

# ETHOM: An Evolutionary Algorithm for Optimized Feature Models Generation

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A *feature model* defines the valid combinations of features in a domain. The automated extraction of information from feature models is a thriving topic involving numerous analysis operations, techniques and tools. The progress of this discipline is leading to an increasing concern to test and compare the performance of analysis solutions using tough input models that show the behaviour of the tools in extreme situations (e.g. those producing longest execution times or highest memory consumption). Currently, these feature models are generated randomly ignoring the internal aspects of the tools under tests. As a result, these only provide a rough idea of the behaviour of the tools with average problems and are not sufficient to reveal their real strengths and weaknesses.

In this technical report, we model the problem of finding computationally-hard feature models as an optimization problem and we solve it using a novel evolutionary algorithm. Given a tool and an analysis operation, our algorithm generates input models of a predefined size maximizing aspects as the execution time or the memory consumption of the tool when performing the operation over the model. This allows users and developers to know the behaviour of tools in pessimistic cases providing a better idea of their real power. Experiments using our evolutionary algorithm on a number of analysis operations and tools have successfully identified input models causing much longer executions times and higher memory consumption than random models of identical or even larger size. Our solution is generic and applicable to a variety of optimization problems on feature models, not only those involving analysis operations. In view of the positive results, we expect this work to be the seed for a new wave of research contributions exploiting the benefit of evolutionary programming in the field of feature modelling.

## 1. Introduction

*Software Product Line* (SPL) engineering is a systematic reuse strategy to develop families of related software systems [16]. The emphasis is on deriving products from a common set of reusable assets reducing production costs and time-to-market. The products of an SPL are defined in terms of features where a *feature* is any increment in product functionality [5]. A key aspect in SPLs is to capture the commonalities (i.e. common features) and variabilities (i.e. variant features) of the systems that belong to the product line. This is commonly done by using a so-called feature model. A *feature model* [26] is a compact representation of all the products of a SPL in terms of features and relationships among them (see example in Fig. 1).

The automated extraction of information from feature models (a.k.a automated analysis of feature models) is a thriving topic that has caught the attention of researchers for the last twenty years [10]. Typical operations of analysis allow us to know whether a feature model is void (i.e. it represents no products), what is the number of products represented by a feature model or whether a model contains any errors. Catalogues with up to 30 analysis operations on feature models identified in the literature have been reported

[10]. Common techniques to perform these operations are those based on propositional logic [5, 39], constraint programming [8, 66] or description logic [61]. Also, these analysis capabilities can be found in several commercial and open source tools including *AHEAD Tool Suite* [3], *Big Lever Software Gears* [15], *FaMa Framework* [17], *Feature Model Plug-in* [18], *pure::variants* [45] and *SPLOT* [37].

Recent publications reflect an increasing interest to evaluate and compare the performance of analysis techniques and tools on the analyses of feature models [19, 22, 39, 64, 65, 42, 44, 50, 52, 57, 67]. One of the main challenges when performing experiments is finding tough problems that shows the strengths and weaknesses of the tools under evaluation in extreme situations (e.g. those producing longest execution times). Feature models from real domains are by far the most appealing input problems. Unfortunately, although there are references to real feature models with hundreds or even thousands of features [6, 33, 56], only trivial examples from research publications or case studies are available. This lack of hard realistic feature models, has led authors to evaluate their tools with large-scale randomly generated feature models of 5,000 [40, 66], 10,000 [22, 39, 57, 64] and up to 20,000 [42] features. More recently, some authors have suggested looking for hard and realistic feature models in the open source community [13, 19, 52, 53]. For instance, She et al. [52] extract a feature model from the Linux kernel containing more than 5,000 features.

The problem of finding motivating input values to evaluate the performance of software systems has been largely studied in the field of software testing. In this context, researchers realized long ago of the ineffectiveness of using random values to reveal the vulnerabilities of the systems under tests. As pointed out by McMinn [36]: “*random methods are unreliable and unlikely to exercise ‘deeper’ features of software that are not exercised by mere chance*”. In this context, metaheuristic search techniques have proved to be a promising solution for the automated generation of test data for both functional [36] and non-functional properties [2]. *Metaheuristic search techniques* are frameworks which use heuristics to find solutions to hard problems at an affordable computational cost. Typical metaheuristic techniques are evolutionary algorithms, hill climbing or simulated annealing [60]. For the generation of test data, these strategies translate the test criterion into an objective function (also called fitness function) that is used to evaluate and compare the candidate solutions with respect to the overall search goal. Using this information, the search is guided toward promising areas of the search space. Wegener et al. [62, 63] were one of the first proposing using evolutionary algorithms to verify the time constraints of software back in 1996. In their work, the authors used genetic algorithms to find input combinations that violate the time constraints of real-time systems, that is, those inputs producing an output too early or too late. Their experimental results showed that evolutionary algorithms are much more effective than random search in finding input combinations maximizing or minimizing execution times. Since then, a number of authors have followed their steps using metaheuristics and especially evolutionary algorithms for the testing of non-functional properties such as execution time, quality of service, security, usability or safety [2, 36].

**Problem description.** Current performance evaluations on the analysis of feature model are mainly carried out using random feature models. However, these only provide a rough idea of the average performance of tools and do not reveal the specific weak points related to the type of technique or algorithm under evaluation. Thus, the

SPL community lacks specific mechanisms to generate computationally-hard feature models that take analysis tools to their limits and reveal their real potential. This problem has negative implications for both tools' users and developers. On the one hand, tool developers have no means of performing exhaustive evaluations of the strengths and weaknesses of their tools making it hard to find faults affecting their performance. On the other hand, users are not provided with full information about the performance of tools in pessimistic cases hindering them from choosing the tool that better meets their needs. Hence, for instance, a user could choose a tool based on its average performance and later realize that it performs very badly in particular cases that appear frequently in its application domain.

The problem of generating hard feature model has been traditionally addressed by the community by simply generating huge feature models with thousand of features and constraints. That is, it is generally assumed that the larger the model the harder its analysis. However, we remark that these models are still random and therefore, as warned by software testing experts, they are not sufficient to exercise the specific features of the tools under evaluation. Another negative consequence of using huge feature models to evaluate the performance of tools is that they frequently fall out of the scope of their users. Hence, both developers and users would probably be more interested to know whether their tool may crash with a hard model of small or medium size rather than knowing the execution times of huge random models out of their scope.

Finally, we may mention that using realistic or standard collection of problems (i.e. benchmarks) is equally not sufficient for a rigorous performance evaluation since they do not consider the internal aspects of the tools or techniques under tests. Thus, feature models that are hard to analyse by one tool could be trivially processed by other and vice versa.

**Solution overview and contributions.** In this article, we propose using evolutionary algorithms for the automated generation of hard feature models. In particular, we propose to model the problem of finding computationally-hard feature models as an optimization problem and we solve it using a novel *Evolutionary algorithm for Optimized feature Models (ETHOM)*. Given a tool and an analysis operation, ETHOM generates input models of a predefined size maximizing aspects such as the executions time or the memory consumed by the tool when performing the operation over the model. For the evaluation of our approach, we performed several experiments using different analysis operations, paradigms, tools and optimization criteria. In particular, we used FaMa and SPLOT, two tools for the automated analysis of feature models developed and maintained by independent laboratories. In total, we performed over 50 million executions of analysis operations for the configuration and evaluation of our algorithm. The results showed how ETHOM successfully identified input models causing much longer executions times and higher memory consumption than random models of identical or even larger size. As an example, we compared the effectiveness of random and evolutionary search in generating feature models with up to 1,000 features maximizing the time required by a constraint programming solver (a.k.a. CSP solver) to check their consistency. The results revealed that the hardest random model found required 0.2 seconds to be analyzed meanwhile ETHOM was able to find several models taking between 1 and 27.5 minutes to be processed. Not only that, we found the hardest feature models generated by ETHOM in the ranges 500-1,000 features were remarkably harder to

process than random models with 10,000 features. More importantly, we found that the hard feature models generated by ETHOM had similar properties to the realistic models found in the literature. This suggests that the long execution times and high memory consumption detected by ETHOM could be therefore reproduced when using real models with the consequent negative effect in the user.

Our work enhances and complements the current state of the art of performance evaluation of feature model analysis tools as follows:

- Our approach is the first one using a search-based strategy to exploit the internal weaknesses of the analysis tools and techniques under evaluation rather than trying to detect them by chance using random models.
- Our work allows developers to focus on the search of computationally-hard models of realistic size that could reveal deficiencies in their tools rather than using huge feature models out of their scope.
- Our approach provides users with helpful information about the behaviour of tools in pessimistic cases helping them to choose the tool that better meets their needs.
- Our algorithm is highly generic being applicable to any automated operation on feature models in which the quality (i.e. fitness) of the models with respect to an optimization criteria can be measured quantitatively.
- Our experimental results show that the hardness of feature models depends on different factors in contrast to related works in which the complexity of the models is mainly associated to their size. Although this is generally true, our work demystifies the belief that large models have to be necessarily harder to process than small ones.
- Our algorithm is ready-to-use and publicly available as a part of the open-source BeTTY Framework [14].

The rest of the article is structured as follows: Section 2 introduces feature models and evolutionary algorithms. In Section 3.1, we present ETHOM, an evolutionary algorithm for the generation of optimized feature models. Then, in Section 3.2, we propose a specific configuration of ETHOM to automate the generation of computationally-hard feature models. The empirical evaluation of our approach is presented in Section 4. Section 5 presents the threats to validity of our work. The related works are presented and discussed in Section 6. Finally, we summarize our conclusions and describe our future work in Section 7.

## 2. Preliminaries

### 2.1. Feature models

A *feature model* defines the valid combination of features in a domain. These are commonly used as a compact representation of all the products of an SPL in terms of features. A feature model is visually represented as a tree-like structure in which nodes

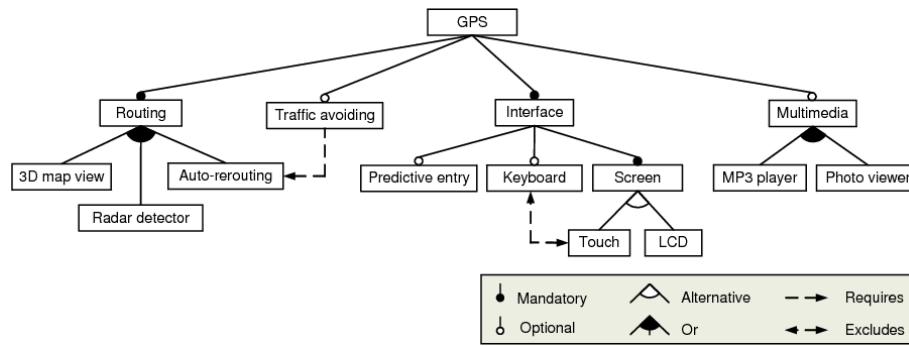


Figure 1: A sample feature model

represent features and connections illustrate the relationships between them. These relationships constrain the way in which features can be combined. Fig. 1 depicts a simplified sample feature model. The model illustrates how features are used to specify and build software for Global Position System (GPS) devices. The software loaded in the GPS is determined by the features that it supports. The root feature (i.e. ‘GPS’) identifies the SPL.

Feature models were first introduced in 1990 as a part of the FODA (Feature–Oriented Domain Analysis) method [26]. Since then, feature modelling has been widely adopted by the software product line community and a number of extensions have been proposed in attempts to improve properties such as succinctness and naturalness [46]. Nevertheless, there seems to be a consensus that at a minimum feature models should be able to represent the following relationships among features:

- **Mandatory.** If a child feature is mandatory, it is included in all products in which its parent feature appears. In Fig. 1, all GPS devices must provide support for *Routing*.
- **Optional.** If a child feature is defined as optional, it can be optionally included in products in which its parent feature appears. For instance, the sample model defines *Auto-rerouting* as an optional feature.
- **Alternative.** A set of child features are defined as alternative if only one feature can be selected when its parent feature is part of the product. In our SPL, software for GPS devices must provide support for either a *LCD* or *Touch* screen but only one of them in the same product.
- **Or-Relation.** A set of child features are said to have an or-relation with their parent when one or more of them can be included in the products in which its parent feature appears. In our example, GPS devices can provide support for a *MP3 player*, a *Photo viewer* or both of them.

Notice that a child feature can only appear in a product if its parent feature does. The root feature is a part of all the products within the SPL. In addition to the parental relationships between features, a feature model can also contain *cross-tree constraints* between features. These are typically of the form:

- **Requires.** If a feature A requires a feature B, the inclusion of A in a product implies the inclusion of B in such product. GPS devices with *Traffic avoiding* requires *Auto-rerouting*.
- **Excludes.** If a feature A excludes a feature B, both features cannot be part of the same product. In our sample SPL, GPS with *Touch* screen cannot include a *Keyboard* and vice-versa.

## 2.2. Evolutionary algorithms

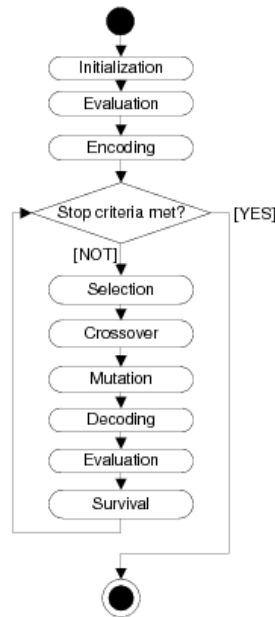
Principles of biological evolution have inspired the development of a whole branch of optimization techniques called *Evolutionary Algorithms (EAs)*. These algorithms manage a set of candidate solutions to an optimization problem that are combined and modified iteratively to obtain better solutions. Each candidate solution is referred to as *individual* or *chromosome* in analogy to the evolution of species in biological genetics where DNA of individuals is combined and modified along generations enhancing species through natural selection. Two of the main properties of EAs are that they are heuristic and stochastic. The former means that there is no guarantee of obtaining the global optimum for the optimization problem. The latter means that different executions of the algorithm with the same input parameters can produce different output, i.e. they are not deterministic. Despite this, EAs are among the most widely used optimization techniques being applied successfully in nearly all scientific and engineering areas by thousands of practitioners [4, Section D]. This success is due to the ability of EAs to obtain near optimal solutions to extremely hard optimization problems with affordable time and resources.

As an example, let us consider the design of a car as an optimization problem. A similar example was used to illustrate the working of EAs in [63]. Let us consider that our goal is to find a car design that maximize speed. This problem is hard since a car is a highly complex system in which speed depends on a number of parameters such as engine type, components as well as shape and body elements. Moreover, this problem is likely to have extra constraints like keeping the cost of the car under a certain value, making some designs infeasible. All EA variants are based on a common working scheme shown in Fig. 2. Next, we detail its main steps relating them to our example.

**Initialization.** The initial population (i.e. set of candidate solutions to the problem) is usually generated randomly. In our example, this could be done by choosing a set of random values for the design parameters of the car. Of course, the chances of finding optimal or near optimal car designs in this initial population are very small. However, promising values found at this step will be used to produce variants along the optimization process leading to better designs.

**Evaluation.** Next, individuals are evaluated using a fitness function. A *fitness function* is a function that receives an individual as input and returns a numerical value indicating its optimality for the problem. This enables the objective comparison of candidate solutions with respect to an optimization problem. The fitness function should be deterministic to avoid interferences in the algorithm, i.e. different calls to the function with





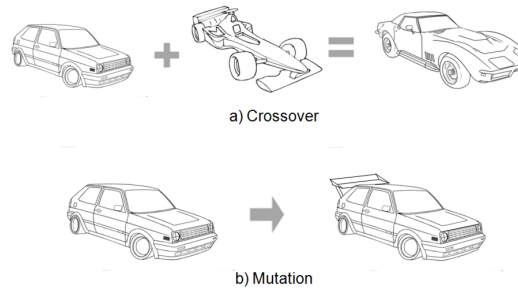
**Figure 2:** UML activity diagram of evolutionary algorithms

the same set of inputs parameters should produce the same output. In our car example, a simulator could be used to provide the maximum speed prediction as fitness.

**Stop criteria.** Iterations on the remainder of the algorithm are performed until a termination criterion is met. Typical stop criteria are: reaching a maximum or average fitness value, maximum execution times of the fitness function, number of iterations of the loop (so-called generations) or number of iterations without improvements on the best individual found.

**Encoding.** In order to create offspring, individuals need to be *encoded* expressing its characteristics in a form that facilitates its manipulation during the rest of the algorithm. In biological genetics, DNA encodes individual’s characteristics on chromosomes that are used on reproduction and whose modifications produce mutants. For instance, classical encoding mechanisms on EAs are binary vectors encoding numerical values in genetic algorithms (so-called binary encoding) [4, Sec. C1.2] and tree structures encoding abstract syntax of programs in genetic programming (so-called tree encoding) [31]. In our car example, this step would imply to express design parameters of cars using some kind of data structure, e.g. binary vectors for each design parameter.

**Selection.** In the main loop of the algorithm (see Fig. 2), individuals are selected from current population in order to create new offspring. In this process, better individuals usually have more probability of being selected resembling the natural evolution where stronger individuals have more chances of reproduction. For instance, two classic selection mechanisms are roulette wheel and tournament selection [21]. When using the former, the probability of choosing an individual is proportional to its fitness determining the width of the slice of a hypothetic spinning roulette wheel. This mechanism is often modified assigning probability based on the position of the individuals in a



**Figure 3:** Sample crossover and mutation in the search of an optimal car design.

fitness-ordered ranking (so-called rank-based roulette wheel). When using tournament selection, a group of  $n$  individuals is randomly chosen from the population and a winning individual is selected according to its fitness.

**Crossover.** These are the techniques used to combine individuals and produce new individuals in an analogous way to biological reproduction. Crossover mechanisms depend on the encoding scheme used but standard mechanisms are present in literature for widely used encodings [4, Sec. C3.3]. For instance, two classical crossover mechanisms for binary encoding are one-point crossover [24] and uniform crossover [1]. When using the former, a random location in the vector is chosen as break point and portions of vectors after the break point are exchanged to produce offspring (see Fig. 5 for a graphical example of this crossover mechanism). When using uniform crossover, the value of each vector element is taken from one parent or other with a certain probability, usually 50%. Fig. 3(a) shows a high-level application of crossover in our example of car design. An F1 car and an small family car are combined by crossover producing a sports car. The new vehicle has some design parameters inherited directly of each parent such as number of seats or engine type and others mixed such as shape and intermediate size.

**Mutation.** At this step, random changes are applied to the individuals. Changes are performed with certain probability where small modifications are more likely than larger ones. This step is crucial to prevent the algorithm from getting stuck prematurely at a locally optimal solution. An example of mutation in our car optimization problem is presented in Fig. 3(b). The shape of a family car is changed by adding a back spoiler while the rest of its design parameters remain intact.

**Decoding.** In order to evaluate the fitness of new and modified individuals *decoding* is performed. For instance, in our car design example, data stored on data structures is transformed into a suitable car design that our fitness function can evaluate. It often happens that the changes performed in the crossover and mutation steps create individuals that are not valid designs or break a constraint, this is usually referred to as an *infeasible individual* [4], e.g. a car with three wheels. Once an infeasible individual is detected, this can be either replaced by an extra correct one or it can be repaired, i.e. slightly changed to make it feasible.

**Survival.** Finally, individuals are evaluated and the next population is conformed in which individuals with better fitness values are more likely to remain in the population.

This process simulates the natural selection of the better adapted individuals that survive and generate offspring improving species.

In order to better clarify the operation of EAs, in algorithm 1 we provide a pseudocode that complements the common working scheme shown in Fig. 2.

---

**Algorithm 1** Evolutionary Algorithm pseudocode
 

---

```

bestEval ←  $-\infty$ 
Population ← initialPopulation() {Initialization of Population}
for all individual ∈ Population do
    nextEval ← f(decode(individual))
    if nextEval < bestEval then
        bestSolution ← individual
        bestEval ← nextEval
    end if
end for
repeat
    {Main loop}
    Parents ← crossoverSelection(Population)
    {Select Individuals for Crossover}
    Offspring ← crossover(Parents) {Crossover}
    Population ← mutation(Population) {Mutation}
    for all individual ∈ (Population ∪ Offspring) do
    {Evaluation of new population and Offspring}
    nextEval ← f(decode(individual))
    if nextEval < bestEval then
        bestSolution ← decode(individual)
        bestEval ← nextEval
    end if
    end for
    {Selection of survival individuals (Next population)}
    Population ← survivalSelection(Population ∪ Offspring)
until Termination Criteria is satisfied
return bestSolution
    
```

---

The first nine lines of the algorithm correspond to the initialization, where the individuals of the population are generated randomly based on the function *initialPopulation*. The loop in this section searches for the best individual present in this initial population and stores it in the variable *bestSolution*. Next, the main loop of the algorithm executes the main elements of the evolutionary algorithm: crossover, mutation and selection for survival. Along the iterative execution of this loop, the best individual found is maintained and stored in the variable *bestSolution*, that is returned as a result of the algorithm.

### 3. Automated generation of hard feature models

In this section, we present the core of our contribution. First, we introduce a novel evolutionary algorithm to deal with optimization problems on feature models. Then, we present a specific instantiation of the algorithm to search for computationally-hard feature models.

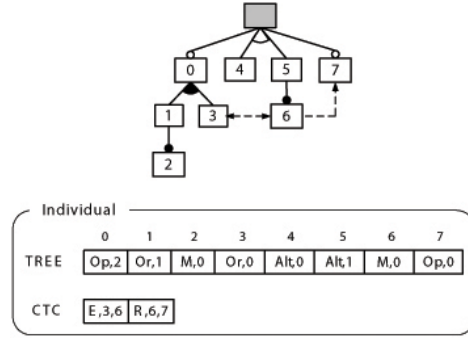
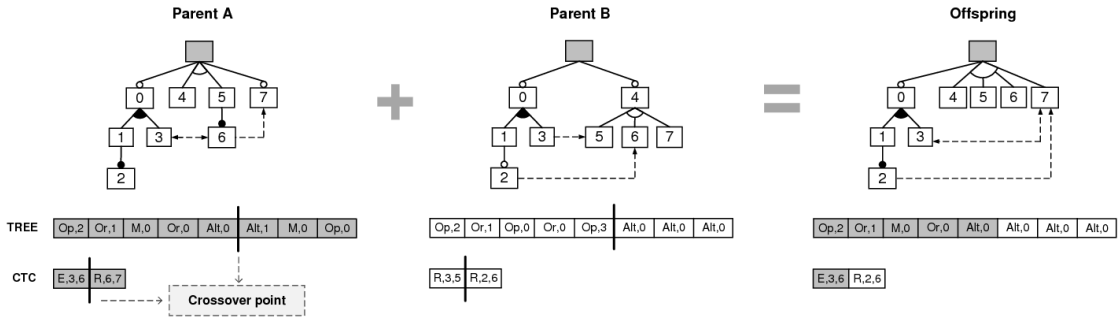
#### 3.1. An evolutionary algorithm for feature models

In this section, we present ETHOM, a novel evolutionary algorithm for the generation of optimized feature models. The algorithm takes several size constraints and a fitness function as input and returns a feature model of the given size maximizing the optimization criteria defined by the function. Key benefit of our algorithm is that it is very generic being applicable to any automated operation on feature models in which the quality (i.e. fitness) of the models can be measured quantitatively. In the following, we describe the basic steps of ETHOM as shown in Fig. 2.

**Initial population.** The initial population is generated randomly according to the size constraints received as input. The current version of ETHOM allows the user to specify the number of features, percentage of cross-tree constraints and maximum branching factor of the feature model to be generated. Several algorithms for the random generation of feature models have been proposed in the literature [47, 57, 67]. There are also tools supporting the random generation of feature models such as BeTTy [14] or SPLOT [37, 55]

**Evaluation.** Feature models are evaluated according to the fitness function received as input obtaining a numeric value that represents the quality of the candidate solution (i.e. its fitness).

**Encoding.** For the representation of feature models as individuals (a.k.a. chromosomes) we propose using a custom encoding. Generic encodings for evolutionary algorithms were ruled out since these were either not adequate to represent tree structures (i.e. binary encoding) or were not able to produce solutions of a fixed size (e.g. tree encoding), a key requirement in our approach. Fig. 4 depicts an example of our encoding. As illustrated, each model is represented by means of two arrays, one storing information about the tree and another one with information about *Cross-Tree Constraints (CTC)*. The order of each feature in the array corresponds to the *Depth-First Traversal (DFT)* order of the tree. Hence, feature labelled with '0' in the tree is stored in the first position of the array, feature labelled with '1' is stored the second position and so on. Each feature in the tree array is defined as a two-tuple  $\langle PR, C \rangle$  where  $PR$  is the type of relationship with its parent feature (M: Mandatory, Op: Optional, Or: Or-relationship, Alt: Alternative) and  $C$  is the number of children of the given feature. As an example, first position in the tree array,  $\langle Op, 2 \rangle$ , indicates that feature labelled with '0' in the tree has an optional relationship with its parent feature and has two child features (those labelled with '1' and '3'). Analogously, each position in the CTC array stores information about one constraint in the form  $\langle TC, O, D \rangle$  where  $TC$  is the type of constraint


**Figure 4:** Encoding of a feature model in ETHOM

**Figure 5:** Example of one-point crossover in ETHOM

(R: Requires, E: Excludes) and  $O$  and  $D$  are the indexes of the origin and destination features in the tree array respectively.

**Selection.** Selection strategies are generic and can be applied regardless of how the individuals are represented. In our algorithm, we implemented both rank-based roulette-wheel and binary tournament selection strategies. The selection of one or the other mainly depends on the application domain.

**Crossover.** We provided our algorithm with two different crossover techniques, one-point and uniform crossover. Fig. 5 depicts an example of the application of one-point crossover in ETHOM. The process starts by selecting two parent chromosomes to be combined. For each array in the chromosomes, the tree and CTC arrays, a random point is chosen (so-called crossover point). Finally, the offspring is created by copying the content of the arrays from the beginning to the crossover point from one parent and the rest from the other one. Notice that the characteristics of our encoding guarantee a fixed size for the individuals.

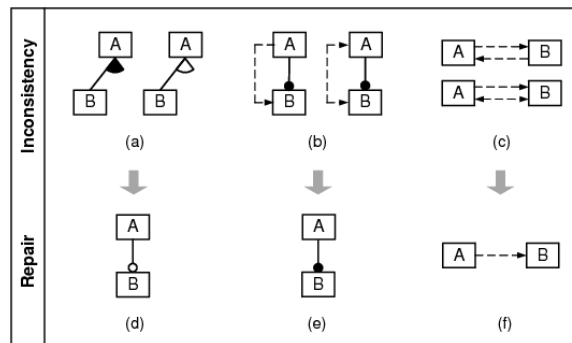
**Mutation.** Mutation operators must be specifically designed for the type of encoding used. ETHOM uses four different types of custom mutation operators, namely:

- *Operator 1.* It changes randomly the type of a relationship in the tree array, e.g. from mandatory,  $\langle \mathbf{M}, 3 \rangle$ , to optional,  $\langle \mathbf{Op}, 3 \rangle$ .
- *Operator 2.* It changes randomly the number of children of a feature in the tree, e.g. from  $\langle M, \mathbf{3} \rangle$  to  $\langle M, \mathbf{5} \rangle$ . The new number of children is in the range  $[0, BF]$  where  $BF$  is the maximum branching factor indicated as input.

- *Operator 3*. It changes the type of a cross-tree constraint in the CTC array, e.g. from excludes  $\langle \mathbf{E}, 3, 6 \rangle$  to requires  $\langle \mathbf{R}, 3, 6 \rangle$ .
- *Operator 4*. It changes randomly (with equal probability) the origin or destination feature of a constraint in the CTC array, e.g. from  $\langle E, \mathbf{3}, 6 \rangle$  to  $\langle E, \mathbf{1}, 6 \rangle$ . Origin and destination features are ensured to be different.

These operators are applied randomly with the same probability.

**Decoding.** At this stage, the array-based chromosomes are translated back into feature models in order to be evaluated. In ETHOM, we identified three types of patterns making a chromosome infeasible or semantically redundant, namely: *i*) those encoding set relationships (or- and alternative) with a single child feature (e.g. Fig. 6(a)), *ii*) those containing cross-tree constraints between features with parental relationship (e.g. Fig. 6(b)), and *iii*) those containing features sharing contradictory or redundant cross-tree constraints (e.g. Fig. 6(c)). The specific approach used to address infeasible individuals, replacing or repairing (see Section 2.2 for details), mainly depend on the problem and it is ultimately up to the user. In our work, we used a repairing strategy described in the next section.



**Figure 6:** Examples of infeasible individuals and repairs

**Survival.** Finally, the next population is created by including all the new offspring plus those individuals from the previous generation that were selected for crossover but did not generate descendants due to probability.

## 3.2. Instantiation of the algorithm

In this section, we propose to model the problem of finding computationally-hard feature models as an optimization problem and to solve it using an instantiation of our evolutionary algorithm. We chose evolutionary computation because it has proved to be a robust search technique suited for the complex search spaces and noisy objective functions used when dealing with non-functional properties [2]. Key benefit of our approach is that it takes into account the characteristics of the tools under test trying to exploit its vulnerabilities. Also, our approach is very generic being applicable to any automated

operation on feature models, not only analyses, in which the quality (i.e. fitness) of the models can be measured quantitatively.

In order to find a suitable configuration of our algorithm, we performed numerous executions of a sample optimization problem evaluating different combination of values for the key parameters of the algorithm, presented in Table 1. The optimization problem was to find a feature model maximizing the execution time invested by the analysis tool when checking the model consistency (i.e. whether it represents at least one product). We chose this analysis operation because it is currently the most quoted in the literature [10]. In particular, we looked for feature models of different size maximizing execution time in the CSP solver JaCoP integrated into the FaMa framework v1.0. FaMa is a widely-used tool of significant size, highly tested [48] and integrated into tools like MOSKitt [41]. These reasons, coupled to our familiarity with the tool as leaders of the project, made us choose FaMa as a good tool to be use in our work. Next, we clarify the main aspects of the configuration of our algorithm:

- **Fitness function.** Our first attempt was to measure the execution time in milliseconds invested by FaMa to perform the operation. However, we found that this was very inaccurate since the result of the function was deeply affected by the system load, i.e. it was not deterministic. To solve this problem, we decided to measure the fitness of a feature model as the number of backtracks produced by the analysis tool during its analysis. A *backtrack* represents a partial candidate solution to a problem that is discarded because it cannot be extended to a full valid solution [58]. In contrast to the execution time, most CSP backtracking heuristics are deterministic. Together with execution time, the number of backtracks is commonly used to measure the complexity of constraint satisfaction problems [58]. Thus, we may assume that the higher the number of backtracks the longer the computation time.
- **Infeasible individuals.** We evaluated the effectiveness of both replacement and repairing techniques. More specifically, we evaluated the following repairing algorithm with infeasible individuals: *i*) isolated set relationships are converted into optional relationships (e.g. the model in Fig. 6(a) is changed as in Fig. 6(d)), *ii*) cross-tree constraints between features with parental relationships are removed (e.g. the model in Fig. 6(b) is changed as in Fig. 6(e)), and *iii*) two features cannot share more than one constraint (e.g. the model in Fig. 6(c) is changed as in Fig. 6(f)).
- **Stop criteria.** There is no means of deciding when an optimum input has been found and the evolutionary algorithm should be stopped [63]. Therefore, we decided to allow the algorithm to continue for a given number of executions of the fitness function taking the largest number of backtracks obtained as the optimum, i.e. solution to the problem.

Table 1 depicts the values evaluated for each parameter. These values were based on: related works using evolutionary algorithms [22], the literature on parameter setting [4, Section E], and our previous experience in this domain [43]. Each combination of parameters was executed 10 times to avoid heterogeneous results and to allow us to

perform statistical analysis on the data. Underlined values were those providing better results and therefore those selected for the final configuration of ETHOM. In total, we performed over 40 million executions of the objective function to find a good setup for our algorithm.

Parameter	Values evaluated and selected
Selection strategy	<u>Roulette-wheel</u> , 2-Tournament
Crossover strategy	<u>One-point</u> , Uniform
Crossover probability	0.7, 0.8, <u>0.9</u>
Mutation probability	<u>0.0075</u> , 0.005, 0.02
Size initial population	50, 100, <u>200</u>
#Executions fitness function	2000, <u>5000</u>
Infeasible individuals	Replacing, <u>Repairing</u>

**Table 1:** Algorithm configuration

## 4. Evaluation

In order to evaluate our approach, we developed a prototype implementation of ETHOM in Java. The program was developed on top of the BeTTY Framework [14], an open-source tool for functional and performance testing on the analysis of feature models developed by the authors.

In general, it is not possible to verify that the solution obtained by ETHOM represents a global optimum. Although there are static techniques that could be used for this (e.g. control flow graph analysis), these are not affordable in general for large complex software [63]. Thus, we decided to evaluate the efficacy of our approach by comparing it to random search since this is the most extended strategy for performance testing in the analysis of feature models. In particular, the evaluation of our evolutionary program was performed through a number of experiments. On each experiment, we compared the effectiveness of random generators and ETHOM on the search of feature models maximizing properties such as the execution time or memory consumption required for their analysis. Additionally, we performed some extra experiments studying the characteristics of the hard feature models generated and the behaviour of ETHOM when allowed to run for a large number of generations. The results of these extra experiments as well as the statistical analysis of the data are briefly mentioned in this section and fully reported in an external technical report due to space limitations [49].

All the experiments were performed on a cluster of four virtual machines equipped with an Intel Core 2 CPU 6400@2.13GHz running Centos OS 5.5 and Java 1.6.0\_20 on 1400 MB of dedicated memory. These virtual machines ran on a cloud of servers equipped with Intel Core 2 CPU 6400@2.13Ghz and 4GB of RAM memory managed using Opennebula 2.0.1.



## 4.1. Experiment #1: Maximizing execution time

In this experiment, we evaluated the ability of ETHOM to search for input feature models maximizing the analysis time of a solver. In particular, we measured the execution time required by a CSP solver to find out if the input model was consistent (i.e. it represents at least one product). This was the same problem used to tune the configuration of our algorithm. Again, we chose the consistency operation because it is currently the most used in the literature. Next, we present the setup and results of our experiment.

### 4.1.1. Maximizing execution time in a CSP Solver

**Experimental setup.** This experiment was performed through a number of iterative steps. On each step, we generated 5,000 random feature models and checked their consistency saving the maximum fitness obtained. Then, we executed ETHOM and allowed it to run for the same number of executions of the fitness function (5,000) and compared the results. We may recall that the size of population in our algorithm was set to 200 individuals which meant that the maximum number of generations was 25, i.e. 5,000/200. This process was repeated with different model sizes to evaluate the scalability of our algorithm. In particular, we generated models with different combinations of features, {200, 400, 600, 800, 1,000} and percentage of constraints (with respect to the number of features), {10%, 20%, 30%, 40%}. The maximum branching factor was set to 10 in all the experiments. For each model size, we repeated the process 25 times to get averages and perform statistical analysis of the data. In total, we performed about 5 million executions<sup>1</sup> of the fitness function for this experiment. The fitness was set equal to the number of backtracks obtained by the analysis tool when checking the model consistency. For the analysis, we used the solver JaCoP integrated into FaMa v1.0 with the default heuristics *MostConstrainedDynamic* for the selection of variables and *IndomainMin* for the selection of values from the domains. To prevent the experiment from getting stuck, a maximum timeout of 30 minutes was used for the execution of the fitness function in both the random and evolutionary search. If this timeout was exceeded during random generation, the execution was cancelled and a new iteration was started. If the timeout was exceeded during evolutionary search, the best solution found until that moment was returned. After all the executions, we measured the execution time of the hardest feature models found for a full comparison, i.e. those producing a larger number of backtracks. More specifically, we executed 10 times each returned solution to get average execution times.

**Analysis of results.** Fig. 7 depicts the effectiveness of ETHOM for each size range of the feature models generated. We define the *effectiveness* (a.k.a score) of our evolutionary program as the percentage of times (out of 25) in which the program found a better optimum than random models, i.e. a higher number of backtracks. As illustrated, the effectiveness of ETHOM was over 80% in most of the size ranges reaching 96% or higher in nine of them. Overall, our evolutionary program found harder feature models

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<sup>1</sup>5 features ranges x 4 constraints ranges x 25 iterations x 10,000 (5,000 random search + 5,000 evolutionary search)

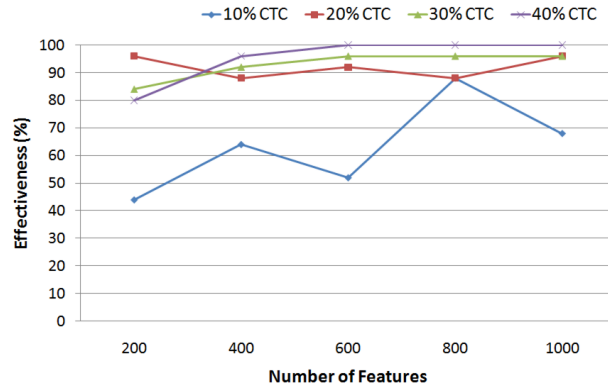


Figure 7: Effectiveness of ETHOM in Experiment #1.

than those generated randomly in 85.8% of the executions. We may remark that our algorithm revealed the lowest effectiveness with those models containing 10% of cross-tree constraints. We found that this was due to the simplicity of the analysis in this size range. The number of backtracks produced by these models was very low, zero in most cases, and thus ETHOM had problems finding promising individuals that could evolve towards optimal solutions.

Table 3 depicts the evaluation results for the range of feature models with 20% of cross-tree constraints. For each number of features and search technique, random and evolutionary, the table shows the average and maximum fitness obtained as well as the average and maximum execution times of the hardest feature models found. The effectiveness of the evolutionary program is also presented in the last column. As illustrated, the evolutionary program found feature models producing a number of backtracks larger by several orders of magnitude than those produced by random models. The fitness of the hardest models generated using our evolutionary approach was on average over 3,500 times higher than that of random models ( 200,668.05 backtracks against 45.35) and 40,500 times higher in the maximum value (23.5 million backtracks against 1,279). As expected, these results were also reflected in the execution times. On average, the CSP solver invested 0.06 seconds to analyse the random models and 8.96 seconds to analyse those generated using our evolutionary generator. The superiority of evolutionary search was especially remarkable in the maximum times ranging from the 0.2 seconds of random models to the 1,032.19 seconds (17.2 minutes) invested by the CSP solver to analyse the hardest feature model generated by our evolutionary program. Overall, our evolutionary approach produced a harder feature model than random techniques in 92% of the executions in the range of 20% of constraints.

Tables 2, 4, and 3 depict the evaluation results for feature models with 10%, 30%, and 40% of cross-tree constraints respectively. Like in Table 3, Tables 2, 4, and 5 show the average and maximum fitness obtained, as well as the average and maximum execution times of the hardest feature models found, and the effectiveness of ETHOM in the last column. It is important to note that the effectiveness of ETHOM is higher than 80% on all the cases of tables 4, and 3, supporting the conclusions stated above. However, table 2 shows a significantly lower effectiveness, drawing a limitation in the applicability of the proposal.

A global summary of the results is presented in Table 6. The table depicts the max-

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	5.24	17	20.97	38.90	24.64	361.00	27.77	60.50	44
400	11.72	96	35.06	51.80	417.60	7871.00	57.97	330.40	64
600	28.56	287	50824.00	96.30	72508.72	1780227.00	2525.58	59862.30	52
800	15.16	87	61.25	89.00	336715.28	5316995.00	18007.71	280405.60	88
1000	40.6	186	94.09	120.70	1184620.60	29491237.00	66244.50	1643863.60	68
<b>Total</b>	<b>20.256</b>	<b>287</b>	<b>10207.07</b>	<b>120.70</b>	<b>318857.37</b>	<b>29491237.00</b>	<b>17372.71</b>	<b>1643863.60</b>	<b>63.2</b>

**Table 2:** Evaluation results on the generation of feature models maximizing execution time in a CSP solver. CTC=10%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	8.08	61	0.02	0.03	63.36	215	0.04	0.06	96
400	30.08	389	0.04	0.07	7,128.44	106,655	0.24	2.93	88
600	40.28	477	0.05	0.09	9,188.20	116,479	0.70	7.98	92
800	91.08	1,279	0.08	0.20	22,427.60	483,971	1.28	24.56	88
1000	57.24	582	0.10	0.13	964,532.64	23,598,675	42.54	1,032.19	96
<b>Total</b>	<b>45.35</b>	<b>1,279</b>	<b>0.06</b>	<b>0.20</b>	<b>200,668.05</b>	<b>23,598,675</b>	<b>8.96</b>	<b>1,032.19</b>	<b>92</b>

**Table 3:** Evaluation results on the generation of feature models maximizing execution time in a CSP solver. CTC=20%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	10.4	32	22.94	37.20	526.00	8069.00	52.16	171.30	84
400	19.28	103	35.57	41.90	1212.56	21696.00	93.46	611.00	92
600	11.72	26	48.99	64.10	8826.72	214536.00	345.91	6621.50	96
800	18.32	80	70.31	97.50	11487.36	174361.00	787.81	13940.30	96
1000	23.08	170	87.78	117.20	1510.76	15372.00	287.13	1617.10	96
<b>Total</b>	<b>16.56</b>	<b>170</b>	<b>53.12</b>	<b>117.20</b>	<b>4712.68</b>	<b>214536.00</b>	<b>313.29</b>	<b>13940.30</b>	<b>92.8</b>

**Table 4:** Evaluation results on the generation of feature models maximizing execution time in a CSP solver. CTC=30%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	9,6	39	25,78	35,50	132,24	959,00	38,26	83,10	80
400	11,28	56	39,00	75,90	131,76	987,00	56,45	130,80	96
600	8,76	31	50,09	68,80	6224,72	77181,00	352,03	4087,10	100
800	7,64	14	64,50	85,90	386,84	4299,00	111,38	519,00	100
1000	8,24	19	82,09	101,40	133,72	949,00	120,36	274,80	100
<b>Total</b>	<b>9,104</b>	<b>56</b>	<b>52,29</b>	<b>101,40</b>	<b>1401,86</b>	<b>77181,00</b>	<b>135,70</b>	<b>4087,10</b>	<b>95,2</b>

**Table 5:** Evaluation results on the generation of feature models maximizing execution time in a CSP solver. CTC=40%

imum execution times invested by the CSP solver to analyse the hardest models found using random and evolutionary search. The data show that our approach was more effective than random models in all size ranges. The hardest random model required 0.2 seconds to be processed. In contrast, our evolutionary approach found four models requiring between 1 and 27.3 minutes to be analysed. Interestingly, our algorithm was able to find smaller and significantly harder feature models (e.g. 600 features and 10% of CTC) than the hardest random model found which had 800 features and 20% of constraints. This emphasizes the ability of our approach to generate motivating input models of realistic size that reveal the vulnerabilities of tools and heuristics instead of just stressing them using large random models.

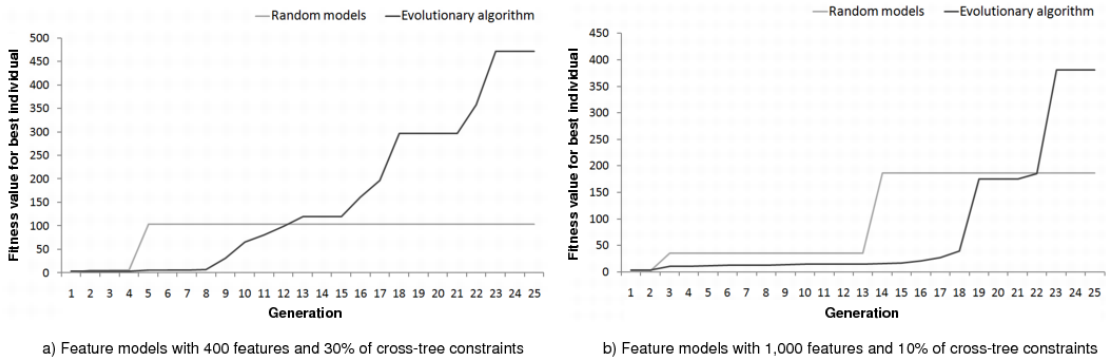
#Features	10% CTC		20% CTC		30% CTC		40% CTC	
	Random Time	ETHOMTime	Random Time	ETHOMTime	Random Time	ETHOMTime	Random Time	ETHOMTime
200	0.04	0.06	0.03	0.06	0.04	0.17	0.04	0.08
400	0.05	0.33	0.07	2.93	0.04	0.61	0.08	0.13
600	0.10	59.86	0.09	7.98	0.06	6.62	0.07	4.09
800	0.09	280.41	0.20	24.56	0.10	13.94	0.09	0.52
1,000	0.12	1,643.86	0.13	1,032.19	0.12	1.62	0.10	0.27

**Table 6:** Maximum execution times produced by random models and our evolutionary program.

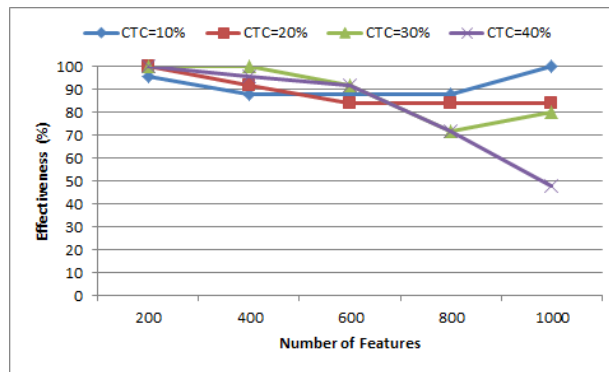
Fig. 8 compares random and evolutionary techniques for the search of a feature model maximizing the number of backtracks in two sample executions. This occurred because the results obtained by our evolutionary program were so much higher than those of random models that it was unfeasible to represent them using a similar scale. Horizontally, the graphs show the number of generations where each generation represent 200 executions of the fitness function. Fig. 8(a) shows that random models reaches its maximum number of backtracks after only 5 generations (about 1000 executions). That is, the generation of 4,000 other random models do not produce any higher number of backtracks and therefore are useless. In contrast to this, our evolutionary approach shows a continuous improvement. After 13 generations (about 2600 executions), the fitness found by evolutionary search are above of those of random models. Fig. 8(b) depicts another example in which random models are lucky to find a high number of backtracks in the 14th generation. Evolutionary optimization, however, once again manages to improve the execution times continuously overcoming the best random fitness after 22 generations. In generation number 23, even a significant leap of about 200 backtracks can be observed. In both examples, the curve trace suggests that the evolutionary algorithm would find even better solutions if the number of generations were increased. This was confirmed in a later experiment in which the program was allowed to run for up to 125 generations (25,000 executions of the fitness function) finding feature models producing more than 70 million backtracks (see Section 4.5 for details).

#### 4.1.2. Maximizing execution time in a SAT Solver

**Experimental setup.** The experimental setup used for SAT-based analysis is the equal to that used with the CSP-based one. For the analysis, we used the SAT solver integrated into FaMa v1.0. Just as in the experiment above described, in order to prevent the experiment from getting stuck, a maximum timeout of 30 minutes was used for the execution of the fitness function in both the random and evolutionary search. If this



**Figure 8:** Comparison of random models and our evolutionary algorithm for the search of the highest number of backtracks



**Figure 9:** Effectiveness of our evolutionary algorithm in Experiment #1.

time was exceeded, a new iteration was started. After all the executions, we measured the execution time of the hardest feature models found for a full comparison, i.e. those producing a larger number of backtracks. More specifically, we executed 10 times each optimal solution to get average execution times.

**Analysis of results.** Fig. 9 depicts the effectiveness of our algorithm for each size range of the feature models generated. As illustrated, the effectiveness of evolutionary program was over 80% in most of the cases reaching 92% or higher in nine of them. Overall, our evolutionary program found harder feature models than those generated randomly in 87.8% of the executions.

Tables 7, 8, 9, and 10 depict the evaluation results obtained using the SAT-based analysis for feature models with 10%, 20% 30%, and 40% of cross-tree constraints respectively. Specifically, those tables show the average and maximum fitness obtained, as well as the average and maximum execution times of the hardest feature models found, and the effectiveness of ETHOM in the last column.

## 4.2. Experiment #2: Maximizing memory consumption in a BDD solver

In this experiment, we evaluated the ability of ETHOM to generate input feature models maximizing the memory consumption of a solver. In particular, we measured the memory consumed by a BDD solver when finding out the number of products represented

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	100.64	121.00	35.72	146.50	148.44	208.00	29.54	59.70	96
400	163.76	221.00	69.53	73.70	234.72	338.00	65.38	77.60	88
600	227.64	306.00	121.63	144.00	299.84	423.00	120.72	128.20	88
800	289.20	397.00	188.85	201.30	390.36	546.00	188.87	199.40	88
1000	316.88	463.00	270.38	316.10	504.88	703.00	287.44	313.20	100
<b>Total</b>	219.62	463.00	137.22	316.10	315.65	703.00	138.39	313.20	92

**Table 7:** Evaluation results on the generation of feature models maximizing execution time in a SAT solver. CTC=10%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	97.64	116.00	31.79	36.10	151.44	244.00	28.72	33.60	100
400	164.36	211.00	75.18	83.20	230.28	406.00	691.72	76.90	92
600	219.36	285.00	12.61	133.90	303.36	408.00	126.80	137.30	84
800	278.44	398.00	198.87	210.60	317.24	399.00	197.79	224.40	84
1000	321.80	457.00	282.14	291.60	422.32	582.00	299.70	312.00	84
<b>Total</b>	216.32	457.00	120.12	291.60	284.93	582.00	268.95	312.00	88.8

**Table 8:** Evaluation results on the generation of feature models maximizing execution time in a SAT solver. CTC=20%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	92.96	116	33.16	35.00	146.52	257.00	28.95	37.40	100
400	131.72	164	78.48	84.60	190.84	252.00	74.12	83.00	100
600	176.24	229	134.12	150.30	252.64	356.00	133.52	143.40	92
800	218.04	276	207.63	247.40	257.36	388.00	212.49	256.50	72
1000	227.4	280	297.06	315.00	271.48	395.00	311.38	334.30	80
<b>Total</b>	169.27	280.00	150.09	315.00	223.77	395.00	152.09	334.30	88.8

**Table 9:** Evaluation results on the generation of feature models maximizing execution time in a SAT solver. CTC=30%

#Features	Random Testing				ETHOM				Score (%)
	Avg Fitness	Max Fitness	Avg Time	Max Time	Avg Fitness	Max Fitness	Avg Time	Max Time	
200	79.96	130	35	39.1	133.52	181	30	33.1	100
400	108.88	147	82.34	87.5	174.88	244	78	85.7	96
600	137.08	190	140	149.1	184.12	298	141	157.6	92
800	145.28	206	217.64	242.8	181.96	334	223	257.6	72
1000	145.68	216	310	320.5	150.92	214	328	364	
<b>Total</b>	117.8	206	118.661	242.8	168.62	334	118.018	257.6	90

**Table 10:** Evaluation results on the generation of feature models maximizing execution time in a SAT solver. CTC=40%

by the model. We chose this analysis operation because it is the hardest one in terms of complexity and it is currently the second operation most quoted in the literature [10]. We decided to use a BDD-based reasoner for this experiment since it has proved to be the most efficient option to perform this operation in terms of time [10]. A *Binary Decision Diagram* (BDD) solver is a software package that takes a propositional formula as input and translates it into a graph representation (the BDD itself) that provides efficient algorithms for counting the number of possible solutions. The number of nodes of the BDD is a key aspect since it determines the consumption of memory and can be exponential in the worst case [40]. Next, we present the setup and results of our experiment.

**Experimental setup.** The experiment consisted of a number of iterative steps. At each step, we generated 5,000 random models and compiled each of them into a BDD for counting the number of solutions measuring its size. We then executed our evolutionary program and allowed it to run for 5,000 executions of the fitness function looking for feature models maximizing the size of the BDD and compared the results. Again, this process was repeated with different combination of features, {50, 100, 150, 200, 250} and percentage of constraints, {10%, 20%, 30%} to evaluate the scalability of our approach. For each size of the model, we repeated the process 25 times to get statistics from the data. In total, we performed 3.75 million executions of the fitness function for this experiment. We may remark that we generated smaller feature models than those presented in previous experiment in order to reduce BDD building time and make the experiment affordable. Measuring memory usage in Java is difficult and computationally expensive since memory profilers usually add a significant overload to the system. To simplify the fitness function, we decided to measure the fitness of a model as the number of nodes of the BDD representing it. This is a natural option used in the research community to compare the space complexity of BDD tools and heuristics [40]. For the analysis, we used the solver JavaBDD integrated into the feature model analysis tool SPLOT. We chose SPLOT because it integrates highly efficient ordering heuristics specifically designed for the analysis of feature models using BDDs. In particular, we used the heuristic ‘*Pre-CL-MinSpan*’ presented by Mendonca et al. in [40]. As in our previous experiment, we set a maximum timeout of 30 minutes for the fitness function to prevent the experiment from getting stuck when finding too good solutions. After all the executions, we measured the compilation and execution time of the hardest feature models found for a more detailed comparison, i.e. those producing a largest BDD. Each optimal solution was compiled and executed 10 times to get average times.

**Analysis of results.** Fig. 10 depicts the effectiveness of ETHOM for each size range of the feature models generated, i.e. percentage of times (out of 25) in which evolutionary search found feature models producing higher memory consumption than random models. As illustrated, the effectiveness of ETHOM was over 96% in most of the cases reaching 100% in 10 out of the 15 size ranges. The lowest percentages were registered in the range of 250 features. When analysing the results, we concluded that this was not a limitation but a proof of the quality of the solutions found. In particular, we found that timeout of 30 minutes was reached frequently in the range of 250 features hindering ETHOM from evolving toward promising solutions. In other words, the feature model generated were so hard that they often took more than 30 minutes to be analyzed and

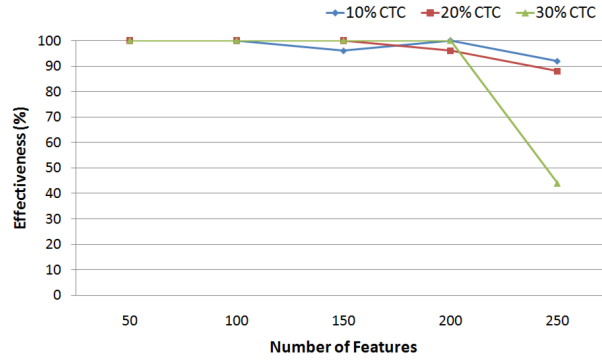


Figure 10: Effectiveness of ETHOM in Experiment #2.

were discarded. In fact, the maximum timeout was reached 18 times during random generation and 62 times during evolutionary search, 25 of them in the range of 250 features and 30% of constraints. In this size range, ETHOM exceeded the timeout after only 7 generations on average (25 being the maximum). Overall, ETHOM found feature models producing higher memory consumption than random models in 94.4% of the executions. The results suggest, however, that increasing the maximum timeout would increase the effectiveness significantly.

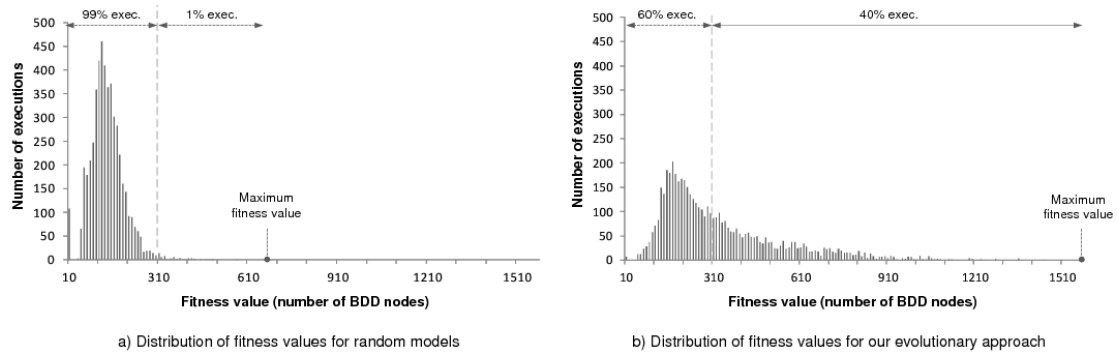
Table 11 depicts the number of BDD nodes of the hardest feature models found using random and evolutionary search. For each size range, the table also shows the computation time (BDD building time + execution time) invested by SPLOT to analyse the model. As illustrated, ETHOM found higher maximum values than random techniques in all size ranges. On average, the BDD size found by our evolutionary approach was between 1.03 and 10.3 times higher than those obtained with random models. The largest BDD generated from random models had 14.8 million nodes while the largest BDD obtained using ETHOM had 20.6 million nodes. Again, results revealed that ETHOM was able to find smaller but harder models (e.g. 150-30%, 17.7 million nodes) than the hardest random model found, 250-30% 14.8 million nodes. We may recall that the maximum timeout was reached 62 times during the execution of ETHOM. This result suggests that the maximum found by evolutionary search would have been much higher if we would not have limited the time to make the experiment affordable. As expected, the superiority of ETHOM was also observed in the computation times required by each model to be compiled and analysed. This suggests that our approach can also deal with optimization criteria involving compilation time in BDD solvers.

#Features	10% CTC				20% CTC				30% CTC			
	Random		Evolutionary		Random		Evolutionary		Random		Evolutionary	
	BDD size	Time	BDD Size	Time	BDD size	Time	BDD Size	Time	BDD size	Time	BDD Size	Time
50	781	0	1,963	0	2,074	0	8,252	0.01	2,455	0.01	10,992	0.01
100	7,629	0.01	20,077	0.02	33,522	0.03	161,157	0.20	95,587	0.08	419,835	0.73
150	65,627	0.10	188,985	0.31	374,675	0.91	3,060,590	12.80	673,410	1.28	11,221,303	24.22
200	203,041	0.09	924,832	0.86	2,735,005	4.34	19,698,780	75.05	3,394,435	58.22	23,398,161	380.52
250	1,720,983	3.69	7,170,121	25.94	25,392,597	82.28	27,970,630	253.32	20,579,015	343.72	22,310,416	431.62

Table 11: BDD size and computation time of the hardest feature models found using random techniques and our evolutionary program.

Fig. 11 shows the frequency with which each fitness value was found during the search of a feature model producing the largest BDD. The data presented corresponds





**Figure 11:** Histograms with the distribution of fitness values for random and evolutionary techniques when searching for a feature model maximizing the size of the BDD.

to the hardest feature models generated in the range of 50 features and 10% of cross-tree constraints. We chose this size range because it produced the smallest BDD sizes and facilitated the comparison of the results of both techniques using the same scale. For random models (Fig. 11(a)), a narrow Gaussian-like curve is obtained with more than 99% of the executions producing fitness values under 310 BDD nodes. During evolutionary execution (Fig. 11(b)), however, a wider curve is obtained with 40% of the execution producing values over 310 nodes. Both histograms clearly show how evolutionary programming performed a more exhaustive search in a larger portion of the solution space than that explored by random models. This trend was also observed in the rest of size ranges.

### 4.3. Experiment #3: Evaluating the impact of the number of generations

During the work with ETHOM, we detected that the maximum number of generations used as stop criterion had a great impact in the results of the algorithm. In this experiment, we evaluated that impact with a double aim. First, we tried to find out the minimum number of generations required by ETHOM to offer better results than random techniques on the search of hard feature models. Second, we wanted to find out whether ETHOM was able to find even harder models than in our previous experiments when allowed to run for a large number of generations. Next, we present the setup and results of our experiment.

**Experimental setup.** We repeated Experiments #1 and #2 using different number of generations from 10 to 25, 50, 75, 100 and 125. To make the experiments affordable, we used a fixed size for the models being generated. In particular, we searched for: *i*) feature models with 500 features and 20% CTCs maximizing the number of backtracks in the CSP solver JaCoP, and *ii*) feature models with 100 features and 20% CTCs maximizing the number of BDD nodes in JavaBDD. In total, we performed over 7.5 million executions of the fitness functions for this experiment. A timeout of 30 minutes was used for all the executions.

**Analysis of results.** Table 12 depicts the results for this experiments. For each number of generations (i.e. stop criterion), the maximum fitness and the effectiveness of both random and evolutionary search are presented. The results revealed that the effectiveness of ETHOM was around 96% (CSP solver) and 100% (BDD solver) when the number of generations was 25 or higher. More importantly, we found that the results provided by evolutionary search were better and better as the number of generations was increased without reaching a clear peak meanwhile the results of random search showed little or no improvement at all. In the execution with the CSP solver, ETHOM produced a new maximum fitness of more than 77 million backtracks meanwhile random search found a maximum value of only 1,603 backtracks. Similarly, the maximum random fitness produced in our experiment with BDD was 89,779 nodes, far from the best fitness obtained by our evolutionary program, 22.7 million nodes. Finally, we may emphasize that the maximum number of BDD nodes found by ETHOM in the range of 125 generations (22.2 million nodes) was 120 times higher than the maximum obtained when using 25 generations as stop criterion (185,203 nodes). This shows the power of ETHOM when it is allowed to run for a long number of generations.

#Generations	CSP Solver (fitness=#backtracks)			BDD Solver (fitness=#BDD nodes)		
	Random Fitness	ETHOM Fitness	Score (%)	Random Fitness	ETHOM Fitness	Score (%)
10	1,603	258	84	36,975	46,023	92
25	588	34,185	96	33,876	185,203	100
50	234	1,123,030	96	89,779	1,531,579	100
75	573	25,603,183	96	66,950	10,831,443	100
100	917	15,085,200	92	38,267	22,714,010	100
125	438	77,635,583	96	80,101	22,237,169	100
<b>Max</b>	<b>1,603</b>	<b>77,635,583</b>	<b>96</b>	<b>89,779</b>	<b>22,714,010</b>	<b>100</b>

**Table 12:** Maximum fitness values obtained in Experiment #3

## 4.4. Experiment #4: Evaluating the generalizability of hardness of Feature Models

In this experiment, we checked whether the hard feature models generated by ETHOM- for a specific tool and configuration were also hard for other tools and heuristics. In particular, we first checked whether the hardest feature models found in Experiment 1 using a CSP solver were also hard when using a SAT solver. The results showed, as expected, that all models were trivially analyzed in a few seconds. Then, we repeated the analysis of the hardest feature models found in Experiment 1 using the other seven heuristics available in the CSP solver JaCoP. This last experiment is described in detail in this section.

**Experimental setup.** In this experiment we fixed the value generation heuristic of the CSP solver JaCoP to “IndomainMin”, and repeated the analysis of the hardest feature models found in Experiment 1 using the other seven heuristics available for variable selection,  $\{MaxRegret, LargestMin, SmallestMax, MostConstrainedDynamic, SmallestMin, MinDomainOverDegree, LargestDomain, SmallestDomain\}$ . A timeout of 30 minutes was used for all executions.

Features	% CTC	Variable Selection Heuristic							
		MaxRegret	LargestMin	SmallestMax	MostConstrainedDynamic	SmallestMin	MinDomainOverDegree	LargestDomain	SmallestDomain
200	10	383645.0	1.65E+14	383645.0	361.0	383645.0	361.0	Ex. time > 3600	383645.0
200	20	56.0	3043.0	56.0	215.0	56.0	215.0	65987.0	56.0
200	30	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	8069.0	Ex. time > 3600	8069.0	Ex. time > 3600	Ex. time > 3600
200	40	200.0	602.0	200.0	959.0	200.0	959.0	417858.0	200.0
400	10	159652.0	Ex. time > 3600	159652.0	7871.0	159652.0	7871.0	Ex. time > 3600	159652.0
400	20	5.0	6.0	5.0	106655.0	5.0	106655.0	Ex. time > 3600	5.0
400	30	649.0	Ex. time > 3600	649.0	21696.0	649.0	21696.0	Ex. time > 3600	649.0
400	40	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	987.0	Ex. time > 3600	987.0	Ex. time > 3600	Ex. time > 3600
600	10	1.0	11.0	1.0	1780227.0	1.0	1780227.0	Ex. time > 3600	1.0
600	20	2507.0	1407.0	2507.0	116479.0	2507.0	116479.0	Ex. time > 3600	2507.0
600	30	1.0	5.0	1.0	214536.0	1.0	214536.0	Ex. time > 3600	1.0
600	40	13.0	17542.0	13.0	77181.0	13.0	77181.0	Ex. time > 3600	13.0
800	10	43.0	3205.0	43.0	5316995.0	43.0	5316995.0	Ex. time > 3600	43.0
800	20	39.0	2897.0	39.0	483971.0	39.0	483971.0	Ex. time > 3600	39.0
800	30	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	174361.0	Ex. time > 3600	174361.0	Ex. time > 3600	Ex. time > 3600
800	40	1.0	1.0	1.0	4299.0	1.0	4299.0	Ex. time > 3600	1.0
1000	10	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	2.95E+14	Ex. time > 3600	2.95E+14	Ex. time > 3600	Ex. time > 3600
1000	20	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	2.36E+14	Ex. time > 3600	2.36E+14	Ex. time > 3600	Ex. time > 3600
1000	30	Ex. time > 3600	Ex. time > 3600	Ex. time > 3600	15372.0	Ex. time > 3600	15372.0	Ex. time > 3600	Ex. time > 3600
1000	40	1093.0	2090.0	1093.0	949.0	1093.0	949.0	Ex. time > 3600	1093.0

**Table 13:** Number of backtracks generated in the analysis of the hardest FMs of Exp. 1 with different variable selection heuristics in JaCoP

**Analysis of results.** Table 13 shows the number of backtracks generated in the analysis of the hardest FMs of Exp. 1 with different variable selection heuristics in JaCoP. The two first columns of this table identify the feature model used for the analysis in this row. For instance, the feature model used in the first data row was the hardest obtained in experiment 1 with 200 feature and 10% of CTC. The results have shown that the hardest feature models found in our experiment, using the heuristic “MostConstrained-Dynamic”, were trivially solved by some of the others heuristics. This finding supports our working hypothesis: feature models that are hard to analyse by one tool or technique could be trivially processed by others and vice-versa. Hence, we conclude that using standard set of problems, random or not, is therefore not sufficient for a full evaluation of the performance of different tools. Instead, as in our approach, the characteristics of the techniques and tools under evaluation must be carefully examined to identify their strengths and weaknesses providing helpful information for both users and developers. Hence, for instance, the hardest model in the range of 800 features and 10% CTC produced 5.3 million backtracks when using the heuristic “MostConstrainedDynamic”, and only 43 backtracks when using the heuristic “SmallestMin”.

## 4.5. Discussion

As a part our evaluation, we also studied the characteristics of the hardest feature models generated using our evolutionary approach in the experiments with CSP, SAT and BDD solvers, presented in Table 14. The data reveals that the models generated have a fair proportion of all different relationships and constraints. This is interesting since ETHOM was free to remove any type of relationship or constraints from the model if this helped to make it harder, but this did not happen in our experiments. We recall that the only constraints imposed by our algorithm are those regarding the number of features, number of constraints and maximum branching factor. Another piece of evidence is that differences between the minimum and maximum percentages of each modelling element are considerably small. More importantly, the average percentages found are very similar to those of feature models found in the literature. In [52], She et al. studied the characteristic of 32 published feature models and reported that they contain, on average, 25% of mandatory features (between 17.1% and 27.9% in our models), 44% of set subfeatures (between 37.0% and 46.3% in our models), 16% of set relationships (between 13.8% and 16.1% in our models), 6% of or-relationships (between 7.0% and 8.9% in our models) and 9% of alternative relationships (between 6.7% and 7.2% in our study). As a result, we conclude that the models generated by our algorithm are by no means unrealistic. On the contrary, in the context of our study, they are a fair reflection of the realistic models found in the literature. This suggests that the long execution times and high memory consumption detected by ETHOM could be therefore reproduced when using real models with the consequent negative effect in the user.

Modelling element	CSP Solver			SAT Solver			BDD Solver		
	Min	Avg	Max	Min	Avg	Max	Min	Avg	Max
<b>% relative to no. of features</b>									
Mandatory	25.3	27.9	31.0	20.0	25.1	28.0	10.0	17.1	24.8
Optional	27.5	34.9	45.0	30.5	36.9	44.0	18.0	35.7	46.5
Set subfeatures	29.0	37.0	41.5	31.0	37.8	45.5	34.5	46.3	62.0
Set relationships	11.0	14.1	16.0	12.0	13.8	15.3	13.3	16.1	20.0
- Or	5.5	7.0	9.0	5.5	7.1	8.3	6.0	8.9	12.0
- Alternative	5.5	7.1	8.5	4.0	6.7	8.8	3.3	7.2	10.0
<b>% relative to no. of constraints</b>									
Requires	31.3	47.5	56.6	41.1	51.9	68.4	31.0	48.5	64.3
Excludes	43.4	52.5	68.8	31.6	48.1	58.9	35.7	51.5	69.0

**Table 14:** Statistics of the hardest feature models found in our experiments.

## 4.6. Statistical Analysis

The goal of statistical analysis is to provide formal and quantitative evidences showing that the algorithm works and that the results were not obtained by mere chance. In fact, this type of analysis is considered mandatory in fields such as data mining and bio-informatics with a long experience in the analysis of experimental data. The statistical analysis of the data was performed using the SPSS 17 statistical package [25].

Statistical analysis is usually performed by formulating two contrary hypothesis. The first hypothesis is referred to as *null hypothesis* ( $H_0^i$ ) and assume that the algorithm has no impact at all on the goodness of the results obtained, i.e. there is no difference between our algorithm and random search. Opposite to the null hypothesis, an *alternative hypothesis* ( $H_1^i$ ) is formulated, stating that the algorithm has a significant effect in the quality of the results obtained. Statistical tests provide a probability (named *p-value*) ranging in  $[0,1]$ . The lower the p-value of a test is, the more likely that the null hypothesis is false and the alternative hypothesis is true, i.e. the algorithm works. Alternatively, high p-values indicates more chances of the null hypothesis being true i.e. the algorithm does not work. Researchers have established by convention that p-values under 0.05 or 0.01 are so-called *statistically significant* and are sufficient to reject the null hypothesis, i.e. prove that the algorithm is actually working.

The techniques used to perform the statistical analysis and obtain the p-values depend on whether the data follow a normal frequency distribution or not. The former assumes that data has come from a type of probability distribution and makes inferences about the parameters. The latter makes no assumptions at all. After some preliminary tests (Kolmogorov-Smirnov [30, 54] and Shapiro-Wilk [51] tests) we concluded that our data did not follow a normal distribution and thus our tests required the use of so-called non-parametric techniques. In particular, we applied the Mann-Whitney U non-parametric test [35] to the experimental results obtained with our evolutionary algorithm and random search. Tables 17 and 18 show the results of these tests in SPSS for the experiments #1 and #2 respectively. For each number of features and percentage of cross-tree constraints, the values of the test are provided. As illustrated, tests rejected null hypotheses with extremely low p-values (zero in most of the cases) for nearly all experimental configurations of both experiments. This, coupled with the results shown in previous sections, clearly shows the great superiority of our algorithm when compared to random search. Only when the percentage of cross tree constraints (CTC) was 10% in Experiment #1, statistical test accepted some null hypotheses. As explained in Section 5, this problem is due to the small complexity of the analysis on those models. This problem makes our fitness landscape extremely flat, with scarce and disperse points of high fitness, where a random algorithm can find solutions nearly as good as those found by our evolutionary algorithm. In experiment #2 all null hypotheses were rejected except for the last one. In this last hypothesis, the number of features, and percentage of cross tree constraints becomes bigger, and consequently it is easier for the random algorithm find hard feature models. Moreover, as described in section 4.2, in this case the maximum timeout of 30 minutes was reached frequently hindering the evolutionary program from evolving toward promising solutions. This effect gives the random algorithm more chance to find solutions similar to those obtained with ETHOM.

For more details about statistical tests and their meaning we refer the reader to [59].

## 5. Threats to validity

In order to clearly delineate the limitations of the experimental study, next we discuss internal and external validity threats [29].

**Internal validity.** This refers to whether there is sufficient evidence to support the conclusions and the sources of bias that could compromise those conclusions. In order to ensure internal validity of the experimental approach, experiments were performed in a randomized order and were replicated 25 times for each experimental configuration. Moreover, statistical tests were performed to ensure significance of the differences identified between the results obtained using random and evolutionary search. Finally, the experiments were executed in a cluster of virtual machines running in a powerful cloud of servers for computing-intensive tasks which provided us with a stable and efficient experimental platform.

**External validity.** This is concerned with how the experiments capture the objectives of the research and the extent to which the conclusions drawn can be generalized. This can be mainly divided into:

- *Limitations of the approach.* Experiments showed no significant improvements when using ETHOM with problems of low complexity, i.e. feature models with 10% of constraints in Experiment #1. As stated in section 4.1, this limitation is due to the extremely flat shape of fitness landscape found in simple problems in which most fitness values are equal or close to zero. Another limitation of the experimental approach is that experiments for extremely hard feature models become too time consuming, e.g. feature models with 250 features in Experiment #2. This threat is caused by the nature of hard feature models we intend to find. As the analysis of those promising feature models becomes more time consuming and memory intensive, evaluating fitness function becomes a difficult task leading to a collapse in the experiment or to a nearly nil advance of the experiment execution along time. We may remark, however, that this limitation is intrinsic to the problem of looking hard feature models and thus it equally affects random search. Finally, we emphasize that in the worst case ETHOM behaves randomly equalling the strategies for the generation of hard feature models used in the current state of the art.
- *Generalizability of the conclusions.* In our experiments, we used two different analysis operations which could seem not to be sufficient to generalize the conclusions of our study. We remark, however, that these operations are currently the most quoted in the literature, have significantly different complexity and, more importantly, are the basis for the implementation of many other analysis operations on feature models [10]. Thus, feature models that are hard to analyze for these operations would certainly be hard to analyze for those operations that use them as an auxiliary function making our results extensible to other analyses. Similarly, we just used two different analysis tools for the experiments, FaMa and SPLOT. However, these tools are developed and maintained by independent laboratories providing a sufficient degree of heterogeneity for our study. Finally, the results revealed that the properties of the hard feature models generated are similar to those models found in the literature and therefore there is little threat to validity due to the lack of realism of the generated models.

## 6. Related work

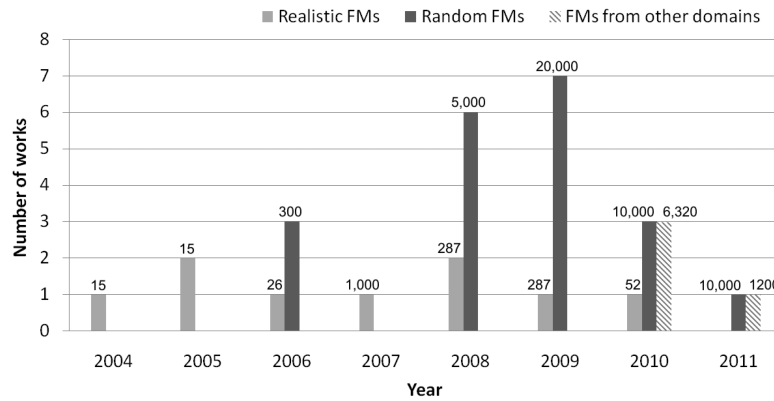
A number of authors have used realistic feature models to evaluate and show the performance of their tools [7, 8, 9, 12, 23, 27, 40, 39, 57, 61]. By *realistic* models we intend those modelling real-world domains or a simplified version of them. Some of the realistic feature models most quoted in the literature are e-Shop [32] with 287 features, graph product line [34] with up to 64 features and BerkeleyDB [28] with 55 features. Although there are reports from the industry of feature models with hundreds or even thousands of features [6, 33, 56], only a portion of them is typically published. This has led authors to generate feature models automatically to show the scalability of their approaches with large problems. These models are generated either randomly [12, 11, 20, 38, 42, 47, 64, 65, 66, 67, 68] or trying to imitate the properties of the realistic models found in the literature [22, 39, 57]. More recently, some authors have suggested looking for tough and realistic feature models in the open source community [13, 19, 52, 53]. As an example, She et al. [52] extract a feature model from the Linux kernel containing more than 5,000 features and compare it with publicly available realistic feature models.

Fig. 12 summarizes the number of related works using realistic and automatically generated models as well as those extracted from other variability domains per each year<sup>2</sup>. For each type of model, we also show the number of features of the largest feature model for each year. As illustrated, first works back in 2004 and 2005 used small realistic feature models in their experiments. However, since 2006, far more automatically generated feature models than realistic ones have been used. Regarding the size of the problems, there is a clear ascendant tendency ranging from the model with 15 features used in 2004 to models with 10,000 and 20,000 features used in the last years. These findings reflect an increasing concern to evaluate and compare the performance of different solutions using complex feature models. This also suggests that the only known mechanism to increase the complexity of the models is by increasing its size. When compared to previous works, our approach is the first one using a search-based strategy to exploit the internal weaknesses of the tools and techniques under evaluation rather than simply using large random models. This allows developers to focus on the search for tough models of realistic size that could reveal deficiencies in their tools rather than using huge feature models out of their scope. Similarly, users could have more information about the expected behaviour of the tools in pessimistic cases helping them to choose the tool or technique that better adapts to their needs.

Regarding related works with evolutionary algorithms, Wegener et al. [62] were the first ones using genetic algorithms to search for input situations that produce very long or very short execution times in the context of real time systems. In their experiments, they used C programs receiving hundreds or even thousands of integer input parameters. Their results showed that genetic algorithms obtained more extreme execution times with equal or less testing effort than random testing. Many authors continued the work of Wegener in the application of metaheuristic search techniques to test non-functional properties such as execution time, quality of service, security, usability or safety. For a detailed survey of these works we refer the reader to [2]. Our approach

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<sup>2</sup>Until August 2011



**Figure 12:** Type and maximum size of the feature models used in experimentation for each year

may be considered a specific application of the ideas of Wegener and later authors to the domain of feature modelling. In this sense, our main contribution is the development and configuration of a novel evolutionary algorithm to deal with optimization problems on feature models and its application to performance testing in this domain.

The application of genetic algorithms to the context of software product lines was explored by Guo et al. [22]. In their work, the authors proposed a genetic algorithm called GAFES for optimized feature selection in feature models, e.g. selecting the set of features that minimizes the total cost of the product. Compared to their work, our approach differs in several aspects. First, our work addresses a different problem domain, hard feature model generation. Second, ETHOM produces optimum feature models meanwhile GAFES produces optimum product configurations. This means that both algorithms bear no resemblance and face different challenges. For instance, GAFES uses a standard binary encoding to represent product configurations meanwhile ETHOM uses a custom array encoding to represent feature models of fixed size.

Pohl et al. [44] presented a performance comparison of nine CSP, SAT and BDD solvers on the automated analysis of feature models. As input problems, they used 90 realistic feature models with up to 287 features taken from the SPLOT repository [55]. The longest execution time found in the consistency operation was 23.8 seconds, far from the 27.5 minutes found in our work. Memory consumption was not evaluated. As a part of their work, the authors tried to find correlations between the properties of the models and the performance of the solvers. Among other results, they identified an exponential runtime increase with the number of features in CSP and SAT solvers. This is not supported by our results, at least not in general, since we found feature models producing much longer execution times than random models of larger size. Also, the authors mentioned that SAT and CSP solvers provided a similar performance in their experiment. This was not observed in our work in which the SAT solver showed to be much more efficient than the CSP solver, i.e. ETHOM was not able to find hard problems for SAT. Overall, we consider that using realistic feature model is helpful but not sufficient to understand the true nature of solvers. In contrast, our work provides the community with a limitless source of motivating problems to exploit the strengths and weaknesses of analysis tools.

Finally, we would like to remark that our approach does not intend to replace the usage of realistic or random models which have proved to be adequate to evaluate the



average performance of analysis techniques. Instead, our work complements previous approaches enabling a more exhaustive evaluation of the performance of analysis tools using hard problems.

## 7. Conclusions and future work

In this paper, we presented ETHOM, a novel evolutionary algorithm to solve optimization problems on feature models and showed how it can be used for the automated generation of computationally-hard feature models. Experiments using our evolutionary approach on different analysis operations and independent tools successfully identified input models producing much longer execution times and higher memory consumption than random models of identical or even larger size. In total, more than 50 million executions of analysis operations were performed to configure and evaluate our approach. When compared to previous works, our approach is the first one using a search-based strategy to exploit the internal weaknesses of the tools and techniques under evaluation rather than simply using large-scale random models. This allows developers to focus on the search of tough models of realistic size that could reveal deficiencies in their tools rather than using huge feature models out of their scope. Similarly, users are provided with more information about the expected behaviour of the tools in pessimistic cases helping them to choose the tool or technique that better meets their needs. Contrary to general belief, we found that the size of the models has an important impact, but not decisive, in the performance of analysis tools. Also, we found that the hard feature models generated by ETHOM had similar properties to the realistic models found in the literature. This means that the long execution times and high memory consumption detected by our algorithm could be therefore reproduced in real scenarios with the consequent negative effect in the user. In view of the positive results obtained, we expect this work to be the first of many other research contributions exploiting the benefits of ETHOM in particular and evolutionary computation in general on the analysis of feature models. In particular, we envision two main research directions to be explored by the community in the future, namely:

- **Algorithms development.** The combination of different encodings, selection techniques, crossover strategies, mutation operators and other parameters may lead to a whole new variety of evolutionary algorithms for feature models to be explored. Also, the development of more flexible algorithms would be desirable in order to deal with other feature modelling languages (e.g. cardinality-based feature models) or stricter structural constraints, e.g. enabling the generation of hard models with a given percentage of mandatory features. Also, the generation of feature models with complex cross-tree constraints (those involving more than two features) remains as an open challenge.
- **Applications.** Further applications of our algorithm are still to be explored. Some promising applications are those dealing with the optimization of non-functional properties in other analysis operations or even different automated treatments (e.g. feature models refactorings). The application of our algorithm to minimization

problems is also an open issue in which we have started to obtain promising results. Additionally, it would be nice to apply our approach to verify the time constraints of real time systems dealing with variability like those of mobile phones or context-aware pervasive systems. Last, but not least, we plan to study the hard feature models generated and try to understand what makes them hard to analyse. From the information obtained, more refined applications and heuristics could be developed leading to a more efficient tool support for the analysis of feature models.

A Java implementation of ETHOM is ready-to-use and publicly available as a part of the open-source BeTTY Framework [14].

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## A. Statistical Analysis Data

Tests of Normality				
Features	CTC	Algorithm	Kolmogorov-Smirnov (a)	Shapiro-Wilk
			p-value	p-value
200	10	ETHOM	.000	.000
		RANDOM	.001	.000
	20	ETHOM	.003	.001
		RANDOM	.000	.000
	30	ETHOM	.000	.000
		RANDOM	.000	.000
	40	ETHOM	.000	.000
		RANDOM	.004	.000
400	10	ETHOM	.000	.000
		RANDOM	.000	.000
	20	ETHOM	.000	.000
		RANDOM	.000	.000
	30	ETHOM	.000	.000
		RANDOM	.000	.000
	40	ETHOM	.000	.000
		RANDOM	.000	.000
600	10	ETHOM	.000	.000
		RANDOM	.000	.000
	20	ETHOM	.000	.000
		RANDOM	.000	.000
	30	ETHOM	.000	.000
		RANDOM	.011	.001
	40	ETHOM	.000	.000
		RANDOM	.000	.000
800	10	ETHOM	.000	.000
		RANDOM	.000	.000
	20	ETHOM	.000	.000
		RANDOM	.000	.000
	30	ETHOM	.000	.000
		RANDOM	.000	.000
	40	ETHOM	.000	.000
		RANDOM	.045	.015
1000	10	ETHOM	.000	.000
		RANDOM	.000	.000
	20	ETHOM	.000	.000
		RANDOM	.000	.000
	30	ETHOM	.000	.000
		RANDOM	.000	.000
	40	ETHOM	.000	.000
		RANDOM	.004	.000

a. Lilliefors Significance Correction

**Table 15:** Experiment #1 Normality test results



Tests of Normality				
Features	CTC	Algorithm	Kolmogorov-Smirnov (a)	Shapiro-Wilk
			p-value	p-value
50	10	RANDOM	.200*	.639
		ETHOM	.200*	.732
	20	RANDOM	.200*	.078
		ETHOM	.089	.027
	30	RANDOM	.034	.004
		ETHOM	.003	.000
100	10	RANDOM	.083	.007
		ETHOM	.005	.001
	20	RANDOM	.001	.000
		ETHOM	.000	.000
	30	RANDOM	.000	.000
		ETHOM	.000	.000
150	10	RANDOM	.194	.009
		ETHOM	.062	.009
	20	RANDOM	.008	.001
		ETHOM	.000	.000
	30	RANDOM	.005	.002
		ETHOM	.000	.000
200	10	RANDOM	.000	.000
		ETHOM	.014	.001
	20	RANDOM	.200*	.002
		ETHOM	.032	.001
	30	RANDOM	.000	.000
		ETHOM	.200*	.499
250	10	RANDOM	.000	.000
		ETHOM	.002	.000
	20	RANDOM	.083	.030
		ETHOM	.200*	.155
	30	RANDOM	.200*	.475
		ETHOM	.200*	.088

a. Lilliefors Significance Correction  
 \*. This is a lower bound of the true significance.

**Table 16:** Experiment #2 Normality Tests results

Test Statisticsa		
Features	CTC	p-value
200	10	.537
	20	.000
	30	.000
	40	.000
400	10	.289
	20	.000
	30	.000
	40	.000
600	10	.360
	20	.000
	30	.000
	40	.000
800	10	.000
	20	.000
	30	.000
	40	.000
1000	10	.123
	20	.000
	30	.000
	40	.000

**Table 17:** Experiment #1 Test Statistics

Test Statistics		
Features	CTC	p-value
50	10	.000
	20	.000
	30	.000
100	10	.000
	20	.000
	30	.000
150	10	.000
	20	.000
	30	.000
200	10	.000
	20	.000
	30	.000
250	10	.000
	20	.000
	30	.854

**Table 18:** Experiment #2 Test Statistics