

## ON-VEHICLE VISUAL TRACKER WITH DISTURBANCE REJECTION

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**Abstract:** This paper presents the synthesis and implementation of a passivity based controller designed for visual tracking of moving objects in a disturbance rejection scheme. The purpose of this application is to control the line of sight of a 2-DOF sensor platform in a moving coordinate frame, when the movement of the vehicle carrying the platform acts as a disturbance of finite energy. External torques due to vehicle movement downgrade the visual tracking performance and can cause instability and total loss of sight of the objective. These disturbances can be compensated for in an effectively manner introducing a classical  $\mathcal{L}_2$ -gain disturbance rejection scheme, widely deployed in inertial frame robotic systems. The proposed controller has been tested in a real 2-DOF platform mounted on a moving testbench that emulates different types of non-inertial vehicle surfaces.

**Keywords:** Nonlinear systems, Visual tracking, Mobile robotics, Passivity-based control

### 1. INTRODUCTION

In recent works, the theories of passive and port Hamiltonian systems have fruitfully given rise to a set of tools that successfully tackle the disturbance suppression problem in electromechanical systems. In (Van der Schaft, 1989) the properties of port-controlled Hamiltonian systems (PCH) have been stated (see also more specific approaches (Wang and Li, Internal report 2002) for multimachine power systems and (Slotine and Li, 1988) for robotic systems). These tools provide a bounded-disturbance bounded-output control in the sense of the  $\mathcal{L}_2$  gain.

On the other hand, on-vehicle sensors like satellite antennas and visual tracking systems are inherently affected by undesired perturbations due to movements in the coordinate frame where they live. These perturbations appear as Coriolis and centrifugal forces typical of non-inertial frames. Consequently, the problem of keeping a

static line of sight in this type of sensor is a disturbance rejection problem, where the disturbance can be caused by vehicle movements or by displacements of the target point (e.g. non-geostationary satellite). When tracking objectives are far, the former case is the one that more severely affects the stability of the line of sight and these will be the ones studied in this work. In vessels, the aforementioned disturbance is mainly due to sea waves and are usually approximated with sinusoidal functions. This type of signals, when amplitudes are low, are well handled in the  $\mathcal{L}_2$  disturbance attenuation framework. We will study a 2-DOF platform designed for vessel guidance and hence perturbed by wave-induced movements of the ship surface. With a laboratory setup that physically emulates different types of perturbation, we will present and analyze a visual servoing system based on the Slotine and Li controller (Slotine and Li, 1988) that guarantees  $\mathcal{L}_2$  disturbance rejection properties.

With the aim of studying the properties and effects of on-vehicle perturbations, a two degree of freedom platform has been set up on a destabilizing 2-DOF desk. A visual servoing system has been implemented with a CCD camera. When analyzing experimentally the effect of the real disturbances on the visual tracking loop, a substantial improvement of the overall behavior has been achieved with the proposed controller. These results are presented graphically.

This paper is organized as follows: in Section 2, the simplified system model of the platform is given. In Section 3, the new control structure is presented, divided in visual estimator and trajectory tracker. In Section 4, technical details of the physical setup and controller implementation are given. Section 5 presents some experimental results. Finally, a set of conclusive remarks are given in Section 6.

## 2. SYSTEM MODEL

The system consists of a platform with two degrees of freedom immersed in a non inertial reference system emulated by a destabilizing desk. The synthesis of controllers for this platform raises important challenges like the robust stabilization rejecting disturbances, visual tracking of moving objects and gyroscopic stabilization to compensate for the coordinate frame movements.

The model used (Gómez-Estern *et al.*, 2000) corresponds to the 2-DOF platform shown in Fig.1. It is composed of two main bodies: the base, whose position is determined by the azimuth angle  $\varphi$  and the head body whose coordinate is the elevation angle  $\theta$ . In our experimental setup, this system is mounted on a mechanical desk capable of turning in two axes. The whole system has four degrees of freedom, but only the two local coordinates (those of the tracker platform) are available from the built-in encoders. Therefore only the 2-DOF platform kinematics are considered, while any coupling effect due to the moving surface will be treated as a disturbance (Gómez-Estern *et al.*, 2003).

The load of the elevation axis is concentrated along the shaft, hence the potential energy is invariant and therefore discarded from the equations. The origin of the azimuth angle is arbitrary. The variable  $\theta$  is zero when both bodies are perpendicular. The generalized coordinates of the system are  $(\varphi, \theta)$ .

The equations of motion are easily obtained in Hamiltonian form. Under the assumption stated above, the total energy of the plant is reduced to the kinetic energy:

$$\frac{1}{2} [\dot{\varphi} \ \dot{\theta}] \begin{bmatrix} \Gamma(\theta) & 0 \\ 0 & I_{yy_2} \end{bmatrix} \begin{bmatrix} \dot{\varphi} \\ \dot{\theta} \end{bmatrix} \quad (1)$$

The term  $\Gamma(\theta)$  stands for

$$\Gamma(\theta) \triangleq I_{zz_1} + I_{xx_2} \sin^2(\theta) + I_{zz_2} \cos^2(\theta) \quad (2)$$

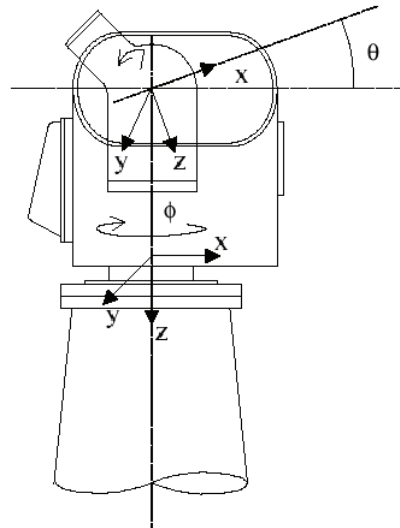


Fig. 1. Two degree-of-freedom platform.

where  $I_{zz_1}$  is the  $z$  axis inertia of the base, and  $I_{xx_2}$ ,  $I_{yy_2}$  and  $I_{zz_2}$  are the second body (elevation) inertia momenta with respect to the  $x$ ,  $y$  and  $z$  axes respectively.

## 3. VISUAL TRACKING IN NON INERTIAL VEHICLES

The visual tracking problem in this platform can be reduced in some cases to the stabilization of equilibria. Indeed, if the object to be tracked (e.g. stationary satellite) is fixed or has relatively slow motion, and the platform is installed on a static surface, an equilibrium stabilization controller with slowly varying set point will do the job. The set point is estimated by an image processing algorithm.

However if the system is immersed in a fast rotating coordinate frame, as is the case of a vehicle antenna, the performance of a set point stabilization controller with varying reference is quickly downgraded even for slow motions, as small line of sight errors due to disturbances are amplified when the tracked objects are distant. The latter case is a far more challenging tracking problem. Summarizing, the angles of the line of sight of the target with respect to the camera move by one of two causes

- Visual tracking of mobile objects from a platform on a fixed ground. This problem can be tackled as a *particular* case of the following.
- Fixed or mobile object tracking from a platform mounted on board of a ground vehicle or a vessel. The objective is to take to zero the angular velocity vector of the line-to-target when it is referred to the camera coordinate frame. This vector is actually the composition of the motion of the vehicle (or sea waves) and the reaction of the 2-DOF platforms in order to compensate it.

As the second of these situations is more general, this will be the one studied in this paper.

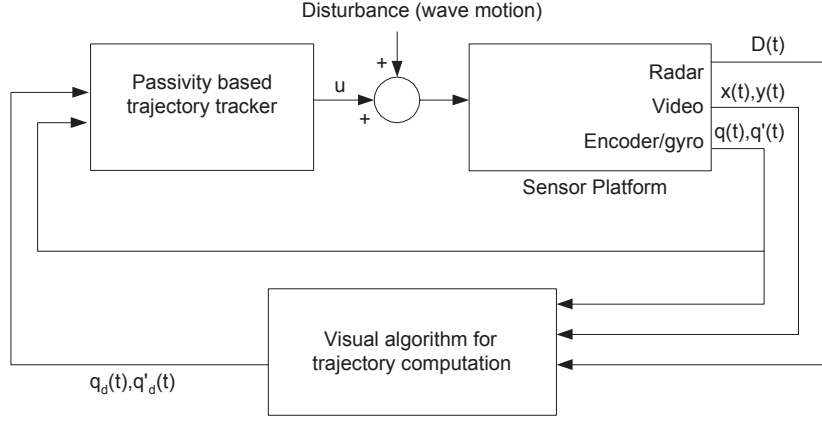


Fig. 2. Passive visual tracking scheme.

The control problem will be divided in two parts (Gómez-Estern, 2003). First, a passivity-based trajectory tracking system with disturbance suppression is designed exploiting detailed knowledge of the mechanical structure of the platform. Then, a visual tracking algorithm estimates the deviation of the tracked object from the line of sight and, based on geometric considerations, it generates the reference trajectory to be tracked by the passive system. The proposed scheme is illustrated in Fig. 2.

### 3.1 Visual tracking

The design of the first block consist of calculating the desired trajectory for the platform coordinates,  $q_d(t) = (\varphi_d(t), \theta_d(t))$  in such a way that the image of the moving object stabilizes at the center of the screen. The input of this block is a 2D vector with the  $(x, y)$  coordinates in the screen, referred to the origin at the center point. A simple image scanning algorithm computes this vector at a 10ms rate. We will assume that there is a unique trajectory  $q_d(t) \in \mathcal{C}^2$  in the local platform coordinates such that

$$q(t) \equiv q_d(t) \Rightarrow (x(t), y(t)) = (0, 0), \forall t > 0$$

This trajectory is obviously unknown, as it depends on the motion of the coordinate frame of the vehicle and the mobile target. However, as will be seen, the knowledge of the projection of the target on the screen is enough to compute the desired trajectory  $q_d(t)$  and an estimate of the derivatives at any instant  $t$ . Once  $q_d(t)$  is known, a passivity-based controller will be designed in order to ensure asymptotic stability of the trajectory and, henceforth

$$\lim_{t \rightarrow \infty} (x(t), y(t)) = (0, 0)$$

The screen coordinates of the tracked object  $(x, y)$  can be viewed as a measure of the tracking error, since these are zero if and only if the object is perfectly tracked. However it is necessary to express this error in terms of the angles of the platform joints,  $(\varphi, \theta)$ . These can be easily obtained from  $(x, y)$  as follows. Assume  $(X, Y, Z)$  are the 3D coordinates of the target in the camera coordinate

frame (see Fig. 3). By triangle equivalence, we have By triangle equivalence, we have

$$\begin{aligned} \frac{x}{d} &= \frac{X}{Z} \\ \frac{y}{d} &= \frac{Y}{Z} \end{aligned}$$

where  $d$  is the distance of the plane of the image to the viewer (this parameter can be calibrated following camera instructions). After some manipulations, the 3D coordinates are isolated

$$\begin{aligned} X &= \frac{xD}{\sqrt{d^2 + x^2 + y^2}} \\ Y &= \frac{yD}{\sqrt{d^2 + x^2 + y^2}} \end{aligned}$$

The azimuth and elevation errors of the camera in terms of  $x$  and  $y$  are given by

$$\begin{aligned} e_\varphi &= \arctan\left(\frac{X}{Z}\right) = \arctan\left(\frac{x}{d}\right) = \varphi_d - \varphi \\ e_\theta &= \arctan\left(\frac{Y}{Z}\right) = \arctan\left(\frac{y}{d}\right) = \theta_d - \theta \end{aligned}$$

Deriving this expression with respect to time, we have

$$\begin{aligned} \dot{e}_\varphi &= \frac{d}{dt} \left( \arctan \frac{X}{Z} \right) = \frac{d}{dt} \left( \arctan \frac{x}{d} \right) \\ &= \frac{\dot{x}d}{d^2 + x^2} = \dot{\varphi}_d - \dot{\varphi} \\ \dot{e}_\theta &= \frac{d}{dt} \left( \arctan \frac{Y}{Z} \right) = \frac{d}{dt} \left( \arctan \frac{y}{d} \right) \\ &= \frac{\dot{y}d}{d^2 + y^2} = \dot{\theta}_d - \dot{\theta}, \end{aligned}$$

From where we obtain the desired trajectory for the platform angles at any instant  $t$

$$q_d(t) = \begin{bmatrix} \varphi(t) \\ \theta(t) \end{bmatrix} + \begin{bmatrix} e_\varphi(t) \\ e_\theta(t) \end{bmatrix} \quad (3)$$

$$\dot{q}_d(t) = \begin{bmatrix} \dot{\varphi}(t) \\ \dot{\theta}(t) \end{bmatrix} + \begin{bmatrix} \dot{e}_\varphi(t) \\ \dot{e}_\theta(t) \end{bmatrix} \quad (4)$$

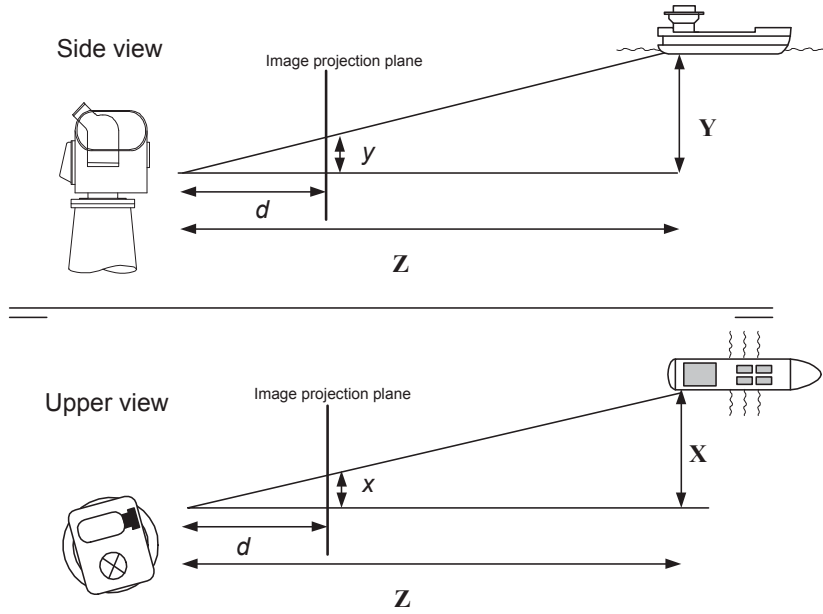


Fig. 3. Screen and real coordinates.

The generalized coordinates  $(\varphi(t), \theta(t))$  are measured in real time with the built-in encoders of the platform independently of the Euler angles of the vehicle. This real time computed target trajectory will be the reference of the passivity-based trajectory tracking controller whose design will be illustrated in the following.

### 3.2 Trajectory tracking subsystem

In order to get the trajectory tracking we will start from the Euler–Lagrange equations, and use the celebrated results of Slotine and Li (Slotine and Li, 1988). Given the nonlinear inertia matrix of the platform

$$M = \begin{bmatrix} \Gamma(\theta) & 0 \\ 0 & I_{yy2} \end{bmatrix} \quad (5)$$

we obtain the dynamic equations in open loop using the Euler-Lagrange description for robotic systems

$$M(q)\ddot{q} + C(q, \dot{q})\dot{q} = \tau, \quad (6)$$

where no potential energy terms are being considered because the head of the platform is mechanically balanced by construction (in order to reduce energy demand). If they were nonzero the treatment would be equivalent except in the fact that an inclinometer would be necessary to measure the real angles of the platform with respect to an inertial frame, in order to properly measure and compensate gravity effects. In order to asymptotically track the reference trajectory  $q_d(t)$  we will apply the control law

$$\tau = M(q)\dot{\xi} + C(q, \dot{q})\xi + \nu \quad (7)$$

where

$$\xi = \dot{q}_d - \Lambda(q - q_d) \quad (8)$$

and  $\Lambda = \Lambda^T > 0$ . Substituting in (7) yields

$$M(q)\dot{s} + C(q, \dot{q})s = \nu \quad (9)$$

where  $s \triangleq \dot{q} - \dot{\zeta}$ . Defining the energy function as

$$H(s, q) = \frac{1}{2}s^T M(q)s \quad (10)$$

then, along the trajectories (9)

$$\begin{aligned} \frac{d}{dt}H &= s^T M(q)\dot{s} + \frac{1}{2}s^T \dot{M}s \\ &= -s^T C s + \frac{1}{2}s^T \dot{M}s + s^T \nu = s^T \nu \end{aligned} \quad (11)$$

The last expression is due to the skew-symmetry of the matrix  $(\dot{M} - 2C)$ . The system is dissipative with respect to  $(s^T \nu)$  and represents a passive  $\nu \mapsto s$  because  $H \geq 0$ , for any initial condition. If, additionally, we define

$$\tilde{\nu} = Ks \quad (12)$$

where  $K = K^T > 0$  is a positive definite matrix that

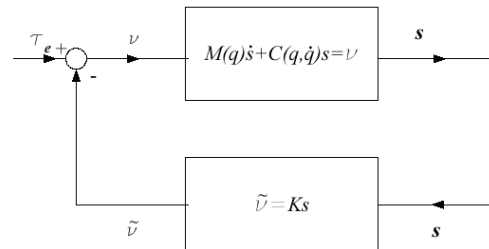


Fig. 4. Control structure for trajectory tracking

appears in the feedback block of Fig.4. Then we have that

*Proposition 1.* The control law

$$\begin{aligned}\tau = & M(q)[\ddot{q}_d - \Lambda(\dot{q} - \dot{q}_d)] \\ & + C(q, \dot{q})(\dot{q}_d - \Lambda(q - q_d)) \\ & + K_d[\dot{q} - \dot{q}_d + \Lambda(q - q_d)]\end{aligned}$$

where  $K_d = K_d^T > 0$  and  $\Lambda = \Lambda^T > 0$  are tuning parameters, and  $q_d(t)$  is the computed trajectory that must be tracked, asymptotically stabilizes the error  $e(t) = q(t) - q_d(t)$  in the origin

For more details on the proof we refer the reader to (Van der Schaft, 1989).

### 3.3 Disturbance rejection in trajectory tracking

The proposed scheme is based on the well known Slotine and Li controller (Slotine and Li, 1988), which in principle lacks of quantifiable disturbance suppression properties when the position error of the robot is taken as the output of the system. A known fact from the literature (see (Sadegh and Horowitz, 1990)) is that the addition of a term proportional to the position error to the Slotine and Li controller produces a disturbance suppression behaviour in the  $\mathcal{L}_2$ -gain sense from the input to the output  $e(t) = q_d(t) - q(t)$  with a attenuation level  $\gamma$  arbitrarily small in the case of fully actuated systems. Hence the previous proposition is transformed into

*Proposition 2.* Consider the 2-DOF platform with the control law

$$\begin{aligned}\tau = & M(q)[\ddot{q}_d - \Lambda(\dot{q} - \dot{q}_d)] \\ & + C(q, \dot{q})(\dot{q}_d - \Lambda(q - q_d)) \\ & + K_d[\dot{q} - \dot{q}_d + \Lambda(q - q_d)] + K_p(q - q_d)\end{aligned}$$

with the same constants defined in proposition 1, and suppose, additionally, that the following conditions hold:

$$\begin{aligned}K_d = & \frac{1}{2} \left( \frac{1}{\gamma^2} + 1 + \lambda \right) \\ K_p = & \frac{1}{2} (\gamma^2 + 1 + \lambda).\end{aligned}$$

Then, the  $\mathcal{L}_2$ -gain from the input  $\tau$  to the output  $(q_d - q)$  is less or equal to the arbitrarily defined gain  $\gamma$ , and the transient behavior can be adjusted using the positive scalar  $\lambda$ .

The proof of this result is based in that of (Sadegh and Horowitz, 1990). We will use it for its implementation in the real 2-DOF platform inside the visual feedback loop. But firstly we will describe, in the following section, how the information is conveyed among the different controller blocks.

## 4. IMPLEMENTATION

Figure 5 shows the experimental setup. The platform turns in two axis powered by two brushless DC motors.

The destabilizing desk is also 2-DOF and is powered by three-phase motors controlled with a velocity variator. The measurements of the position sensors (differential encoders for the desk and inclinometers for the desk) and velocities (gyroscopes) are fed back into a PC that contains two dSpace<sup>TM</sup> DSP cards (one for each axis) based on the DSP TMS320C31 processor and equipped with a control development environment ControlDesk.

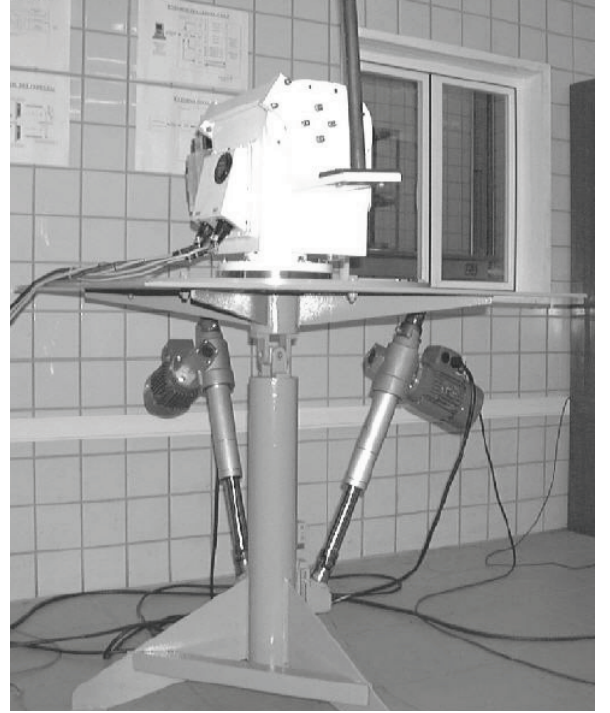


Fig. 5. Experimental setup.

For the visual tracker we have developed a simple algorithm for image scanning running on a spare PC. Such algorithm is a C++ routine that determines the screen coordinates of the tracking target  $(x, y)$ , in our experiment just a black circle printed on a white background. This image is first used to calibrate the parameters of the camera. The acquired data is packed into an UDP datagram with a time stamp and sent via Ethernet to the peer computer, where the dSpace cards are running the tracking controller in connection with the platform sensors and actuators. In order to check the validity of the proposed scheme, it has been observed that the total time in acquiring an image, identifying the angles of the target, and sending the datagram, does not exceed a total time of 20ms. Thus, with a sample period of 100ms the jitter due to unmodeled delays is not larger than 20% of the sampling time.

The PC acting as controller receives the UDP packets (no packet losses have been accounted for), finds out the error angles from the received  $(x, y)$  coordinates, and conveys the data to the DSP cards, where the value of  $q_d$  is computed according to encoder measurements and equation (3). In these processors, a Simulink<sup>TM</sup>



RTW<sup>1</sup> algorithm applies the voltage the torque to the DC servomotor of the corresponding axis .

The physical constants of the model have been obtained through least squares identification over several records on the step response captured by the DSP boards. As friction will be to some extent compensated for in the final controller. the LuGre model parameters have been identified as indicated in (Astrom K.J., 1995).

## 5. EXPERIMENTAL RESULTS

The quality of the experimental results significantly increases when our controller is enhanced with a feedforward compensator of the friction phenomena based on the LuGre model.

The elements depicted in (6) are the slow sinusoidal reference provided by the visual tracker when the destabilizing desk oscillates in sinusoidal slow motion (marine vehicle emulation), together with the position given by the encoders. The tracking controller is also artificially perturbed with a fast sinusoidal signal (included in the figure) directly added to the DC motor inputs. The small deviations between the position and the reference are due to this disturbance, which is the one to be attenuated with the robust scheme. The  $\mathcal{L}_2$ -gain of the fast disturbance-to-output map has been adjusted according to proposition 2. Although the value of  $\gamma$  can be made arbitrarily small, in experiments we have observed that it should not be chosen below a certain value due to the appearance of a sustained oscillation, possibly due to communication delays inducing a limit cycle. As a matter of fact any unmodeled oscillation is amplified through the derivative term of the controller, which is in turn increased as parameter  $\gamma$  goes smaller.

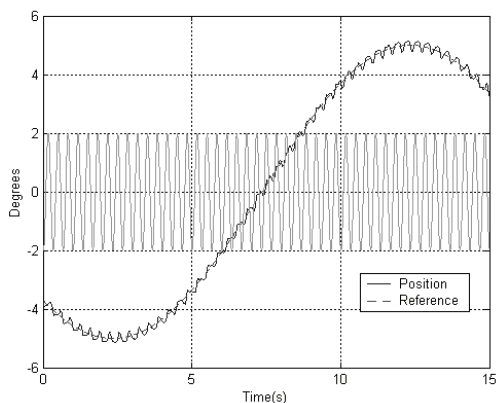


Fig. 6. Visual tracking of a fixed target with sinusoidal desk motion and additive white noise disturbance.

## 6. CONCLUSIONS

In this work we have presented the design and practical implementation of a controller based on the Slotine

and Li scheme immersed in a visual feedback loop with Ethernet data transmission. The controller is split between image processing, target trajectory computation and trajectory tracking. The latter block is a passive controller specifically designed for suppression of undesired disturbances up to a level that, in theory, can be made arbitrarily small.

The main contribution lies in the use of passivity and robustness techniques in a visual servoing framework. In the experimental results we have checked that well known control techniques designed for other domains have proved to be effective in this challenging type of application. The extension of the techniques to visual servoing systems is natural and only relies on the computation of a trajectory to be tracked as a result of a fast image analysis C++ algorithm.

The powerful experimental setup consisting of a 2-DOF sensor platform mounted on a 2-DOF destabilizing desk has allowed us to verify experimental results in a most realistic environment, and this makes us believe that the controller can be easily upgraded into the real ground and water vehicle world.

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<sup>1</sup> Real Time Workshop<sup>TM</sup>.