineral was measured by  $\alpha$ -particle spectrometry using a method previously validated (Aguado et al., 1999), yielding an activity concentration  $a = 1152 \pm 54 \text{ Bq } ^{226}\text{Ra/kg}$ .  $\gamma$ -spectrometric measurements from 1 to 5.0 cm, in increments of 5 mm, were also done. A total of nine spectra were collected. The measurements were performed using a coaxial Ge detector XtRa model GX3518 (Canberra Industries, Meriden, USA), 38% relative efficiency and

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Table 1  
Uncertainties at a confidence level of  $1\sigma$ , due to countings statistics and fitting of parameters

| Radionuclide            | $^{152}\text{Eu}$ | $^{133}\text{Ba}$ | $^{60}\text{Co}$ | $^{137}\text{Cs}$ |
|-------------------------|-------------------|-------------------|------------------|-------------------|
| Certified (Bq/kg)       | $1338 \pm 36$     | $1053 \pm 51$     | $620 \pm 10$     | $2025 \pm 39$     |
| Our calibration (Bq/kg) | $1262 \pm 43$     | $988 \pm 49$      | $674 \pm 34$     | $1988 \pm 72$     |

shielded with 10 cm thick lead. For each energy, the best simple relation for  $\varepsilon'$  vs  $E_\gamma$  was an exponential function  $\varepsilon' = \varepsilon'_0 e^{bh}$ , where the parameters  $\varepsilon'_0$  and  $b$  depend on the energy. An empirical energy-dependency relation for these parameters ( $\varepsilon'_0$  and  $b$ ) was found. A reduced chi-square ( $\chi^2_R$ ) of around unity and a regression coefficients of higher than 0.99 were obtained for all fittings.

Including the parameter fittings in the previous equation, and noting that  $\varepsilon_c = \varepsilon'/a$ , we find

$$\varepsilon_c = 18.08 E_\gamma^{-0.972} \exp(-0.417 h E_\gamma^{-0.138}). \quad (1)$$

This expression relates the FEPE in the calibration sample with the  $\gamma$ -emission energy  $E_\gamma$  (keV) and its height  $h$  (in cm). This calibration was validated, including the necessary self-absorption corrections

(Bolívar et al., 1996), via a certified aqueous calibration standard containing  $^{152}\text{Eu}$ ,  $^{137}\text{Cs}$ ,  $^{133}\text{Ba}$  and  $^{60}\text{Co}$ . The results are shown in Table 1.

## References

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