ROM-Based Finite State Machine Implementation in Low Cost FPGAs

I. García-Vargas, R. Senhadji-Navarro, G. Jiménez-Moreno and A. Civit-Balcells

Departamento de Arquitectura y Tecnología de Computadores Universidad de Sevilla Sevilla, Spain Email: {ignacio,raouf,gaji,civit}@atc.us.es

Abstract—This work presents a technique for the resource optimization of input multiplexed ROM-based Finite State Machines. This technique exploits the *don't care* value of the inputs to reduce the memory size as well as multiplexer complexity. This technique has been applied to a publicly available FSM benchmarks and implemented in a low-cost FPGA. Results have been compared with tools supported ROM and standard logic cells implementations. In a significant number of test cases, the proposed technique is the best design alternative, both in resource requirements and speed.

I. INTRODUCTION

The concept of the Finite State Machine (FSM) is at the very centre of control and computing theories and provides an excellent abstraction framework for the definition of complex control-dominated automata. Depending on the application and system complexity, FSMs are implemented with microcontrollers, signal processors (DSP) or programmable logic. This work deals with the efficient implementation of FSMs on programmable logic making use of the embedded memory.

In the last decade Field Programmable Gate Array (FPGA) have evolved from a replacement of glue-logic to a serious competitor of complex application specific integrated circuits (ASIC). This has been possible through the mass production of submicrometer technologies, which have enabled the integration of thousands of elementary cells in a single device. Among the elements nowadays integrated in these devices, embedded synchronous memory blocks (RAM) have shown to be a significant breakthrough in many digital signal processing and networking applications. However, RAM blocks may also be used for other tasks, such as the implementation of sequential circuits. This fact has motivated a growing interest on the implementation of ROM-based Finite State Machines (FSM) [1,2,3,4,5]. In fact, the latest versions of Xilinx ISE Foundation include the option of limited mapping of sequential logic and FSMs into on-chip memory [6].

P. Guerra-Gutiérrez

Departamento de Ingeniería Electrónica Universidad Politécnica de Madrid Madrid, Spain Email: pguerra@die.upm.es

Whenever an FPGA is considered for the implementation of a complex FSM, circuit optimization must be addressed in order to cope with the limited number of available resources. The availability of new on-chip modules such as memories provides new alternatives to controller synthesis. FSM implementation with embedded ROM blocks provides some benefits compared to synthesis on logic cells. The maximum clock frequency of a FSM implemented in a ROM block is independent of its complexity. Moreover memory blocks provide control signals that allow for module deactivation when the FSM is inactive, providing an efficient mechanism for power saving. In any case, it has been proved that complex FSMs consume less power when implemented as memory blocks [4].

However, the ROM implementation of FSMs poses a significant problem: If no optimization is considered, memory size grows exponentially with the number of inputs and the number of state encoding bits. This is a critical aspect, as memory requirements may easily exceed the available on-chip RAM even with a simple FSM. In order to cope with memory size, additional resources are introduced to trade ROM size with logic [2,3,4,7].

Some of the previously referred techniques reduce the ROM address bitwidth by multiplexing FSM inputs. This approach is useful with those FSMs where the current state is only function of a subset of the inputs. Multiplexers select for each state only those inputs that are of relevance, thus reducing the number of addresses in the ROM. With this scheme, memory size is exchanged for multiplexers, modules that are efficiently implemented with modern FPGAs [8,9]. As an example, a 32:1 multiplexer takes only two Configurable Logic Blocks (CLB) of a Xilinx Spartan-3 [10]. Moreover, some FPGA families provide tristate buffers, allowing the implementation of wired multiplexers that take no additional logic [10,11].

This works presents a technique based on input multiplexing with the aim of reducing resource needs, not only in memory size but in the number of multiplexers as well. Unlike previous state-of-the-art techniques, which only reduce the number of inputs, the proposed approach exploits multiplexing to reduce both the number of inputs and the number of bits required to code the machine states. Additionally, in order to simplify multiplexer complexity, an optimization algorithm is applied to reduce the number of inputs of each multiplexer. As it is shown in the results section, this step will also have an impact on memory size, as multiplexer control bits of each state are also stored in the memory.

This paper is structured as follows, the second section details the proposed technique, whose results with MCNC benchmark [12] are analyzed in the third section. The work closes with conclusions and future work.

II. TECHNIQUE DESCRIPTION

The FSM is abstracted as a 5-tuple (*X*, *Y*, *S*, *f*, *g*) where *X*, *Y* and *S* are finite collections of the input, output and state variables; $f:X \times S \rightarrow S$ is the transition function that provides the next state s_i for the given inputs and the current state s_i and $g:X \times S \rightarrow Y$ is the output function that computes the machine output for the given inputs and current state.

FSMs are usually represented as State Transition Diagrams (STD). These diagrams are treated as directed graphs, where each vertex is a machine state and each arc (s_i, s_j) represents a transition between current state s_i and next state s_j . Additionally, each arc is labelled as 'x/y' with $s_j=f(x,s_i)$ and $y=g(x,s_i)$. These concepts are summarized in Fig. 1a, which shows a STD for a simple FSM.

The STD representation is a commonly used to summarize any FSM behaviour; however for a proper description of the proposed technique it is more convenient to represent the FSM in the form of a State Transition Table (STT). The STT, as shown in Fig. 1b, is table whose rows represent transitions which are expressed as the 4-tuple (*in*, *ps*, *ns*, *out*), which correspond to the inputs, present state, next state and output variables.

It is obvious that the STT highlights the ROM-ability of the FSM. Fig. 2 shows the reference architecture for the hardware synthesis, which may be seen as a direct implementation of the STT. Each word of the memory will store the outputs and the next state, while address is determined by the inputs and the current state, under this assumption the size of the required memory is:

$$2^{m+p} \mathbf{X} \left(n+p \right) \tag{1}$$

where m is the number of inputs, p the bitwidth of the coded state and n is the number of outputs. Equation (1) shows that the memory needs are exponential with the number of inputs and state codeword size. For this reason, if no additional measure is taken, even a simple FSM may easily take up an unacceptable amount of memory.

In those FSMs where the next state and output are function of a subset of the inputs, ROM size is reduced by the input multiplexing technique, whose reference architecture is shown



Fig. 1. FSM example: (a) STD, (b) STT, (c) ESTT, (d) ESTT representation after state encoding bit reduction.

in Fig. 3. The multiplexer bank selects for each state the subset of inputs that are of interest, thus reducing the number of signals that contribute to the memory address word.

Two alternative strategies are possible for the multiplexer control, either the state codeword is used (Fig. 3a) or additional control bits are stored in the memory (Fig. 3b). The first option



Fig. 2. ROM-based FSM implementation.



Fig. 3. FSM implementation with input multiplexing: (a) multiplexers controled by the state codeword, (b) control bits stored in ROM.

has the advantage of preserving memory size; however including new control bits in the memory may allow multiplexer complexity reduction and provide an overall FSM simplification. Therefore the proposed technique selects the second alternative. In this case, ROM size is given by the following expression:

$$2^{m'+p} \mathbf{X} \left(n+p+r \right) \tag{2}$$

where m' is maximum number of selected inputs, n is the number of outputs, p the state codeword bitwidth and r the number of bits devoted to multiplexer control. In the particular case where the multiplexer is controlled by the state code, r is equal to zero. The ability of the technique to reduce memory size is based on the fact that m' is equal or smaller than m. However, the actual value is determined by the state that is sensitive to the highest number of inputs. Therefore, such technique will yield bad results in FSMs where only a reduced fraction of states are sensitive to a high number of inputs. In the worst case, a single state which is sensitive to all inputs will prevent any ROM simplification.

The technique herein described solves this problem with a twofold approach: on one hand input multiplexing is used in order to reduce both the number of inputs (m) and the state bitwidth (p), on the other an optimization algorithm is applied in order to reduce the number of bits used in the multiplexer control (r). This way overall complexity of the FSM is minimized.

We will define those inputs which influence on a particular state as *state effective inputs* (SEI). The SEI number is different for each state, but the number of inputs selected by a multiplexer is fixed, therefore in each state the control multiplexer selects not only the SEI but also some inputs that have no influence on the current state, these inputs will be denominated as *don't care selected inputs* (DCSI). In order to reduce state codeword bitwidth, the proposed technique will partially use the DCSI for the state codification.

In order to properly represent the input multiplexed FSM (FSMIM), it is mandatory to extend the information stored in the STT. Each row of the Extended State Transition Table (ESTT) will store a 6-tuple (*in*, *pis*, *ps*, *nis*, *ns*, *out*), where the new items are the present (*pis*) and next (*nis*) input selection. For each state, *pis* stores information about the selected inputs and *in* contains the actual value of these inputs. The information about which subset of inputs will be selected for the next state *ns* is stored in *nis*. Unlike FSMs, whose states are only identified by the *ps* word, FSMIMs are identified by the 2-tuple (*ps*, *pis*). Fig. 1c shows the ESTT of the FSM corresponding to the STD in Fig. 1a. It is observed that the first two rows of the ESTT the input selection for state s_0 is "-a". That means that the first input is a DCSI and the second input is the *a* input of the original FSM.

It is said that two states share a DCSI if it selected by both states and with the same multiplexer. With this convention, two states sharing a DCSI may be coded setting the DCSI value to '0' in one state and '1' in the other. In formal notation, let A and B to be two states sharing at least one DCSI, with (PS_j, PIS_j) as the 2-tuple that univocally identifies state A and (PS_k, PIS_k) identifies the state B. Both states may be coded with the same PS if they differ in the PIS having a different code at the shared DCSI. Fig. 1d shows the states (s_{00} , -a) and (s_{22} , -c), which have been coded using the same code s_{02} for the state and considering a different value for the shared DCSI ("0" is chose for s_0 and "1" for s_2). The final states are (s_{02} , 0a) and (s_{02} , 1c).

Multiplexer complexity, and also the number of the required control bits, depends on the way inputs are assigned to each multiplexer. As an example, Fig. 4 shows two possible assignments related to the example FSM of Fig. 1. In order to find an optimum partitioning, it has been decided to assign each input to a single multiplexer. For example, in the Fig. 4a, where the input c is linked to two multiplexers, the resulting logic turns out to be more complex than Fig 4b. This is accomplished by guaranteeing that two inputs acting upon a given state do not share the same multiplexer (dependent inputs). In the Fig. 4b, inputs b and c are dependent inputs and are assigned to different multiplexer.

In this case, the optimization problem consists on maximizing the number of independent inputs for each multiplexer. This problem may be modelled as a Maximum Independent Set Problem (MISP) [13]. In case a solution is not found, constraints will be relaxed by allowing the assignment of dependent inputs to the same multiplexer.



Fig. 4. Example of multiplexer bank: (a) without simplification, (b) with simplification

III. EXPERIMENTAL RESULTS

The proposed technique has been applied to the MCNC benchmark [12]. On one hand, the technique ability to optimize ROM size and multiplexer bank complexity is shown. On the other, in order to assess the quality of the optimized implementation in terms of actual resource use and maximum clock frequency, several implementations with a commercially available FPGA have been carried out.

FSMs have been synthesized on a Xilinx Spartan-3 xc3s5000 with the device vendor's reference tool ISE Foundation 7.1i (Xilinx Inc. San Jose, CA, USA). Implementation results obtained with the FSMIM have been compared against alternative FSM implementations where either (a) ROM synthesis without optimization, (b) a standard implementation on logic cells or (c) tool supported ROM synthesis are considered. The four alternative implementations will be referred as FSMIM, ROM, ISE-LUT and ISE-RAM respectively.

The optimization process consists of two steps. The first step is the Multiplexer Bank Complexity Simplification (MBCS) and the second is the State Encoding Bit Reduction (SEBR). Table I shows the results after both steps, where ROM size is compared to the case where optimization is performed and finally the overall reduction factor is summarized.

These results show that the use of a non-complex multiplexer bank provides a significant theoretical memory reduction (87% on average). The highest memory reductions are achieved for the s510, s820, s832 y scf FSM. For the considered benchmark, only 19% of the FSMs require multiplexers with more than 4 inputs.

In order to evaluate the usefulness of the SEBR step, results are also compared against input multiplexing alone. Fig. 5 shows the ROM size reduction after the MBCS and the SEBR steps. Dark gray bars show memory reduction after the MBCS step, while light gray bars reflect the additionaly size improvement provided by the SEBR step. It is observed that, although multiplexing provides a significant improvement, the SEBR yields an additional 67% average reduction that in half the cases is as high as 70%.

TABLE I OPTIMIZATION RESULTS

FSM		FSMIM				
Name	ROM	F	OM	MUX Bank		
	Size	Size	Reduction			
	(Kbits)	(Kbits)	(%)	(Input Number)		
bbsse	22.00	3.75	83.0	4,2		
cse	22.00	7.50	65.9	2,2,2		
ex1	384.00	16.50	95.7	2,4,4,2,2,2		
ex4	13.00	1.00	92.3	4,2		
keyb	28.00	9.00	67.9	2,2		
mark1	10.00	1.50	85.0	4,2,2		
opus	5.00	0.94	81.3	2,2,2,2		
planet	200.00	8.00	96.0	2,2,2,4,4		
pma	104.00	11.00	89.4	4,2,2,2,2		
s1	88.00	18.00	79.5	2,2,2,2,2		
s1488	400.00	15.00	96.3	4,4,2,2		
s1494	400.00	15.00	96.3	4,4,2,2		
s27	0.50	0.31	37.5	2		
s386	22.00	3.50	84.1	3,2		
s510	425984.00	2.38	≈100	14,7		
s820	196608.00	38.00	≈100	7,6,4,4,2,2,2		
s832	196608.00	66.00	≈100	5,6,4,4		
sand	896.00	13.00	98.5	4,4,4,4,2,4,2		
scf	$\approx 10^9$	156.00	≈100	13,3,4,4,2,2,2,2		
sse	22.00	3.75	83.0	4,2		
styr	240.00	21.00	91.3	4,4,2,2		

In four cases (*keyb*, *opus*, *s21* and *s27*) the SEBR step has a dramatic impact on memory reduction. It is important to highlight that in the particular case of the *keyb*, *opus*, *s21* and *s27* test FSMs, the MBCS by itself yielded no memory reduction and it is only due to the SEBR.

Table II shows the average resource requirements of different implementations. The FSMIM technique requires an average of 1.76 BRAMs, the ISE_BRAM 16.31 and the ROM technique 13.06. Thanks to the reductions provided by the proposed technique, the number of benchmark FSMs that can be synthesized into the smallest member of the Xilinx Spartan-



Fig. 5: Impact of each optimization step on the final design

RESOURCE USE SUMMARY										
FSM	ISE-LUT	ISE-BRAM		ROM	FSMIM					
	LUT	LUT	BRAM	BRAM	LUT	BRAM				
bbsse	53	33	3	2	3	1				
cse	140	79	3	2	3	1				
ex1	296	213	25	35	6	2				
ex4	38	29	2	1	3	1				
keyb	85	45	6	2	3	1				
mark1	45	28	1	1	3	1				
opus	19	0	1	1	2	1				
planet	370	363	35	13	5	1				
pma	167	120	15	7	3	1				
s1	103	0	6	6	5	2				
s1488	639	601	68	38	5	1				
s1494	665	576	54	38	5	1				
s27	11	1	1	1	2	1				
s386	63	37	3	2	3	1				
s510	118			1	12	1				
s820	197			-	9	5				
s832	187				8	5				
sand	515			56	7	2				
scf	466				19	5				
sse	53	33	3	2	3	1				
styr	395	317	35	15	4	2				

TABLE II



bbsse ex keyt

Fig. 6. Maximum Operation Frequency

3 family (with 4 BRAMs) is doubled (86% in FSMIM vs. 43% in the best case of other ROM-based implementations). This significant improvement is at the cost of small number of lookup tables (LUT). The average number of LUTs of the FSMIM implementation is as low as 5, while up to 220 LUTs are required in a standard logic synthesis of the FSM (ISE-LUT).

In tests *sl488* and *sl494*, BRAM reduction is higher than 97% with the extra cost of only 5 LUT. Some of the FSMs in the testbench (s510, s820, s832 and scf) could not be implemented into the FPGA with ISE-BRAM and ROM implementation, due to the high memory requirements, despite the fact that the selected model is the biggest of the family with 104 RAM blocks. In four cases (ex4, mark1, opus and s27) the traditional approach only requires a single RAM block and therefore there is no apparent benefit in using the proposed technique and this situation may be common due to the relatively high size of the individual RAM block (18Kb). However, as the on-chip RAMs are double-port memories, it is feasible to implement two FSMs in the same block, making use of the second address/data ports to access the available space [5] and in this case there is still motivation to reduce memory size.

Fig. 6 shows the FSM maximum operating clock frequency after placement and routing with the different techniques under consideration. In 81% of the test cases, the FSMIM frequency is higher that the LUT-based implementation, being the improvement higher than 57% in a fourth of the test cases. These results show that the FSMIM is a valid alternative to standard cell based FSM implementation.

Compared to the BRAM approaches, the FSMIM allows for higher operating frequency in 59% of the considered scenarios in the ROM case and 81% in the ISE-BRAM case. This is mostly due to the distribution of the RAM blocks within the device. Overall, the FSMIM approach provides better results both in area and frequency in 29% of the test cases.

IV. CONCLUSION AND FUTURE WORK

This work has presented a technique that achieves a significant reduction in the number of required on-chip memory blocks for the implementation of a FSM in an FPGA. making use of a reduced number of extra logic resources, such as look-up tables. This block reduction has a positive impact on the maximum clock frequency of the FSM.

The proposed technique has been compared against other alternatives, making used of a standard FSM benchmark. Results show that in a significant number of test cases the proposed technique is the best design alternative, both in resource requirements and speed, even when comparing against traditional cell based FSM implementations.

The proposed implementation is not limited to low cost FPGAs, but can be used by any FPGA device that includes RAM blocks. As future work, it seems interesting to study the performance of the technique with the latest Xilinx architecture based on 6-input LUTs (Virtex-5) that allows for a more efficient multiplexor implementation.

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